

Current state of Flavour Physics



Martin Bauer



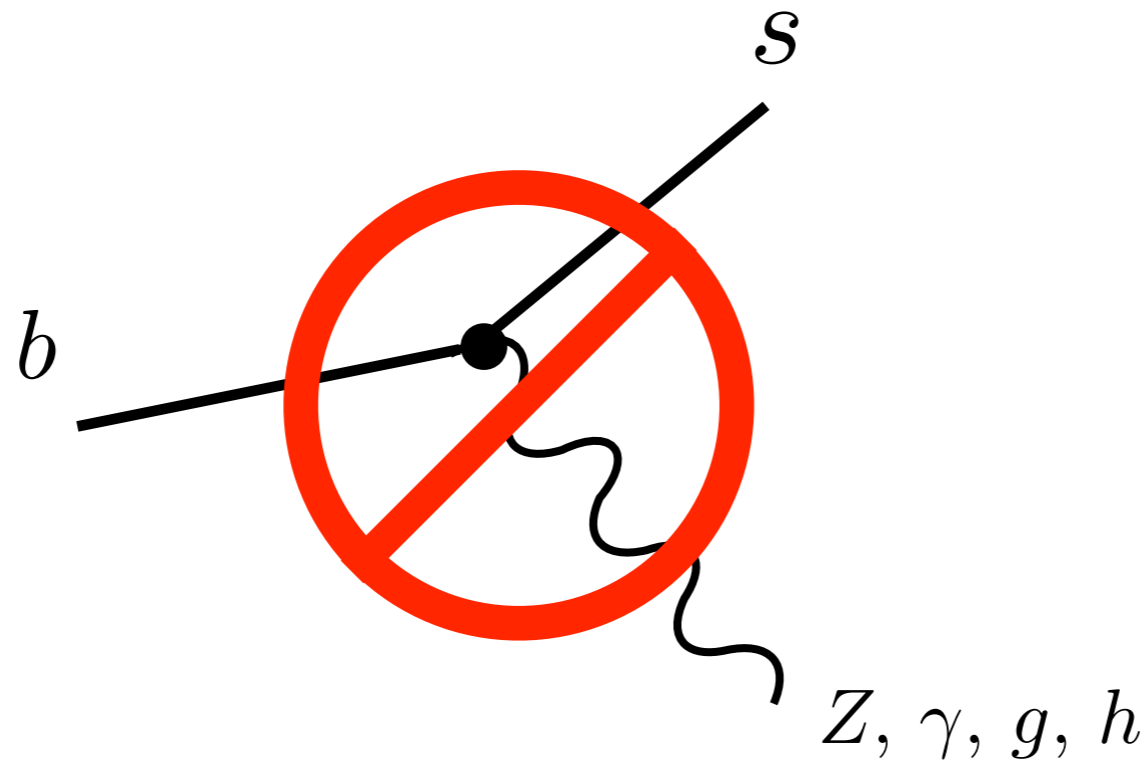
Annual theory meeting, 17.12.2018

Why Flavour is important

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Flavour changing neutral currents probe the SM as a quantum field theory.

Classically, there are no flavour transitions with neutral currents:



Why Flavour is important

$$\mathcal{L}^{\text{SM}} \ni \bar{d}_L Y_d d_R \phi + \bar{u}_L Y_u u_R \tilde{\phi}$$

Symmetry breaking:
 $\phi \rightarrow v + h$

$$d = \begin{pmatrix} d \\ s \\ b \end{pmatrix} \quad u = \begin{pmatrix} u \\ c \\ t \end{pmatrix} \quad Y_{u,d} = \begin{pmatrix} y_{11} & y_{12} & y_{13} \\ y_{21} & y_{22} & y_{23} \\ y_{31} & y_{32} & y_{33} \end{pmatrix}$$

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Rotate to the mass eigenbasis:

$$D_L Y_u D_R^\dagger = \frac{1}{v} \text{diag}(m_d, m_s, m_b) \quad U_L Y_u U_R^\dagger = \frac{1}{v} \text{diag}(m_u, m_c, m_t)$$

gives

$$\mathcal{L}^{\text{SM}} \ni \bar{d}_L \frac{m_d}{v} d_R (v + h) + \bar{u}_L \frac{m_u}{v} u_R (v + h)$$

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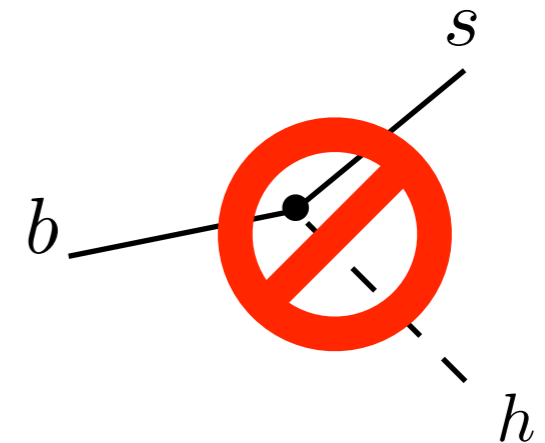
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$$\mathcal{L}^{\text{SM}} \ni \bar{d}_L Y_d d_R \phi + \bar{u}_L Y_u u_R \tilde{\phi}$$

$$+ \bar{d}_L g \gamma_\mu d_L Z^\mu + \bar{u}_L g \gamma_\mu u_L Z^\mu + \bar{u}_L g \gamma_\mu d_L W_+^\mu + \dots$$

$$\begin{pmatrix} g & 0 & 0 \\ 0 & g & 0 \\ 0 & 0 & g \end{pmatrix}$$


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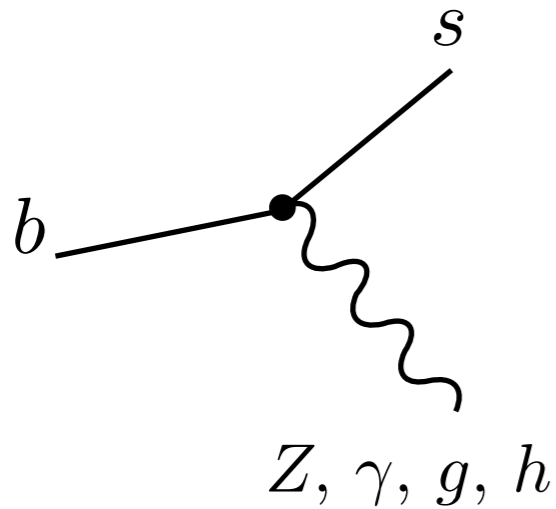
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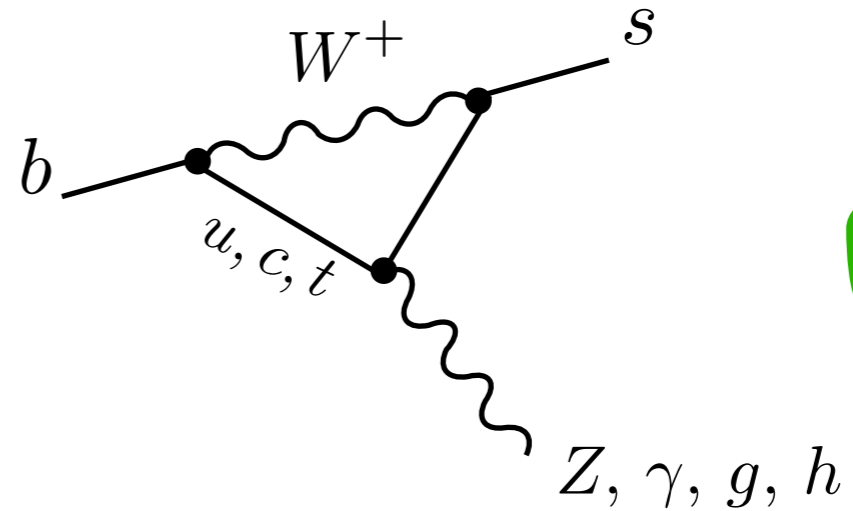
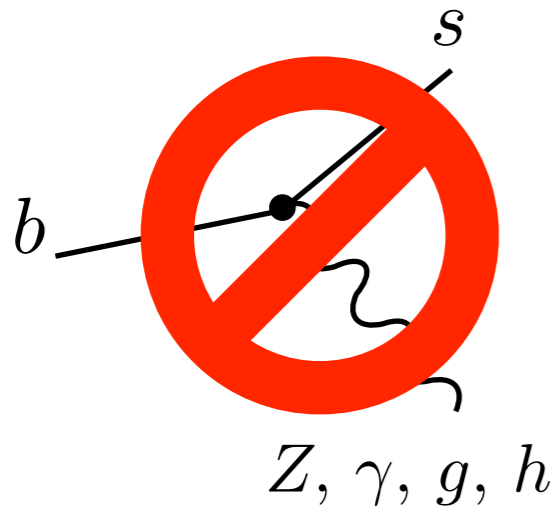
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$$\begin{aligned}
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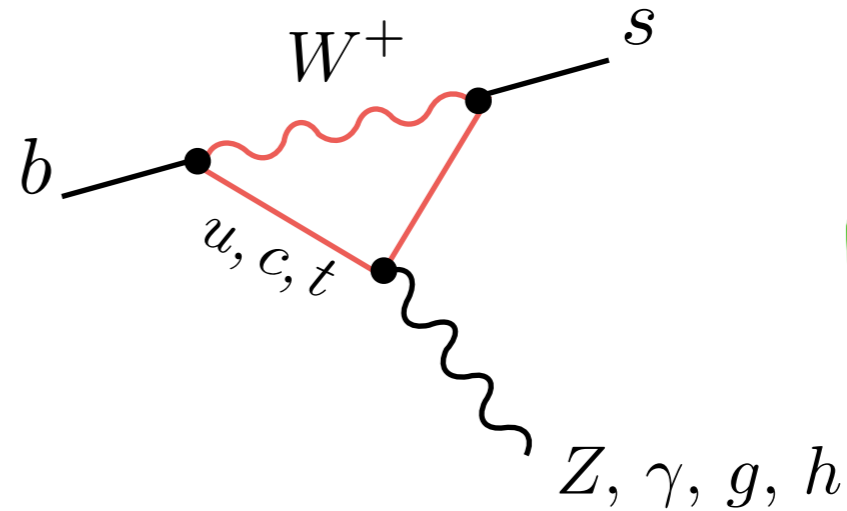
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Why Flavour is important

- Loop suppressed

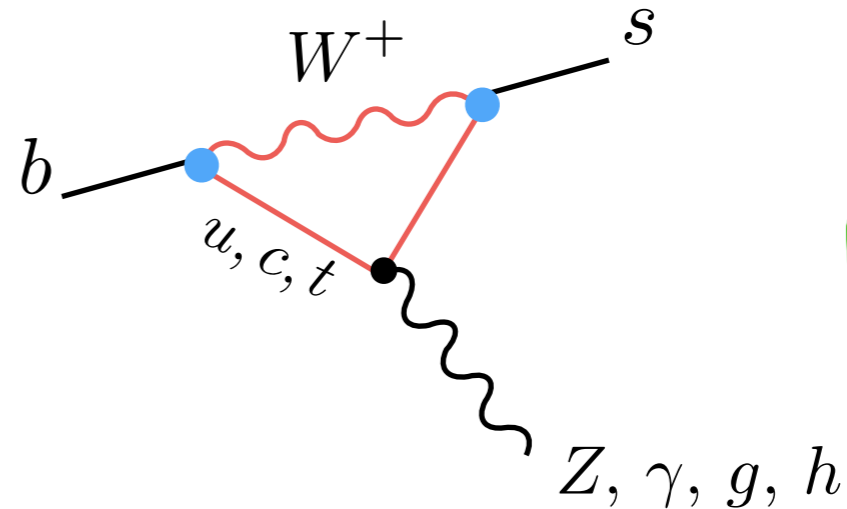


$$\mathcal{A} \propto V_{ub}V_{us}^* f_u + V_{cb}V_{cs}^* f_c + V_{tb}V_{ts}^* f_t$$

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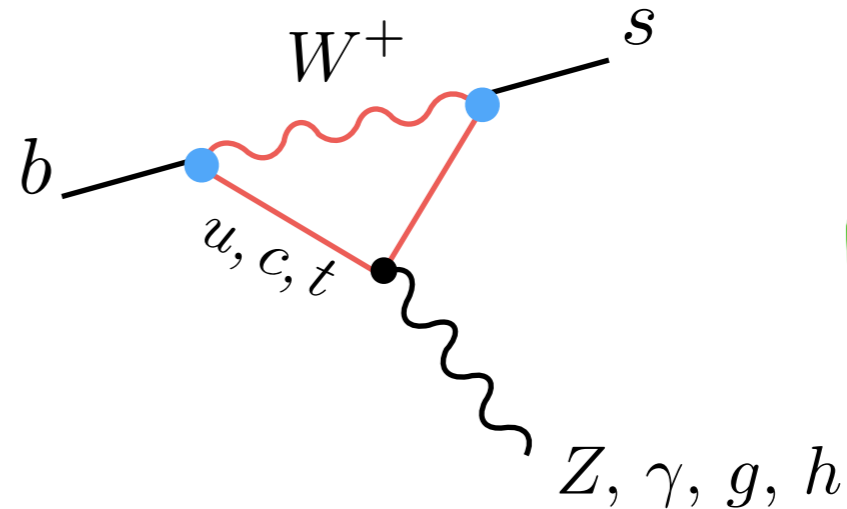
$$\begin{aligned} \mathcal{A} &\propto V_{ub}V_{us}^* f_u + V_{cb}V_{cs}^* f_c + V_{tb}V_{ts}^* f_t \\ &= V_{tb}V_{ts}^*(f_t - c.) \end{aligned}$$

$$\begin{pmatrix} V_{ud}^* & V_{cd}^* & V_{td}^* \\ V_{us}^* & V_{cs}^* & V_{ts}^* \\ V_{ub}^* & V_{cb}^* & V_{tb}^* \end{pmatrix} \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

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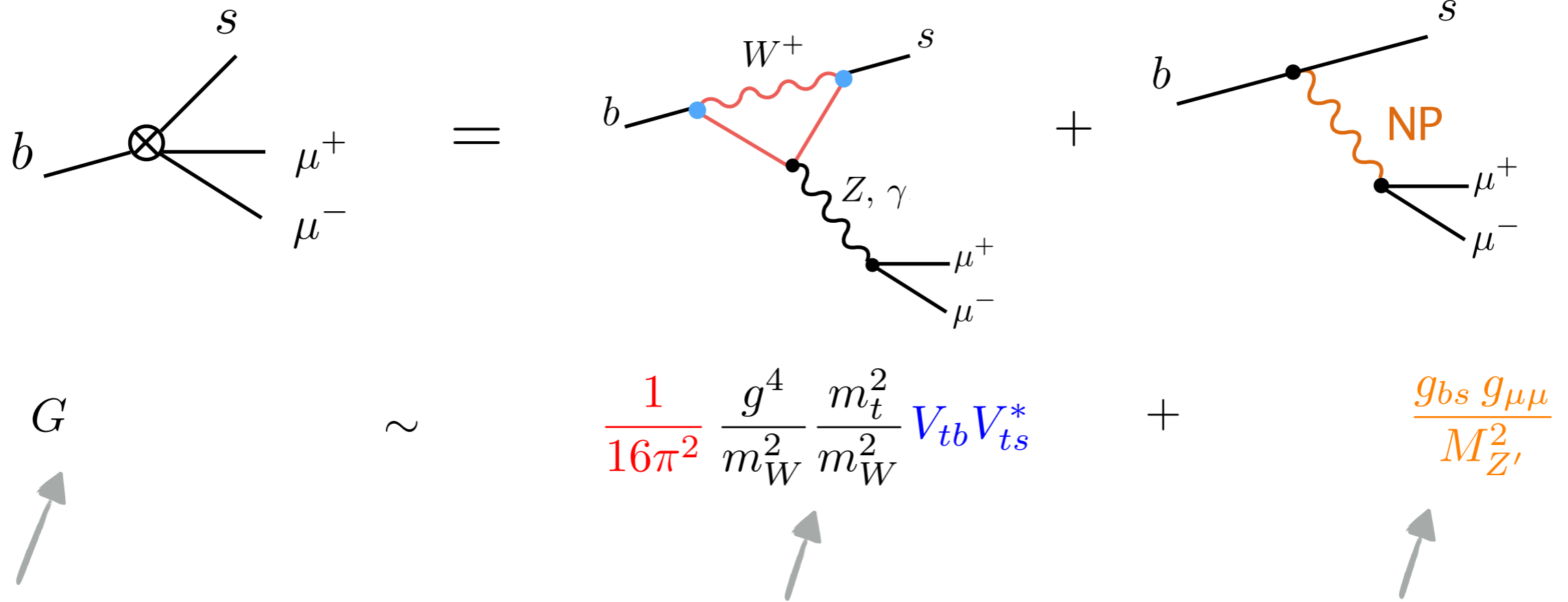
$$\begin{pmatrix} V_{ud}^* & V_{cd}^* & V_{td}^* \\ V_{us}^* & V_{cs}^* & V_{ts}^* \\ V_{ub}^* & V_{cb}^* & V_{tb}^* \end{pmatrix} \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \approx \begin{pmatrix} 1 & \lambda & \lambda^3 \\ \lambda & 1 & \lambda^2 \\ \lambda^3 & \lambda^2 & 1 \end{pmatrix} \quad \text{with} \quad \lambda \approx 0.23$$

[Glashow, Iliopoulos, Maiani, Phys. Rev. D2, 1285 (1970)]

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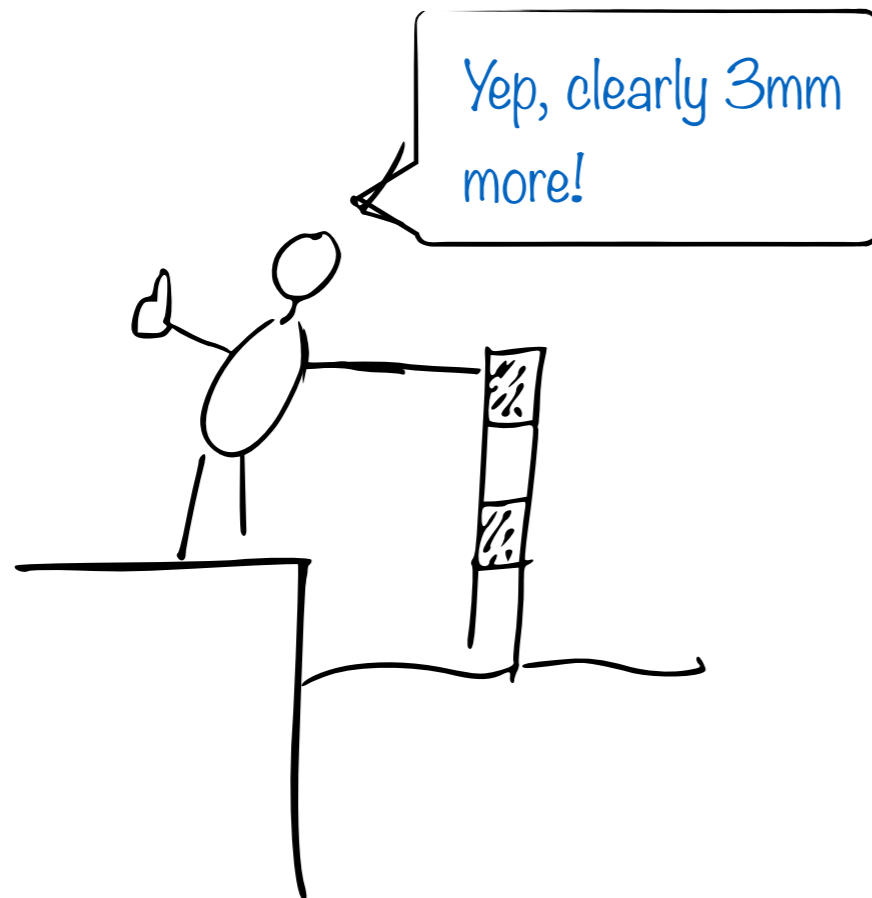
Measure

Compute

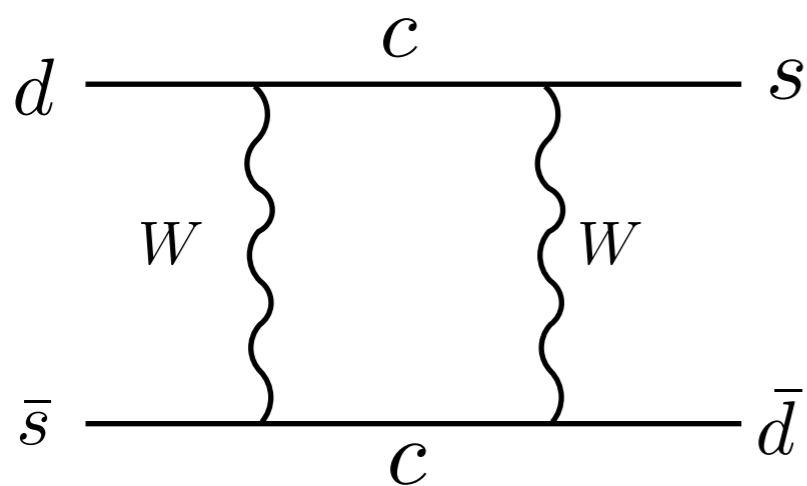
Find

Why Flavour is important

This is why we look for New Physics there. The effects might be small, but still large relative to the SM.



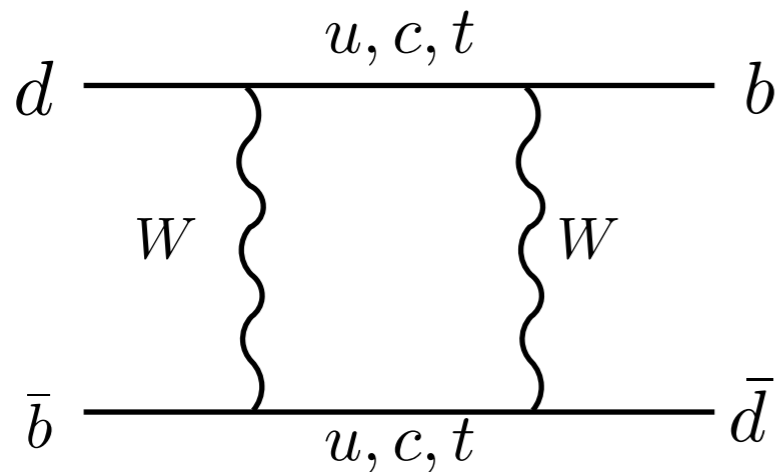
Historical Successes



$$\Rightarrow \Delta m_K \propto \frac{G_F^2}{4\pi^2} \left((M_W^2 + m_u^2) - (M_W^2 + m_c^2) \right) \cos^2 \theta \sin^2 \theta f_K^2 m_K$$

$$\Delta m_K^{\text{exp}} \approx 10^{-12} \text{ MeV} \Rightarrow m_c \approx 1 \text{ GeV}$$

[K. Gaillard and B. W. Lee, 1974]

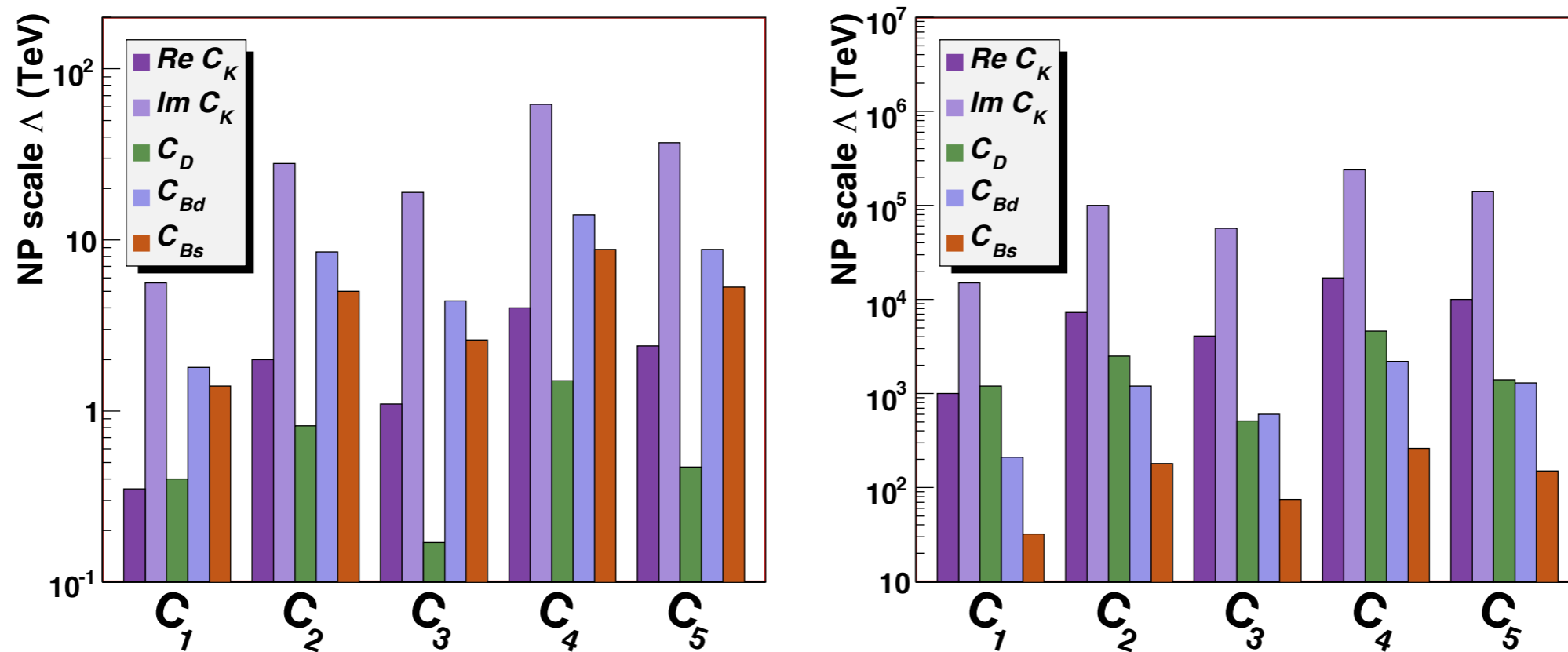


ARGUS 1987 : $m_t > 50 \text{ GeV}$

Flavour observables predicted the charm and the top.

Historical Successes

Flavour also predicted no new physics at the TeV scale...



[UTfit collaboration 2007]

Future Successes ?

Several measurements of rare transitions deviate from the SM prediction ... a sign of new physics?

- An intriguing pattern in $b \rightarrow s\mu^+\mu^-$ transitions 4σ
- Lepton flavour non-universality in R_K, R_{K^*} 2.5σ
- Lepton flavour non-universality in $R(D^{(*)})$ 4σ
- The anomalous magnetic moment of the muon $(g-2)_\mu$ 3.6σ
and of the electron $(g-2)_e$ 2.5σ

A pattern in $b \rightarrow s$ transitions

and

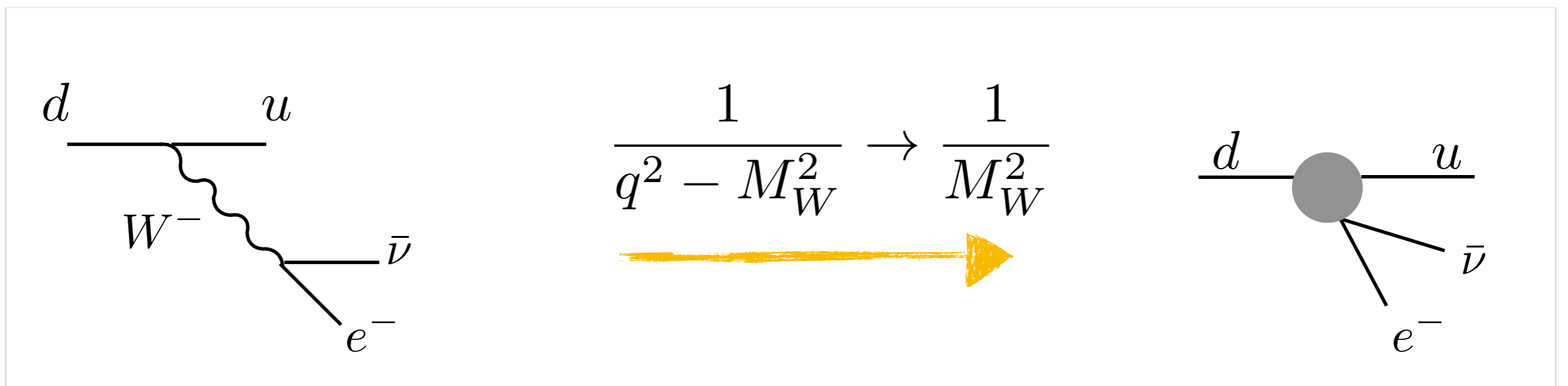
Lepton Non-Universality in $b \rightarrow s$

A pattern in $b \rightarrow s$ transitions

In flavour physics the momentum transfer is small

$$M_{\text{Neutron}} \approx 1 \text{ GeV} \ll M_W \approx 80 \text{ GeV}$$

Example: Beta decay in Fermi theory

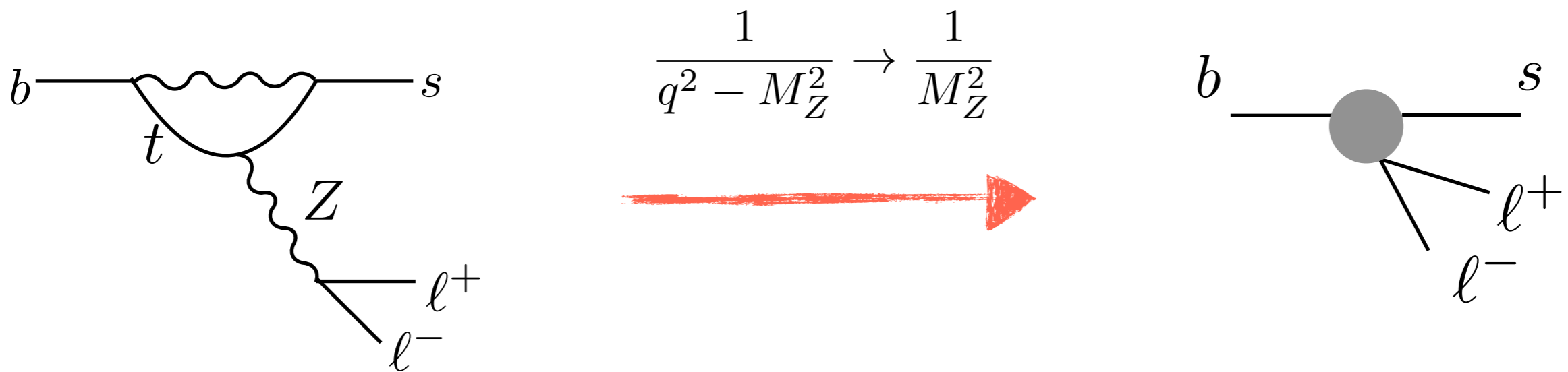


$$\mathcal{L} = -\frac{4G_F}{\sqrt{2}} (\bar{d}_L \gamma_\mu u_L) (\bar{e}_L \gamma^\mu \nu_L)$$

$$G_F \propto \frac{1}{M_W^2}$$

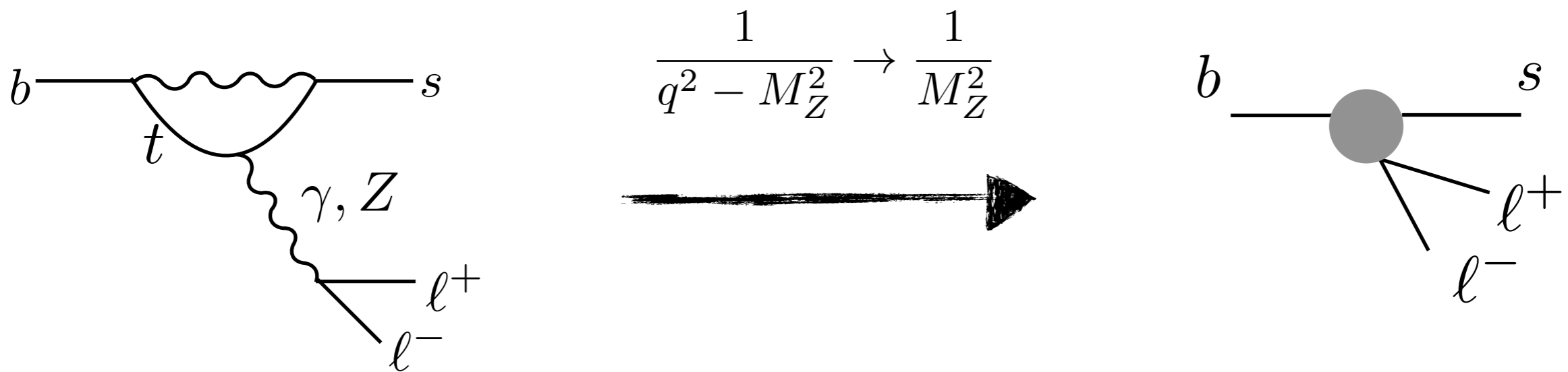
A pattern in $b \rightarrow s$ transitions

Since B decays involve an on-shell B meson (~ 5 GeV), heavy SM particles can be integrated out



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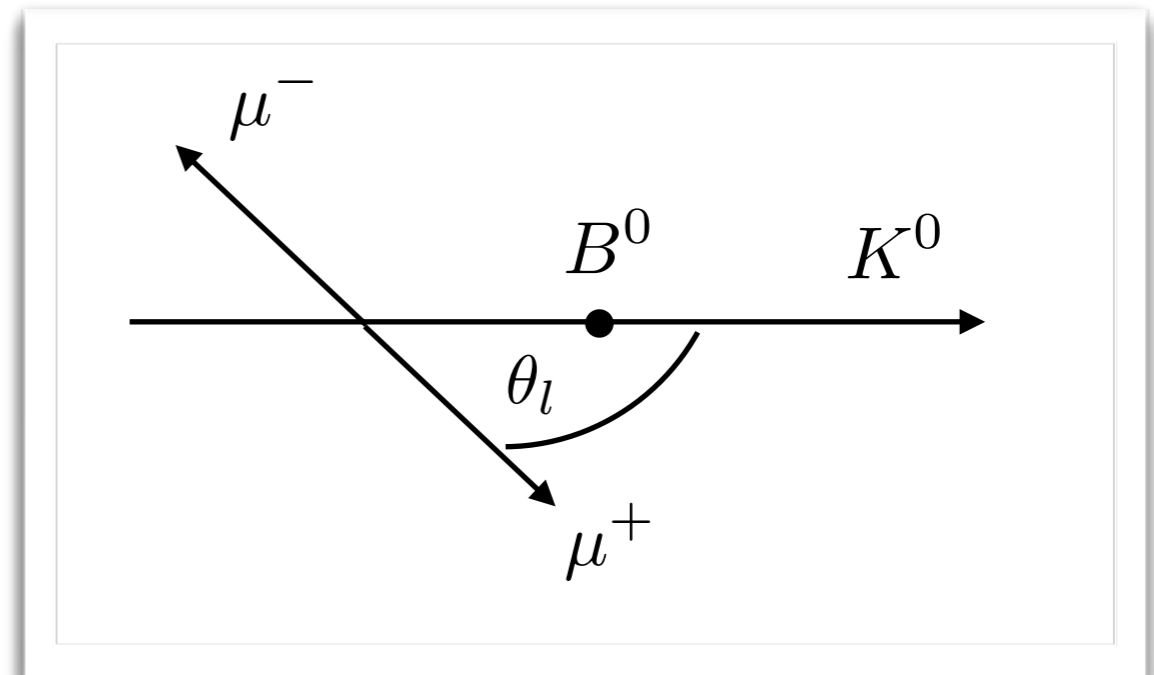
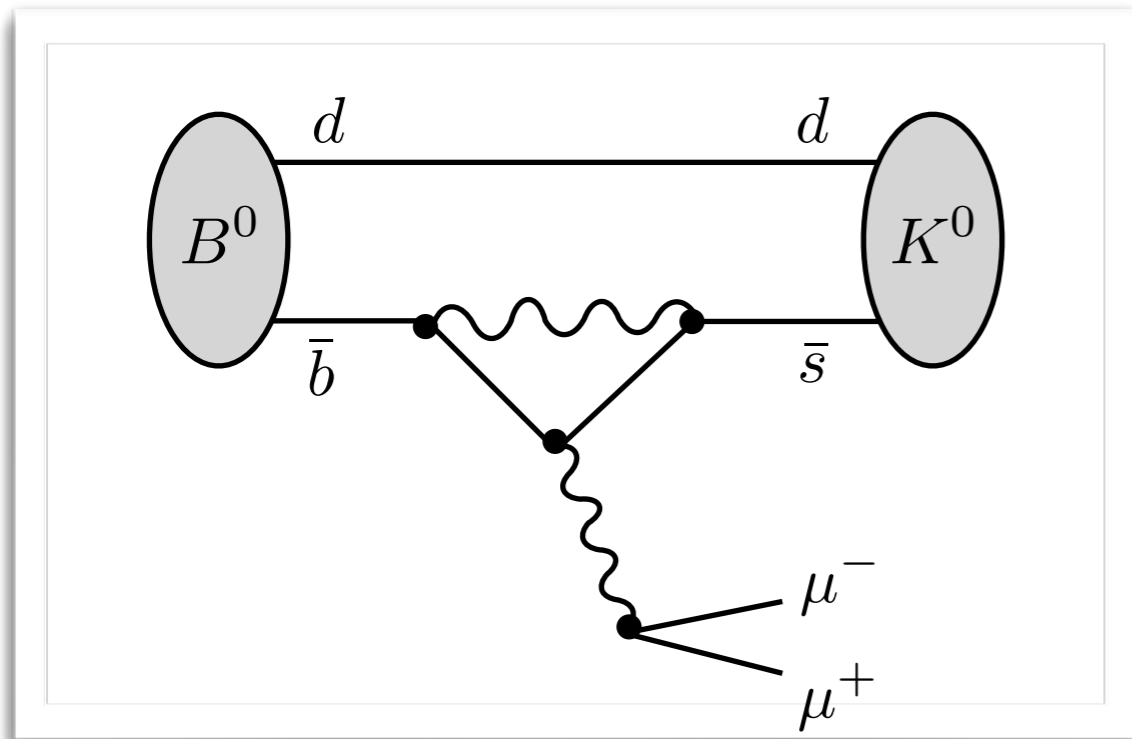
$$\mathcal{H}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \frac{\alpha_e}{4\pi} \sum_i C_i(\mu) \mathcal{O}_i(\mu),$$

$$\mathcal{O}_9 = [\bar{s} \gamma_\mu P_L b] [\bar{\ell} \gamma^\mu \ell], \quad \mathcal{O}_{10} = [\bar{s} \gamma_\mu P_L b] [\bar{\ell} \gamma^\mu \gamma_5 \ell],$$

$$\mathcal{O}_S = [\bar{s} P_R b] [\bar{\ell} \ell], \quad \mathcal{O}_P = [\bar{s} P_R b] [\bar{\ell} \gamma_5 \ell],$$

$$\mathcal{O}_7 = \frac{e}{16\pi^2} m_b (\bar{s} \sigma_{\mu\nu} P_R b) F^{\mu\nu}$$

A pattern in $b \rightarrow s$ transitions



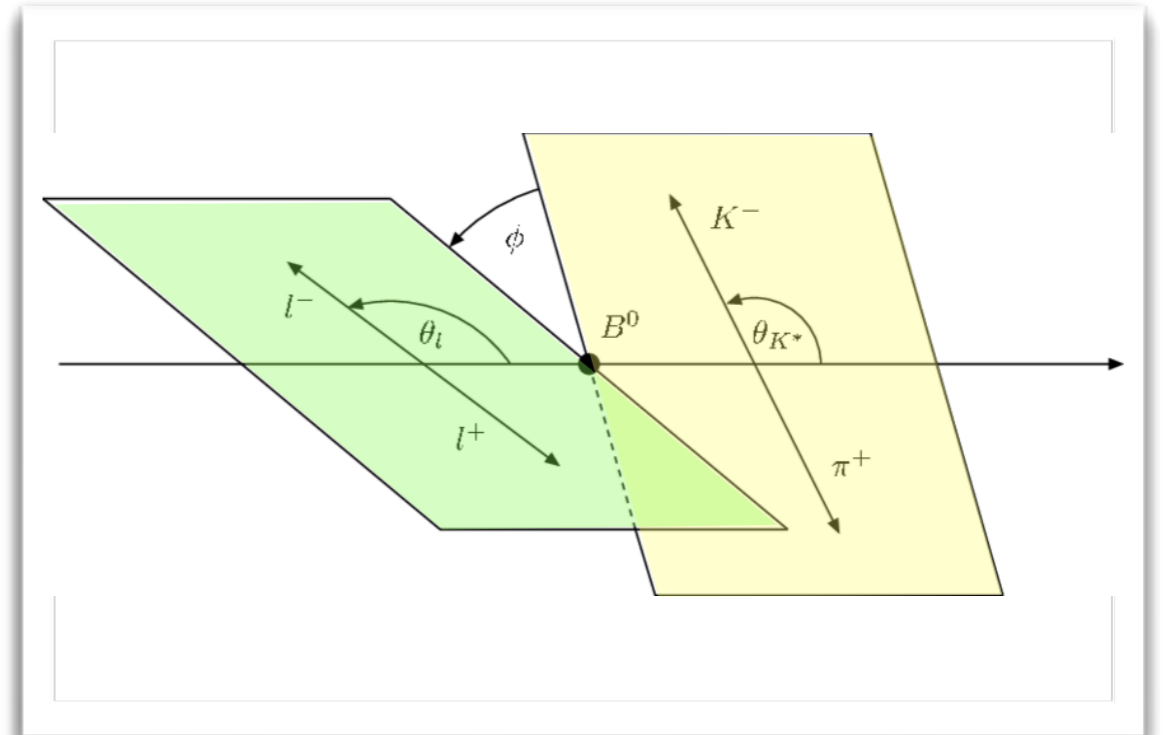
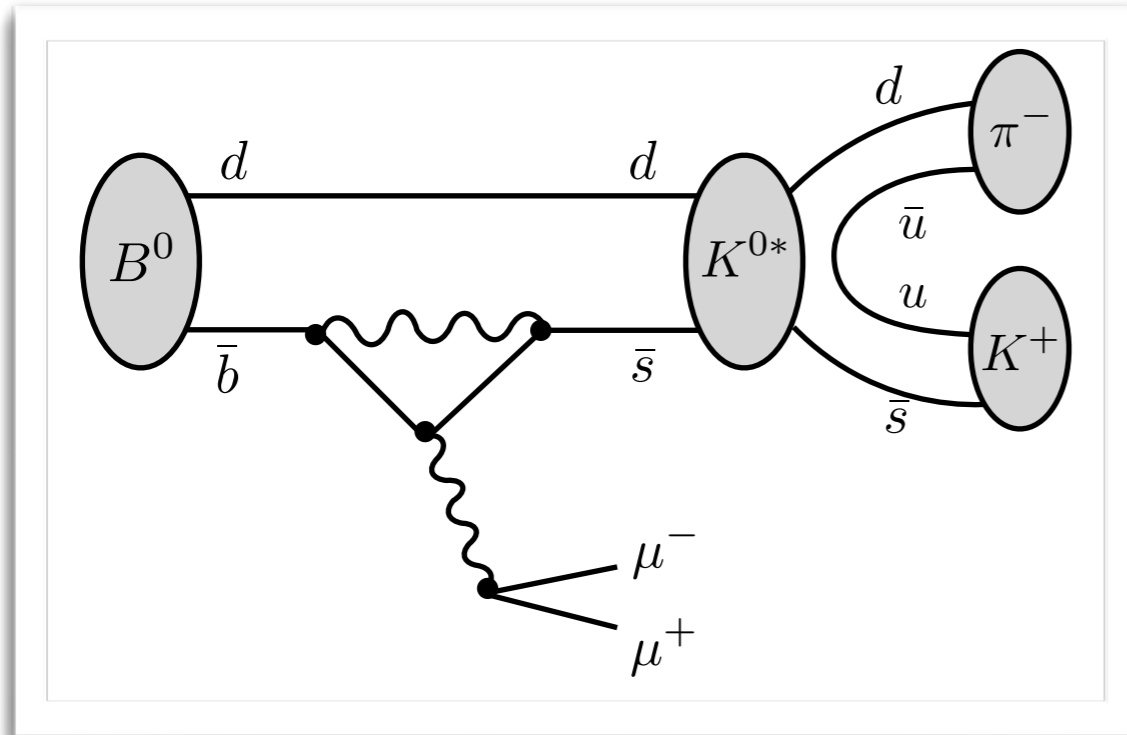
$$\frac{1}{\Gamma} \frac{d^2\Gamma}{dq^2 d\cos\theta} = \lambda^{3/2}(M_B^2, M_K^2, q^2) \frac{1}{4} (1 - \cos^2\theta_l) \left[|F_A|^2 + |F_V|^2 \right]$$

$$F_A = C_{10} f_+(q^2) \qquad F_A = C_9 f_+(q^2) + 2C_7^{\text{eff}} m_b \frac{f_T(q^2)}{M_B + M_K}$$

$$C_9^{\text{SM}} = -C_{10}^{\text{SM}} \approx -4.2$$

$$C_7^{\text{SM}} = -0.31$$

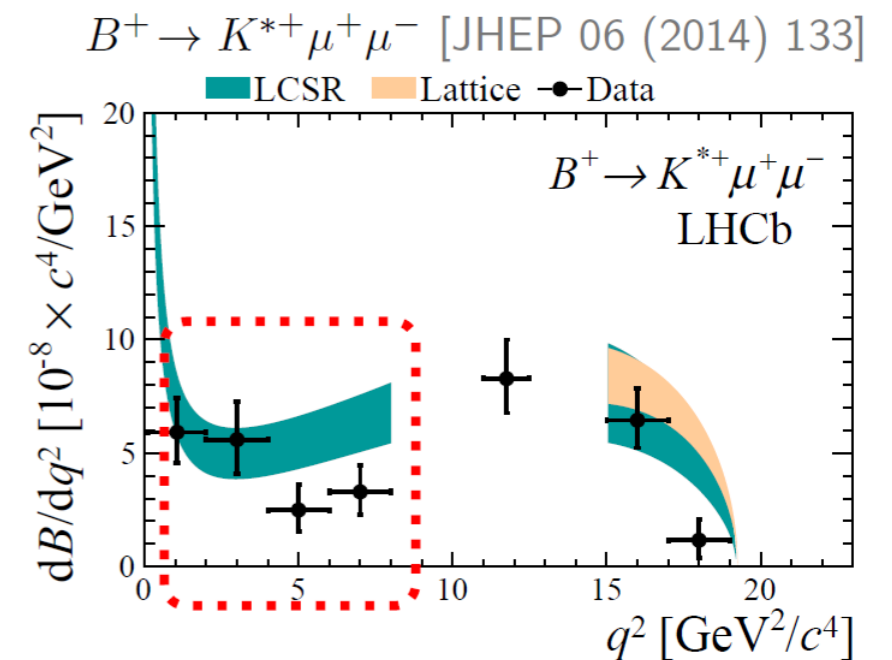
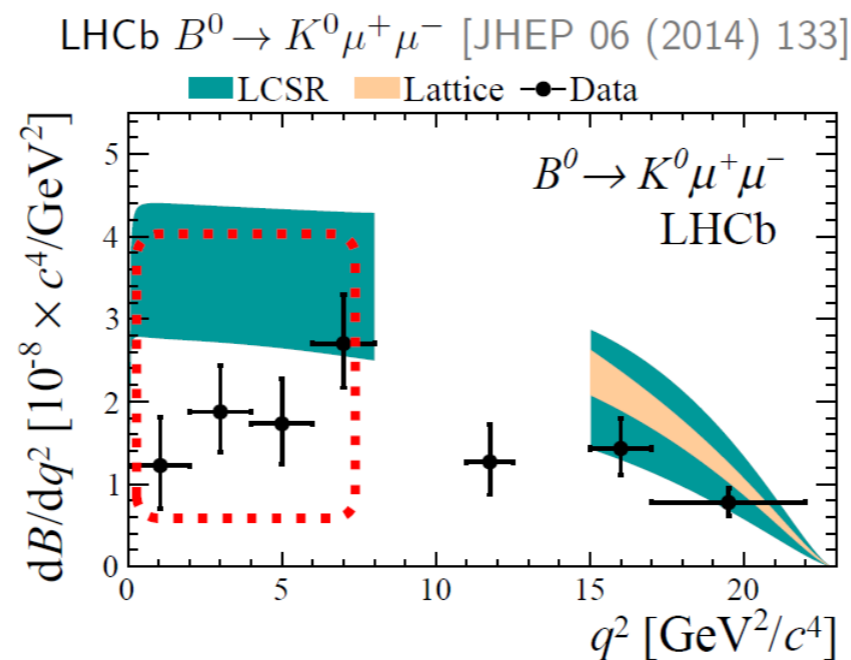
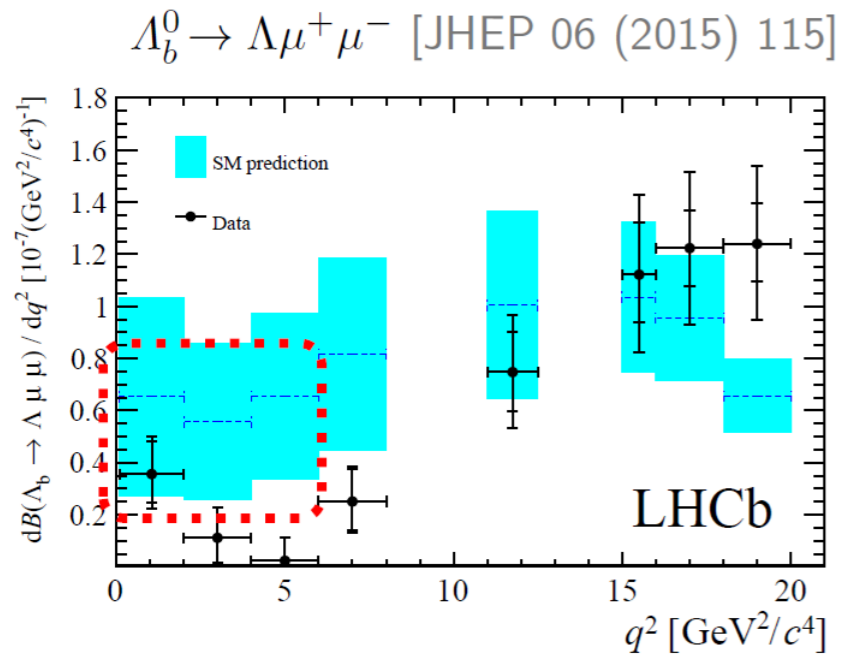
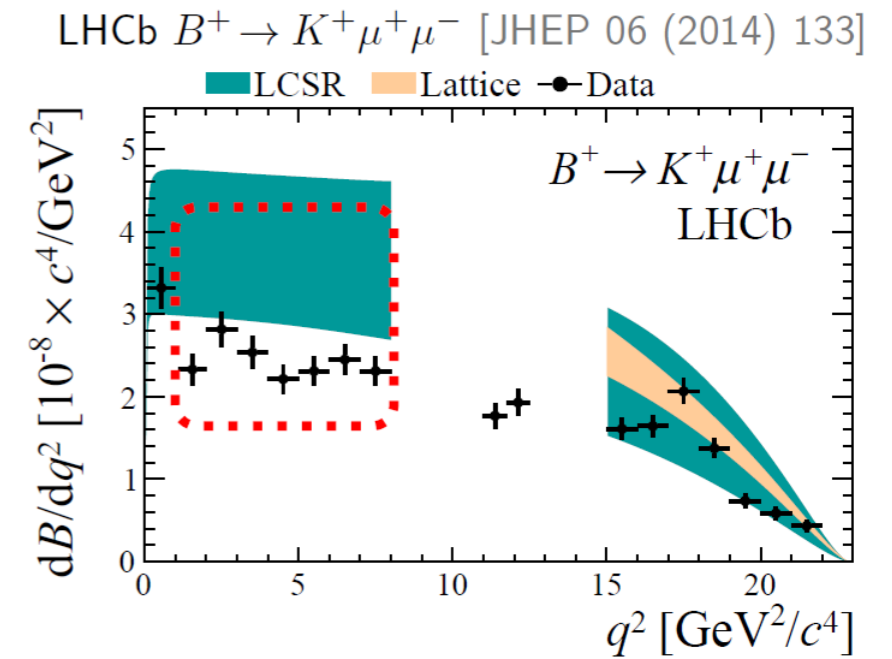
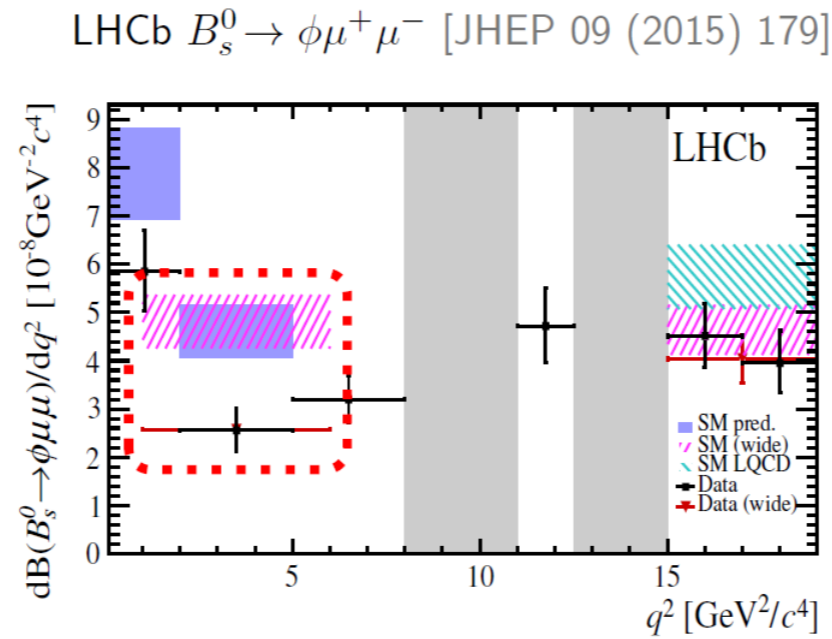
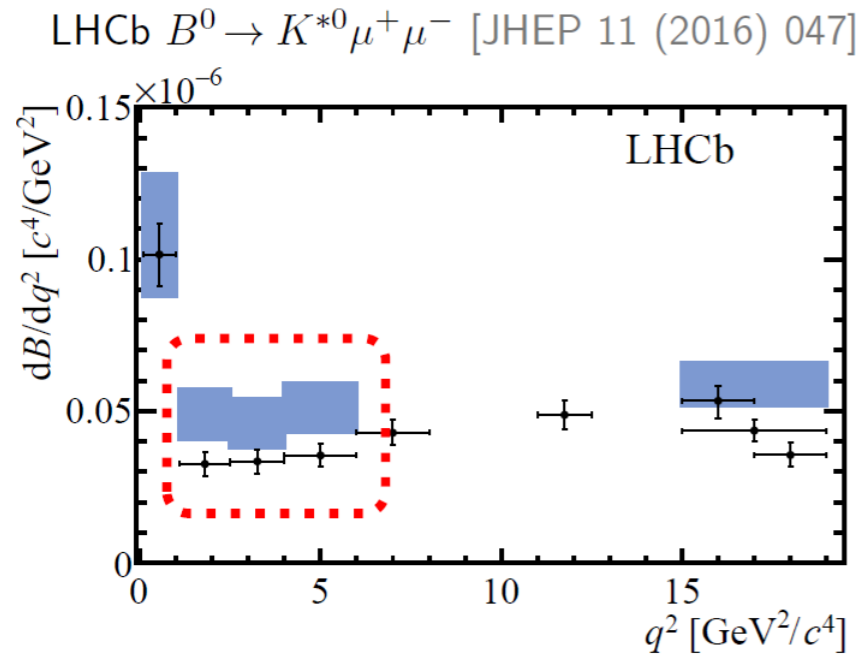
A pattern in $b \rightarrow s$ transitions



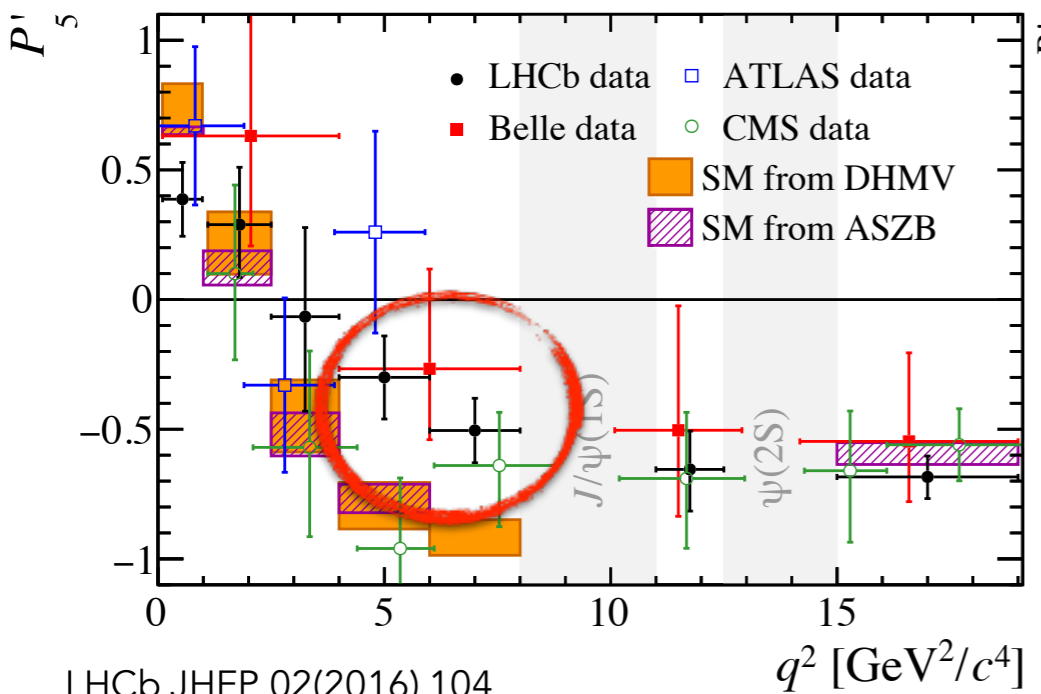
$$\frac{1}{d\Gamma/dq^2} \frac{d^4\Gamma}{d\cos\theta_\ell d\cos\theta_K d\phi dq^2} = \frac{9}{32\pi} \left[\frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K + \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_\ell \right. \\ \left. - F_L \cos^2 \theta_K \cos 2\theta_\ell + S_3 \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\phi \right. \\ \left. + S_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi + S_5 \sin 2\theta_K \sin \theta_\ell \cos \phi \right. \\ \left. + S_6 \sin^2 \theta_K \cos \theta_\ell + S_7 \sin 2\theta_K \sin \theta_\ell \sin \phi \right. \\ \left. + S_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_\ell \sin 2\phi \right]$$

$$P'_{i=4,5,6,8} = \frac{S_{j=4,5,7,8}}{\sqrt{F_L(1 - F_L)}}$$

A pattern in $b \rightarrow s$ transitions



A pattern in $b \rightarrow s$ transitions



LHCb JHEP 02(2016) 104

Belle PRL118, 111801 (2017)

ATLAS, preliminary Moriond EW

CMS, preliminary Moriond EW

Marie-Hélène Schune, Moriond

Deviations in several observables

Decay	obs.	q^2 bin	SM pred.	measurement	pull
$\bar{B}^0 \rightarrow \bar{K}^{*0} \mu^+ \mu^-$	F_L	[2, 4.3]	0.81 ± 0.02	0.26 ± 0.19	ATLAS +2.9
$\bar{B}^0 \rightarrow \bar{K}^{*0} \mu^+ \mu^-$	F_L	[4, 6]	0.74 ± 0.04	0.61 ± 0.06	LHCb +1.9
$\bar{B}^0 \rightarrow \bar{K}^{*0} \mu^+ \mu^-$	S_5	[4, 6]	-0.33 ± 0.03	-0.15 ± 0.08	LHCb -2.2
$\bar{B}^0 \rightarrow \bar{K}^{*0} \mu^+ \mu^-$	P'_5	[1.1, 6]	-0.44 ± 0.08	-0.05 ± 0.11	LHCb -2.9
$\bar{B}^0 \rightarrow \bar{K}^{*0} \mu^+ \mu^-$	P'_5	[4, 6]	-0.77 ± 0.06	-0.30 ± 0.16	LHCb -2.8
$B^- \rightarrow K^{*-} \mu^+ \mu^-$	$10^7 \frac{dBR}{dq^2}$	[4, 6]	0.54 ± 0.08	0.26 ± 0.10	LHCb +2.1
$\bar{B}^0 \rightarrow \bar{K}^0 \mu^+ \mu^-$	$10^8 \frac{dBR}{dq^2}$	[0.1, 2]	2.71 ± 0.50	1.26 ± 0.56	LHCb +1.9
$\bar{B}^0 \rightarrow \bar{K}^0 \mu^+ \mu^-$	$10^8 \frac{dBR}{dq^2}$	[16, 23]	0.93 ± 0.12	0.37 ± 0.22	CDF +2.2
$B_s \rightarrow \phi \mu^+ \mu^-$	$10^7 \frac{dBR}{dq^2}$	[1, 6]	0.48 ± 0.06	0.23 ± 0.05	LHCb +3.1

[Altmannshofer, Straub, 1503.06199]

A pattern in $b \rightarrow s$ transitions

Coefficient	Best fit	1σ	3σ	Pull _{SM}
C_7^{NP}	-0.02	[-0.04, -0.00]	[-0.07, 0.04]	1.1
C_9^{NP}	-1.11	[-1.32, -0.89]	[-1.71, -0.40]	4.5
C_{10}^{NP}	0.58	[0.34, 0.84]	[-0.11, 1.41]	2.5
$C_{7'}^{\text{NP}}$	0.02	[-0.01, 0.04]	[-0.05, 0.09]	0.7
$C_{9'}^{\text{NP}}$	0.49	[0.21, 0.77]	[-0.33, 1.35]	1.8
$C_{10'}^{\text{NP}}$	-0.27	[-0.46, -0.08]	[-0.84, 0.28]	1.4
$C_9^{\text{NP}} = C_{10}^{\text{NP}}$	-0.21	[-0.40, 0.00]	[-0.74, 0.55]	1.0
$C_9^{\text{NP}} = -C_{10}^{\text{NP}}$	-0.69	[-0.88, -0.51]	[-1.27, -0.18]	4.1
$C_9^{\text{NP}} = -C_{9'}^{\text{NP}}$	-1.09	[-1.28, -0.88]	[-1.62, -0.42]	4.8

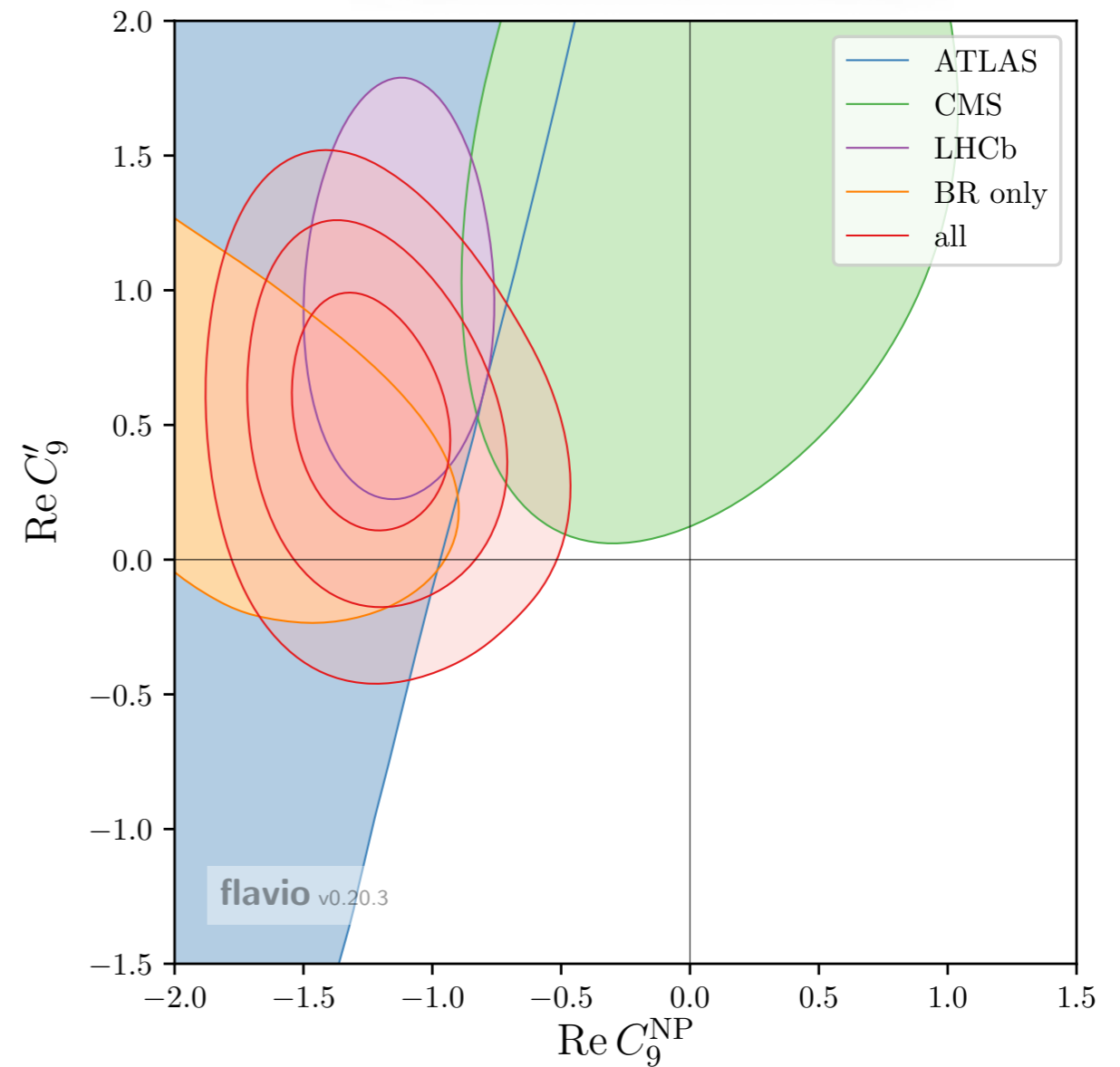
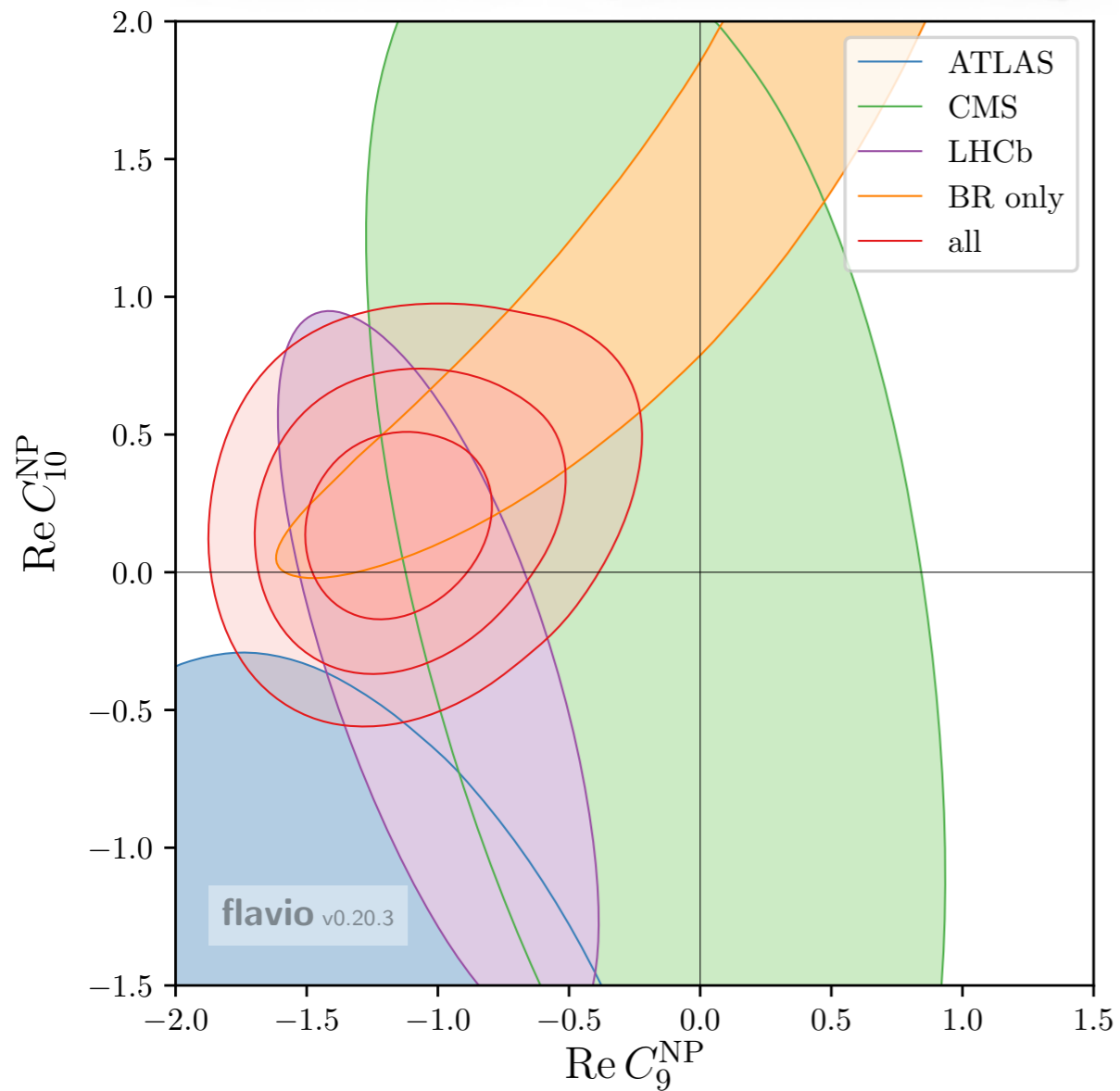
$$\mathcal{O}_9 = [\bar{s}\gamma_\mu P_L b] [\bar{\ell}\gamma^\mu \ell], \quad \mathcal{O}_{10} = [\bar{s}\gamma_\mu P_L b] [\bar{\ell}\gamma^\mu \gamma_5 \ell],$$

A pattern in $b \rightarrow s$ transitions

$$C_9^{\text{NP}}$$

$$C_9^{\text{NP}} = -C_{10}^{\text{NP}}$$

$$C_9^{\text{NP}} = -C_{9'}^{\text{NP}}$$

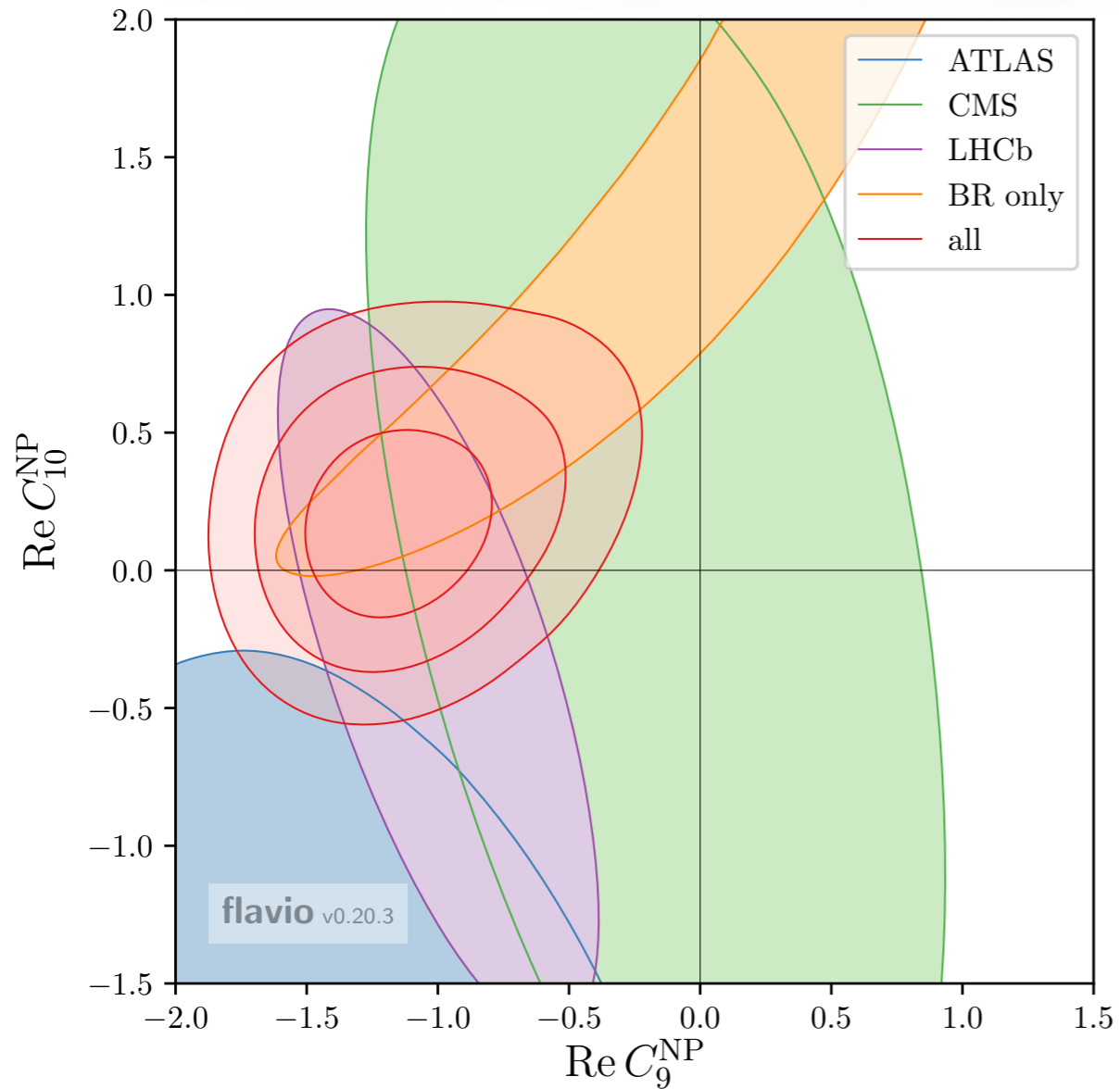


[Altmannshofer, Straub, 1703.09189]

A pattern in $b \rightarrow s$ transitions

$$C_9^{\text{NP}}$$

$$C_9^{\text{NP}} = -C_{10}^{\text{NP}}$$



Is this New Physics?

$$\sim 4 - 5 \sigma$$

$$C_{9/10}^{\text{NP}} \approx C_{10}^{\text{SM}} / 4$$

$$\Rightarrow \frac{1}{M^2} \left(\frac{2V_{tb}V_{ts}^*}{v^2} \frac{\alpha_e}{4\pi} \right)^{-1} = \frac{1}{4}$$

$$\Rightarrow M \approx 35 \text{ TeV}$$

A pattern in b \rightarrow s transitions

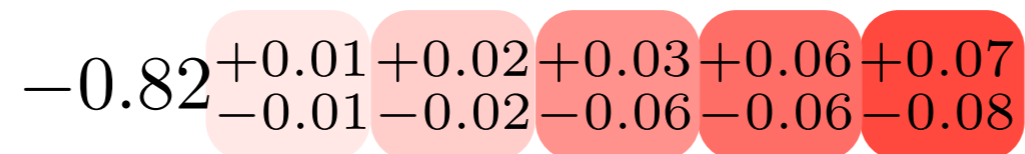
...an enhanced SM contribution would have the right structure to explain this as well...

$$c_9^{NP} = -c_{10}^{NP}$$



A pattern in $b \rightarrow s$ transitions

- Error budget of P'_5 in $[4, 6]$ GeV^2 bin:



parametric



non-factorizable power corrections



form factors



factorizable power corrections



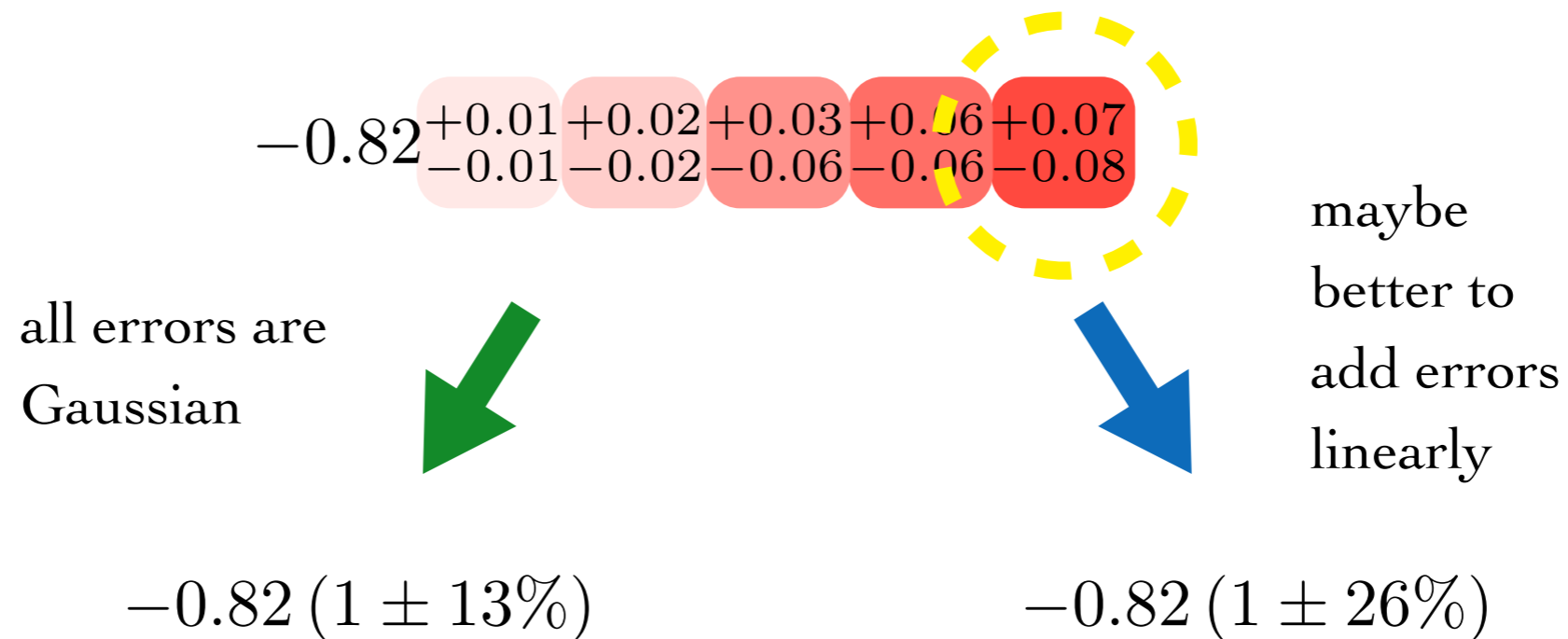
long-distance $c\bar{c}$ effects

[Matias, talk at Moriond EW 2015]

[from Haisch 2016]

A pattern in $b \rightarrow s$ transitions

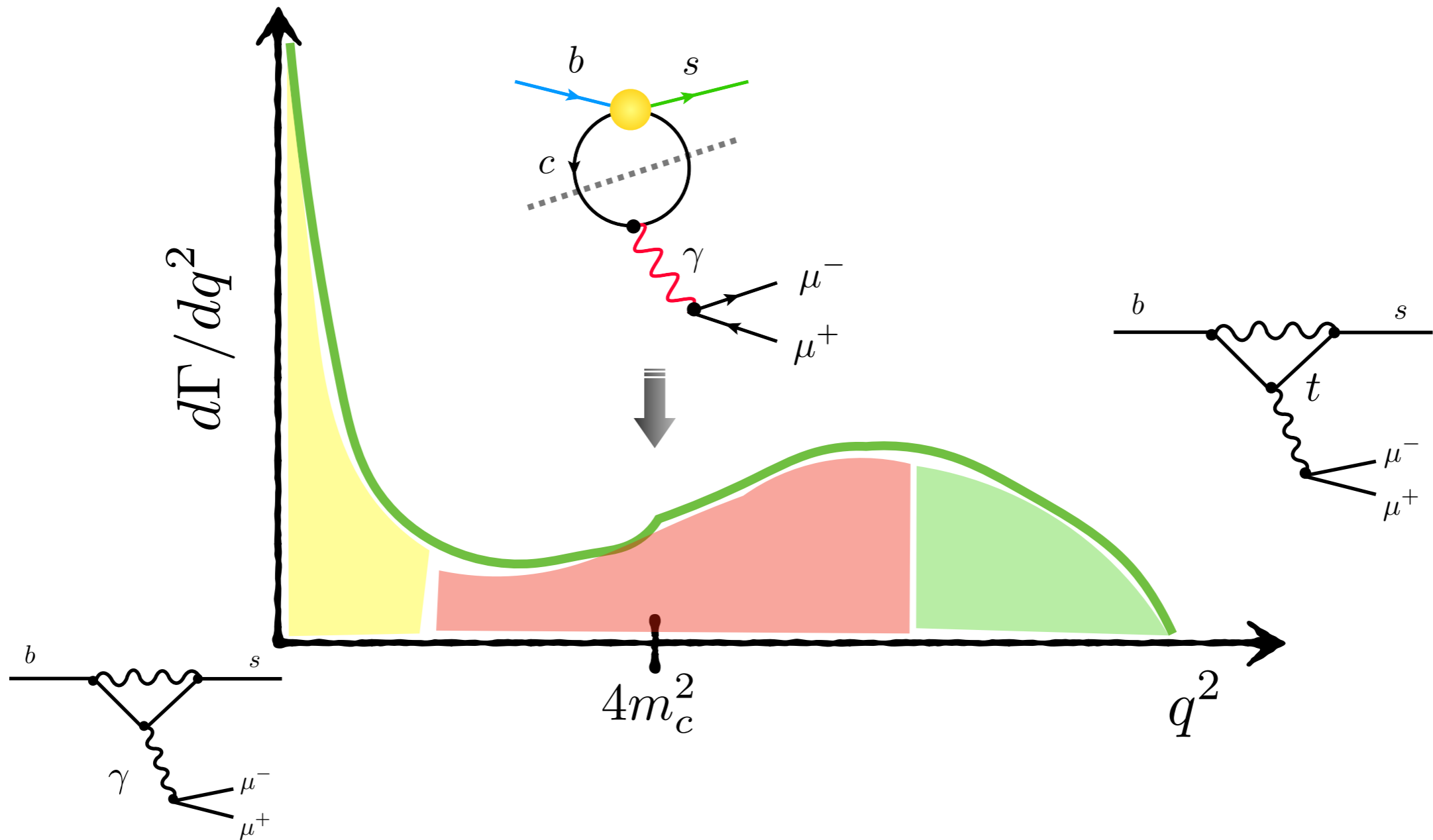
- Dominant uncertainties of theoretical origin. What to do?



- Largest individual uncertainty due to long-distance $c\bar{c}$ effects. What is the problem & what does this mean for the error?

A pattern in $b \rightarrow s$ transitions

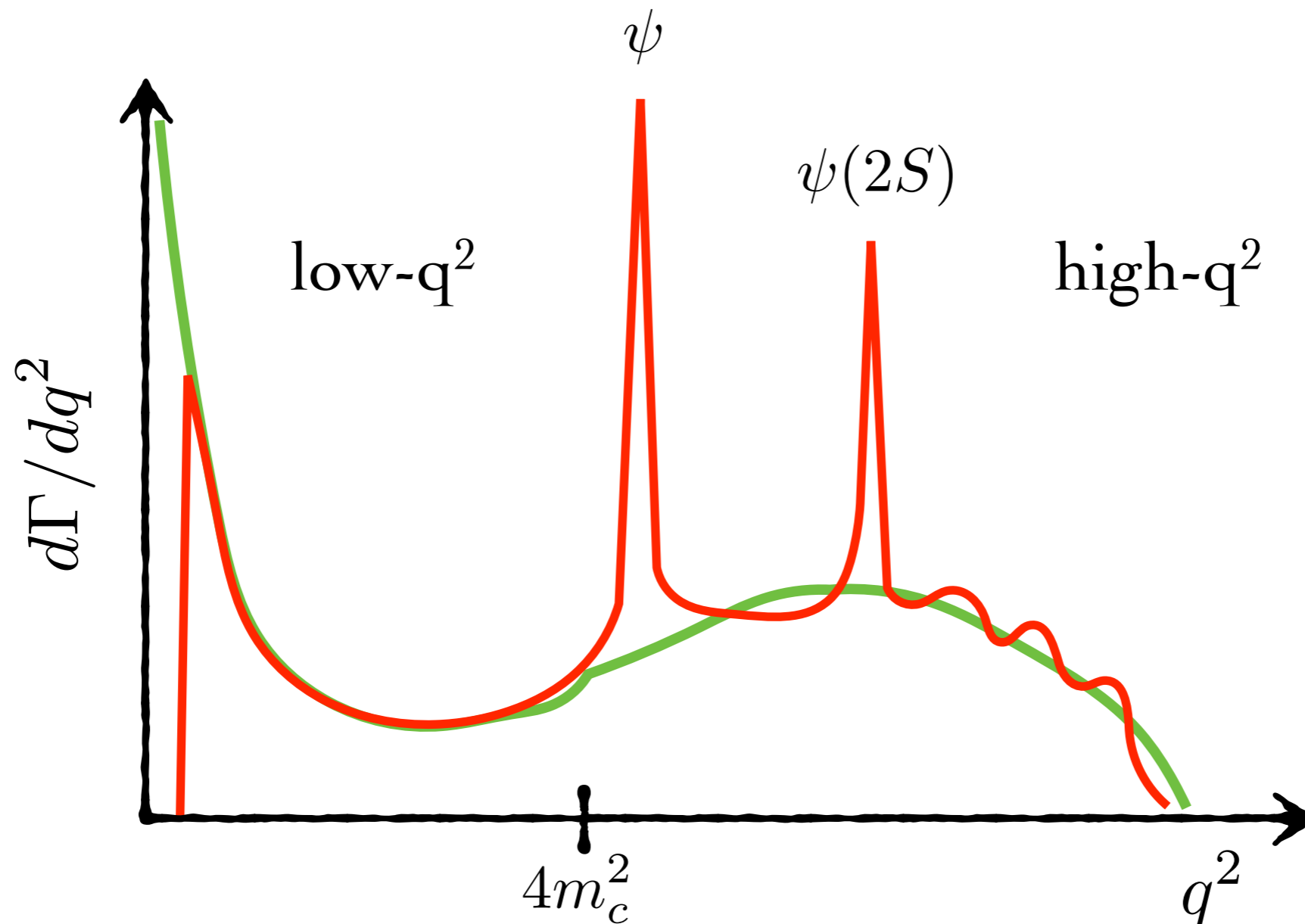
In an ideal world ...



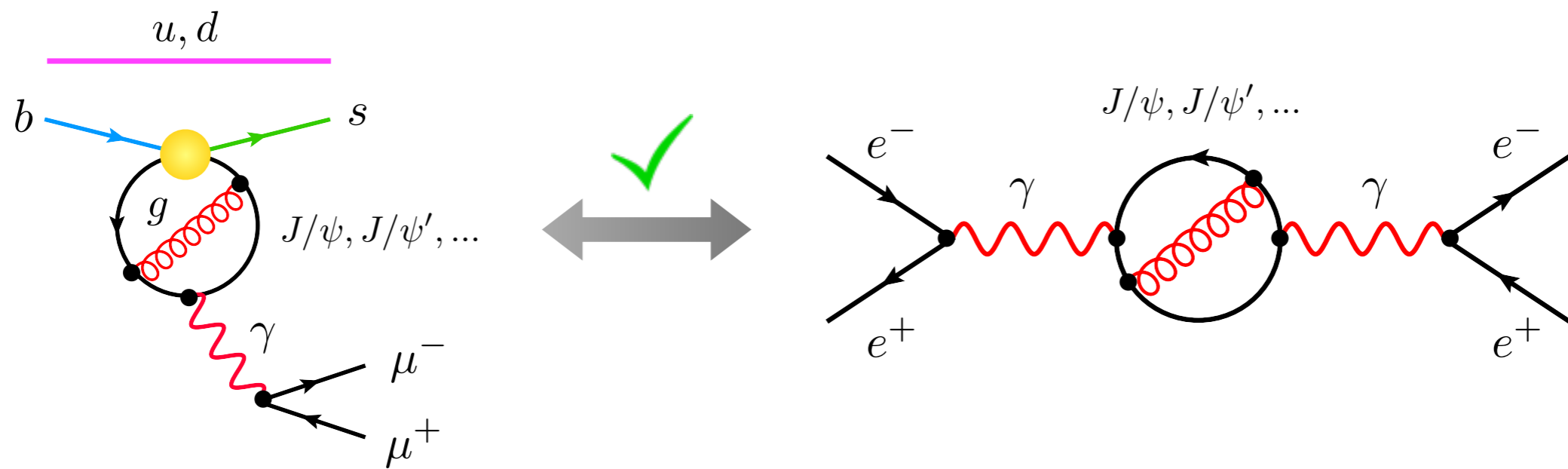
[from Haisch 2016]

A pattern in $b \rightarrow s$ transitions

... in reality

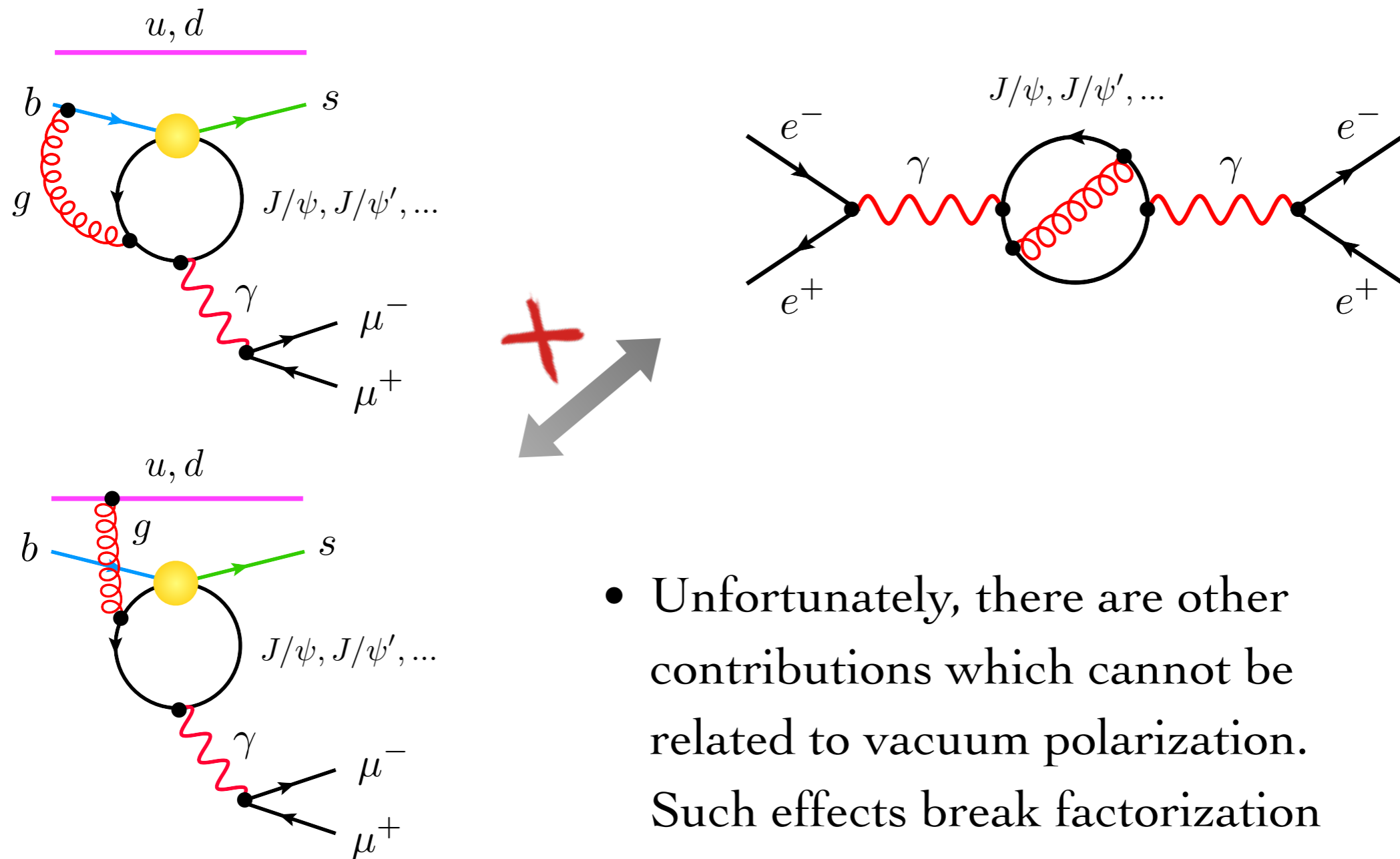


A pattern in $b \rightarrow s$ transitions



A pattern in $b \rightarrow s$ transitions

Breakdown of factorization

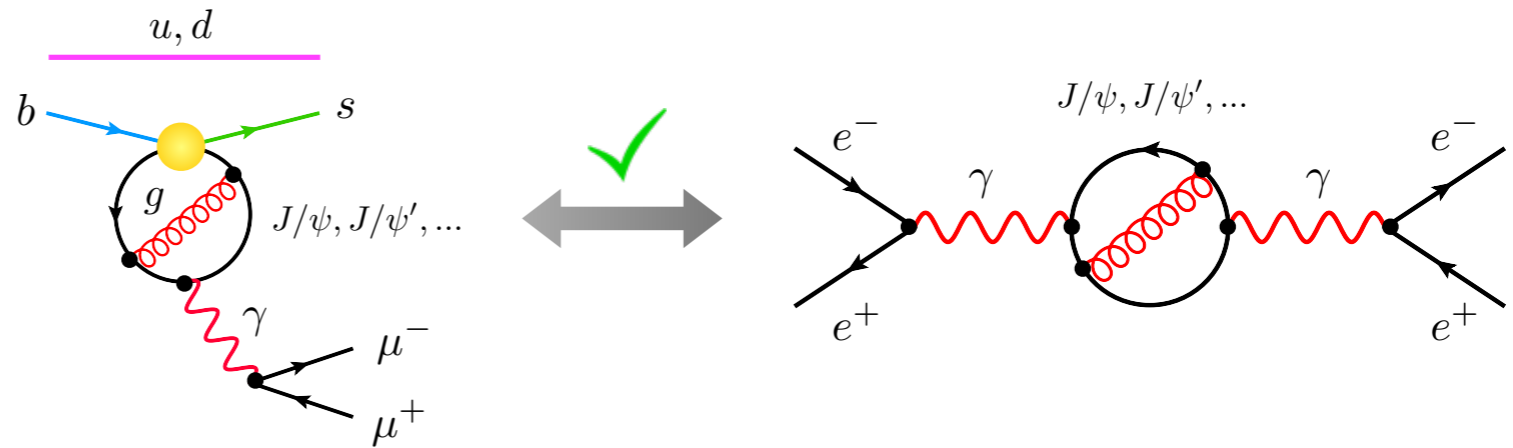


- Unfortunately, there are other contributions which cannot be related to vacuum polarization. Such effects break factorization

A pattern in $b \rightarrow s$ transitions

How bad is it?

[Lyon, Zwicky 1406.0566]

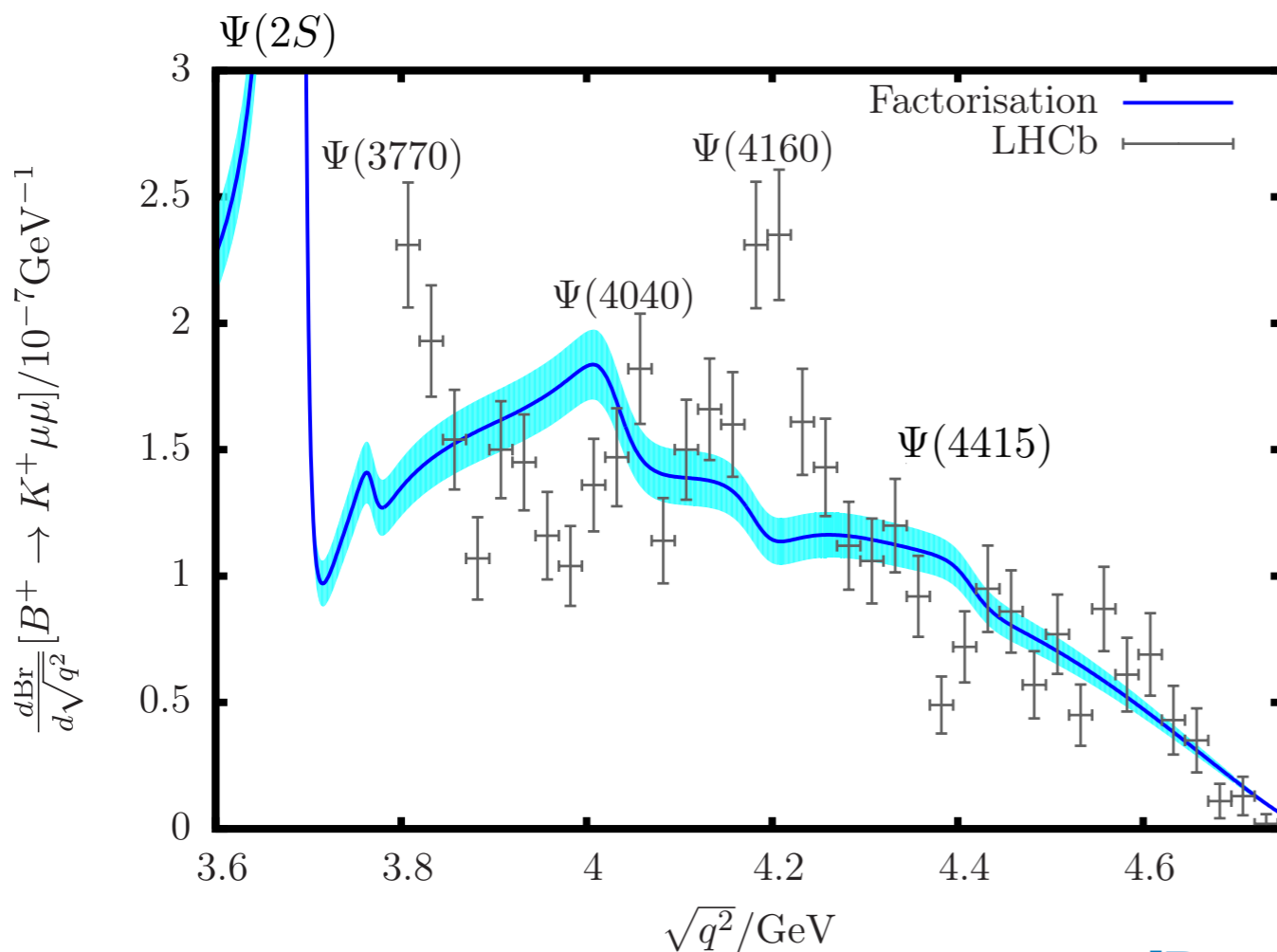


Quark-hadron
duality is broken
globally!

$$\frac{d\Gamma(B \rightarrow \pi\pi)}{dq^2} \propto (\text{Im } \Pi(q^2))^2$$

$$\frac{d\Gamma(B \rightarrow X_s \ell^+ \ell^-)}{dq^2} \propto |\Pi(q^2)|^2$$

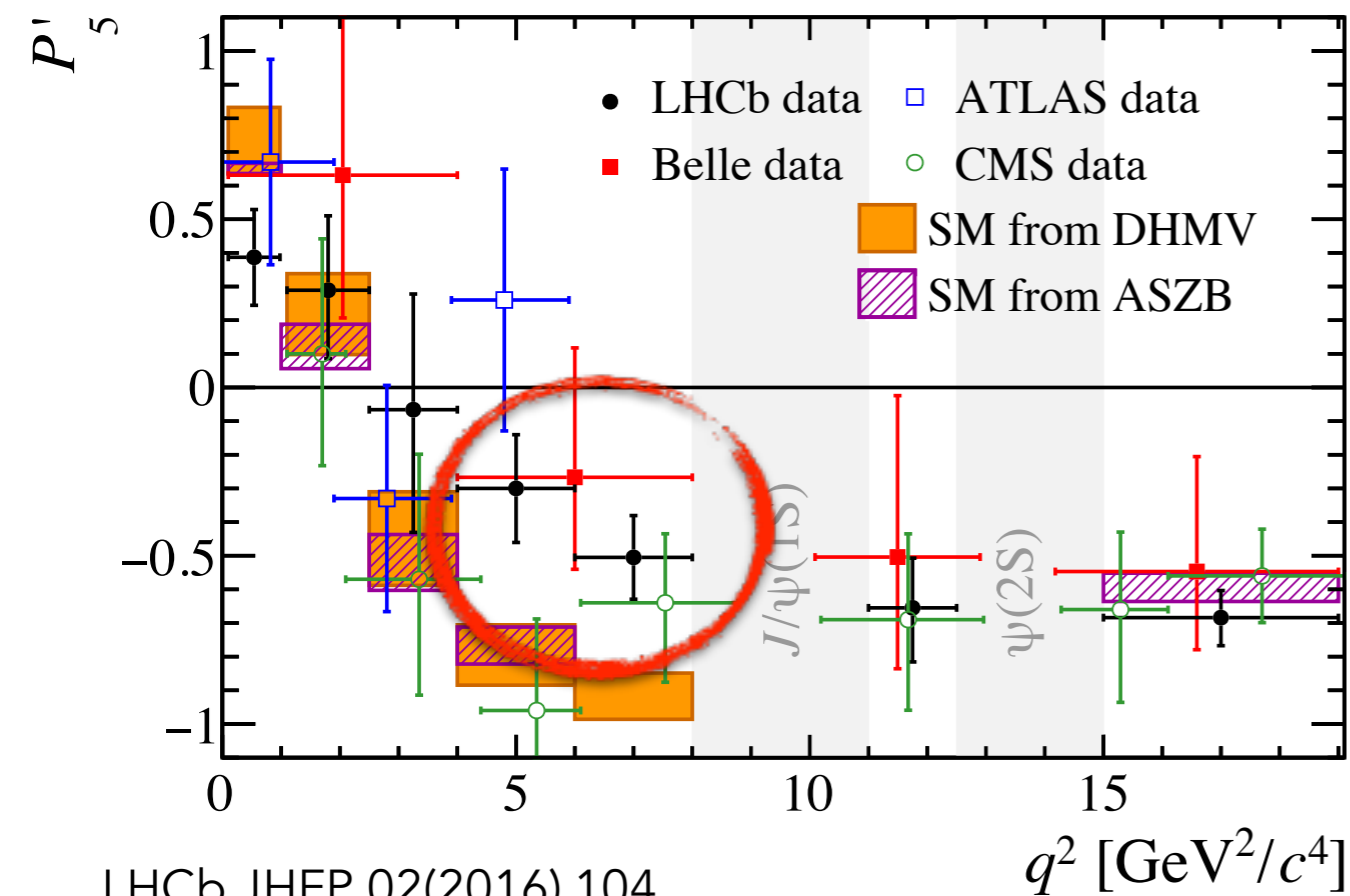
Beautiful toy model in



[Beneke, Buchalla, Neubert, Sachrajda, 0902.4446]

A pattern in $b \rightarrow s$ transitions

Largest deviations are expected close to the J/Psi resonance, which is exactly where the anomaly sits.

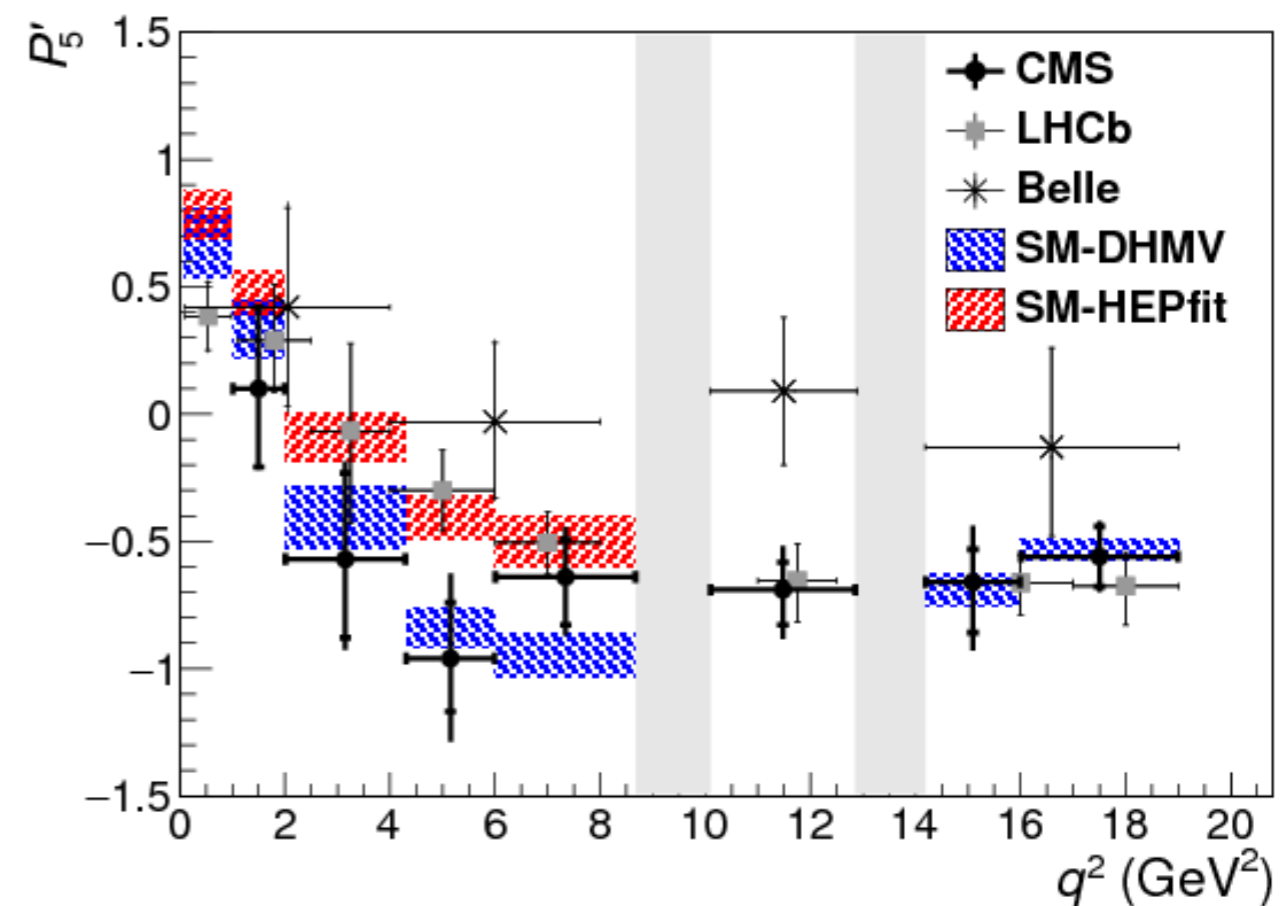


LHCb JHEP 02(2016) 104

Belle PRL118, 111801 (2017)

ATLAS, preliminary Moriond EW

CMS, preliminary Moriond EW



[Albrecht, Reicher, van Dyk, 1806.05010]

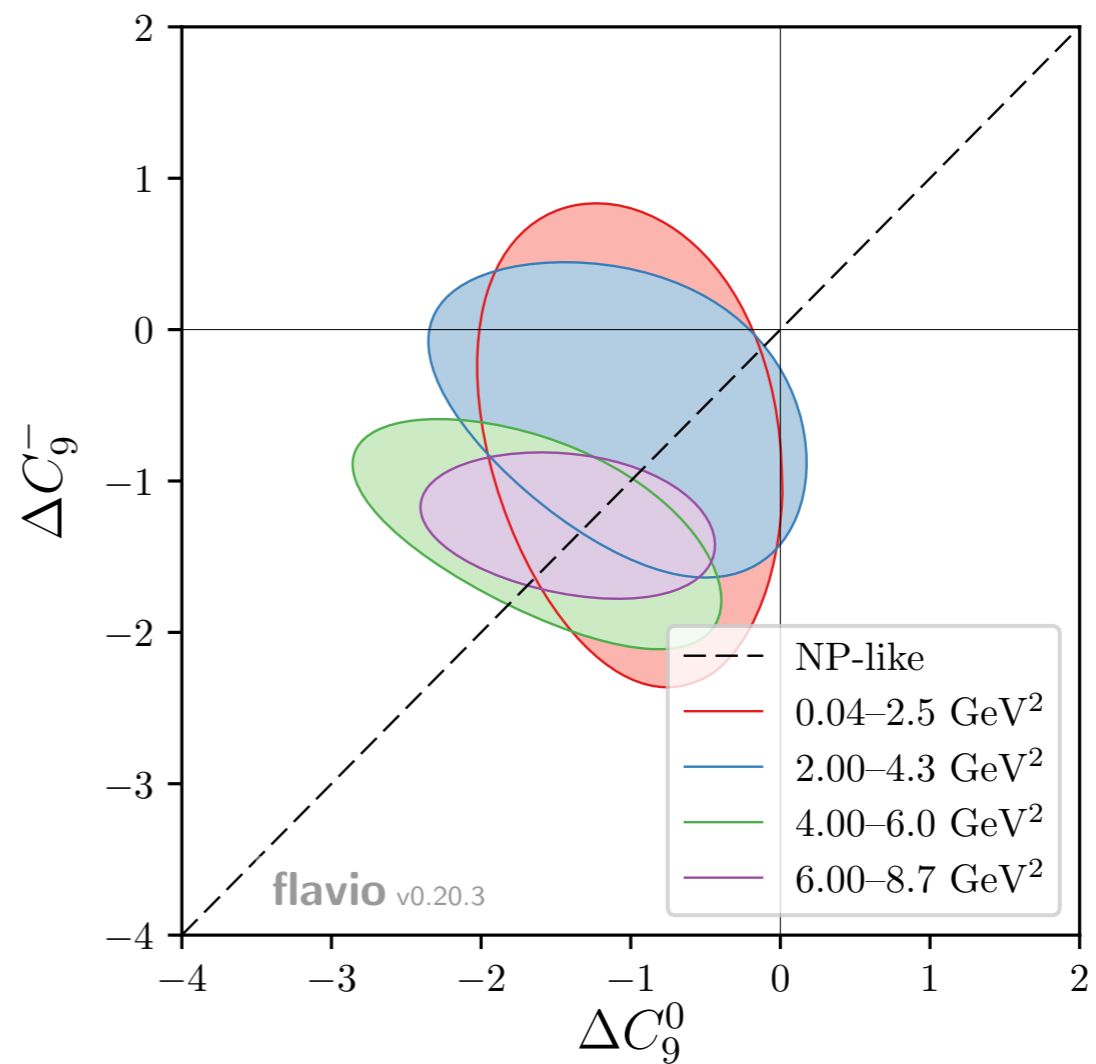
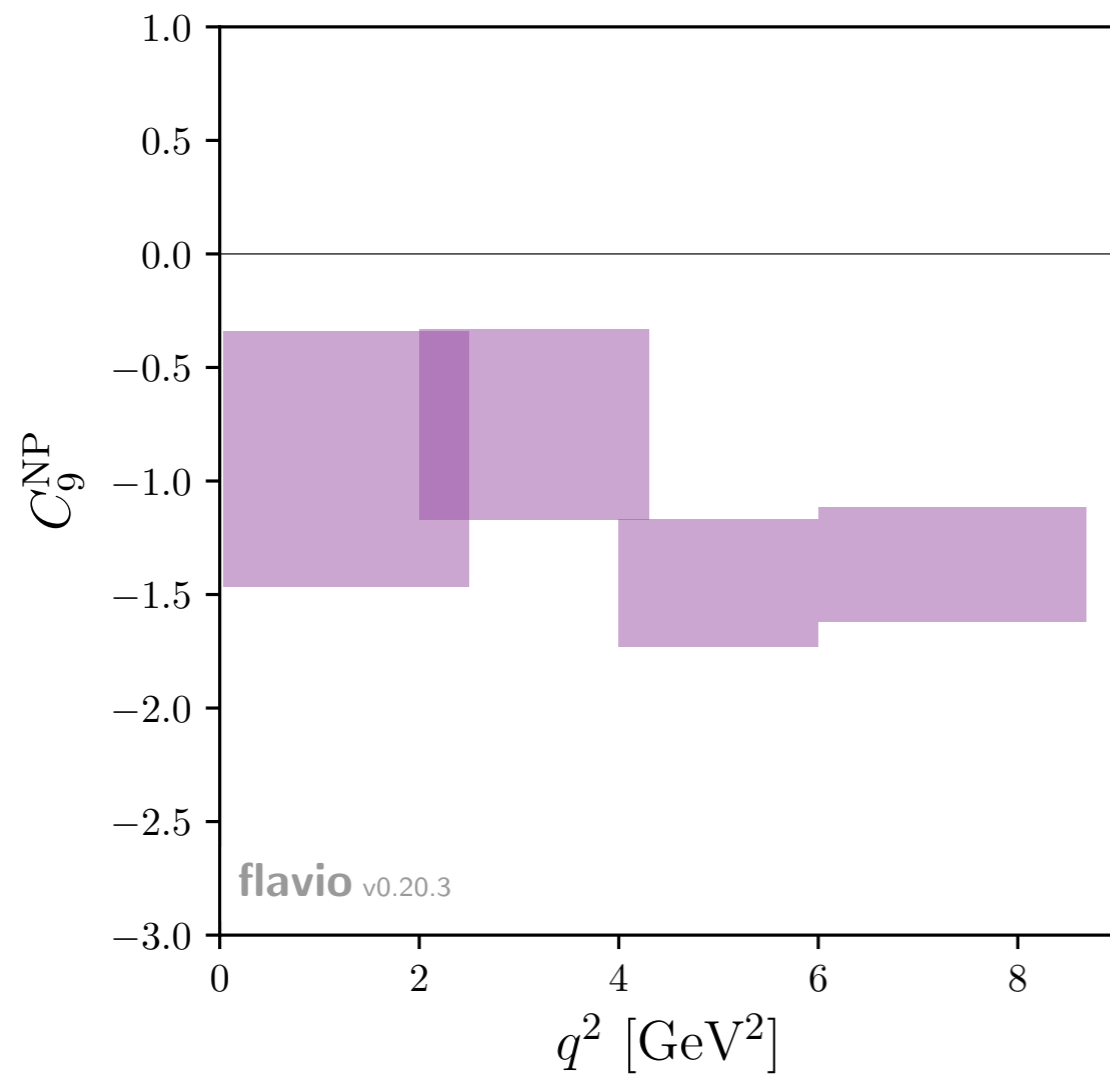
[Ciuchini et.al. 1809.03789]

A pattern in $b \rightarrow s$ transitions

How can we know whether it is new physics?

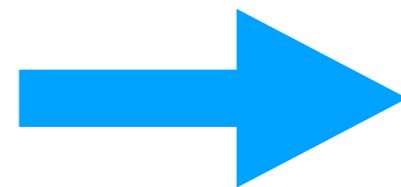
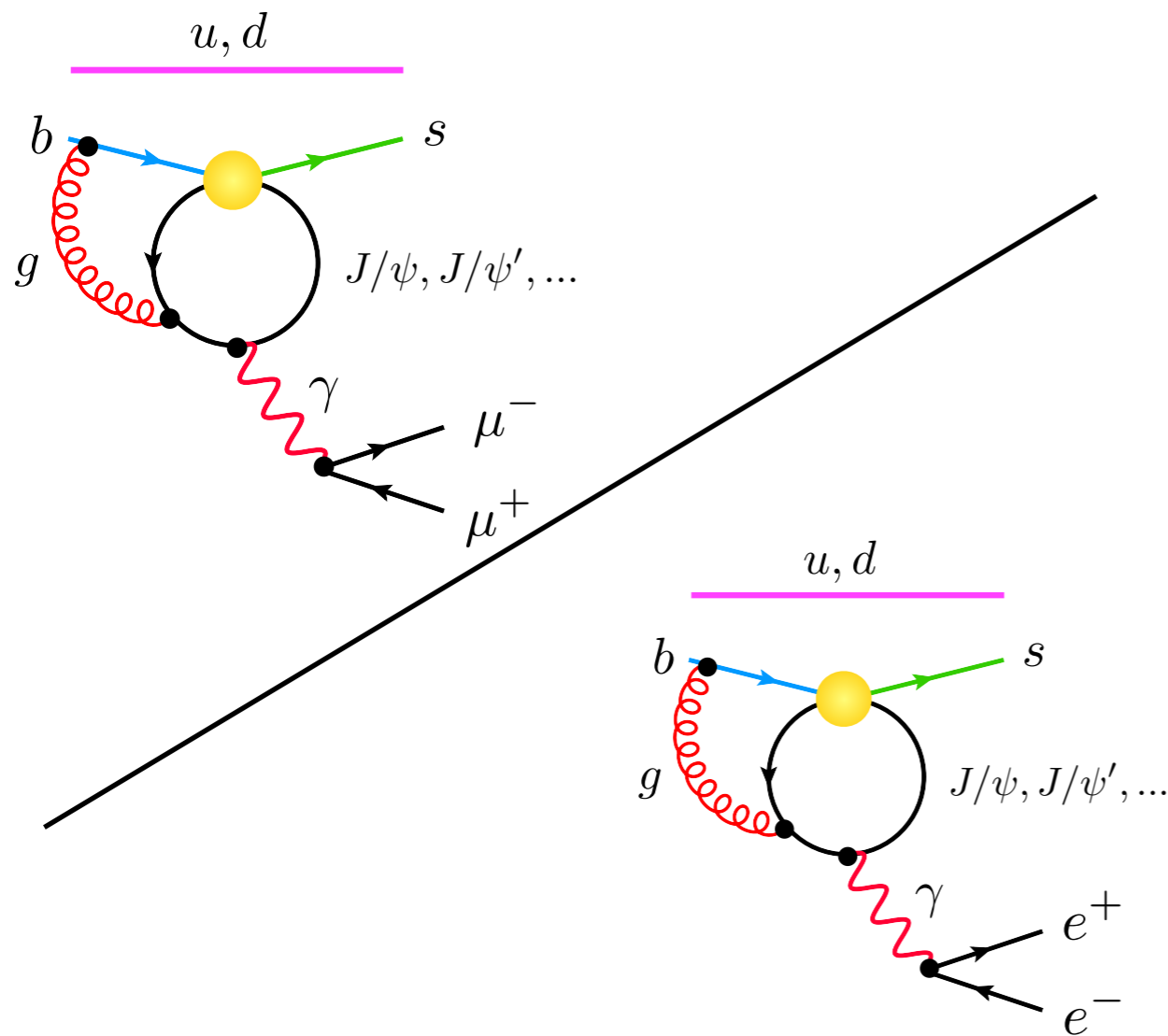
A pattern in $b \rightarrow s$ transitions

The fit is flat in q^2 and prefers no helicity amplitude at 1 sigma...



Lepton Non-Universality in $b \rightarrow s$

Much better: Measure ratios free from hadronic uncertainties

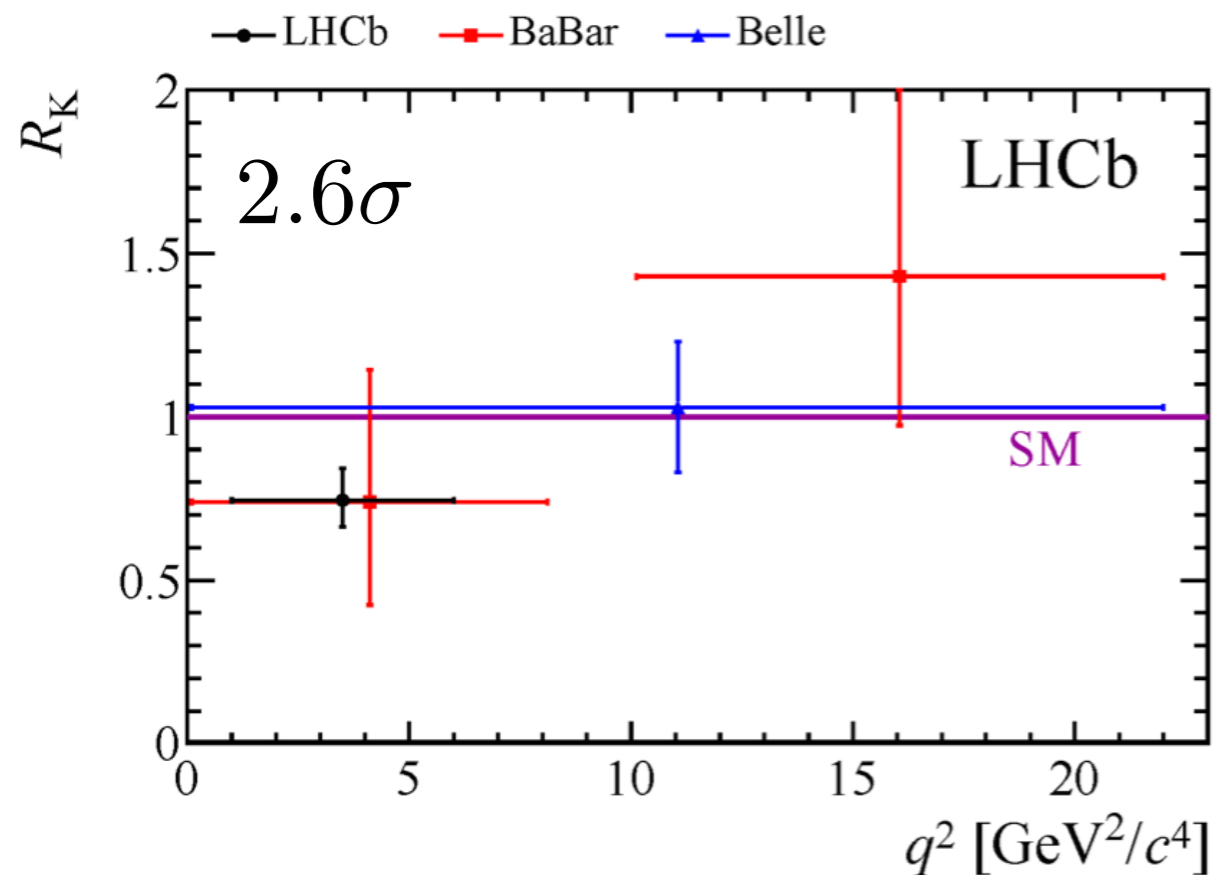


$$\frac{\Gamma(\bar{B} \rightarrow \bar{K} \mu^+ \mu^-)}{\Gamma(\bar{B} \rightarrow \bar{K} e^+ e^-)}$$

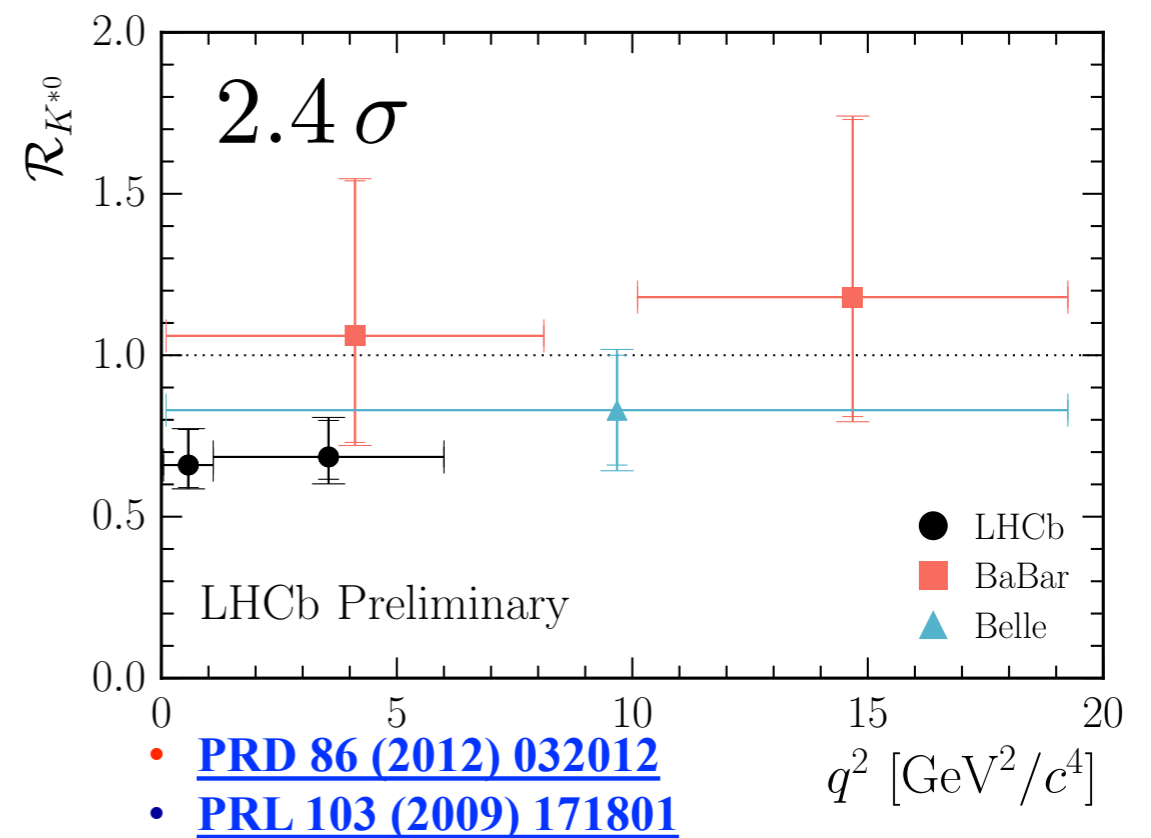
Lepton Non-Universality in $b \rightarrow s$

$$R_K = \frac{\Gamma(\bar{B} \rightarrow \bar{K} \mu^+ \mu^-)}{\Gamma(\bar{B} \rightarrow \bar{K} e^+ e^-)} = 0.745^{+0.090}_{-0.074} \pm 0.036$$

$$R_{K^*} = \frac{\Gamma(\bar{B} \rightarrow \bar{K}^* \mu^+ \mu^-)}{\Gamma(\bar{B} \rightarrow \bar{K}^* e^+ e^-)} = \begin{cases} 0.660^{+0.110}_{-0.070} \pm 0.024 \\ 0.685^{+0.113}_{-0.069} \pm 0.047 \end{cases}$$



[LHCb, 1406.6482]



[Simone Bifani CERN Seminar]
 [LHCb, 1705.05802]

Theoretically **very clean**, QED
 corrections $\sim 1\%$

[Bordone, Isidori, Pattori, 1605.07633]

Lepton Non-Universality in $b \rightarrow s$

What about the inclusive rate?

Hard to do at the LHC, because the second B meson cannot be reconstructed.

Belle:

$$R_{X_s} = \frac{\int_{1 \text{ GeV}^2}^{6 \text{ GeV}^2} dq^2 \frac{d\Gamma(B \rightarrow X_s \mu^+ \mu^-)}{dq^2}}{\int_{1 \text{ GeV}^2}^{6 \text{ GeV}^2} dq^2 \frac{d\Gamma(B \rightarrow X_s e^+ e^-)}{dq^2}} = 0.34 \pm 0.16$$

$R_{X_s}^{\text{SM}} = 1 - 4.3\%$ \longleftrightarrow 3.9σ

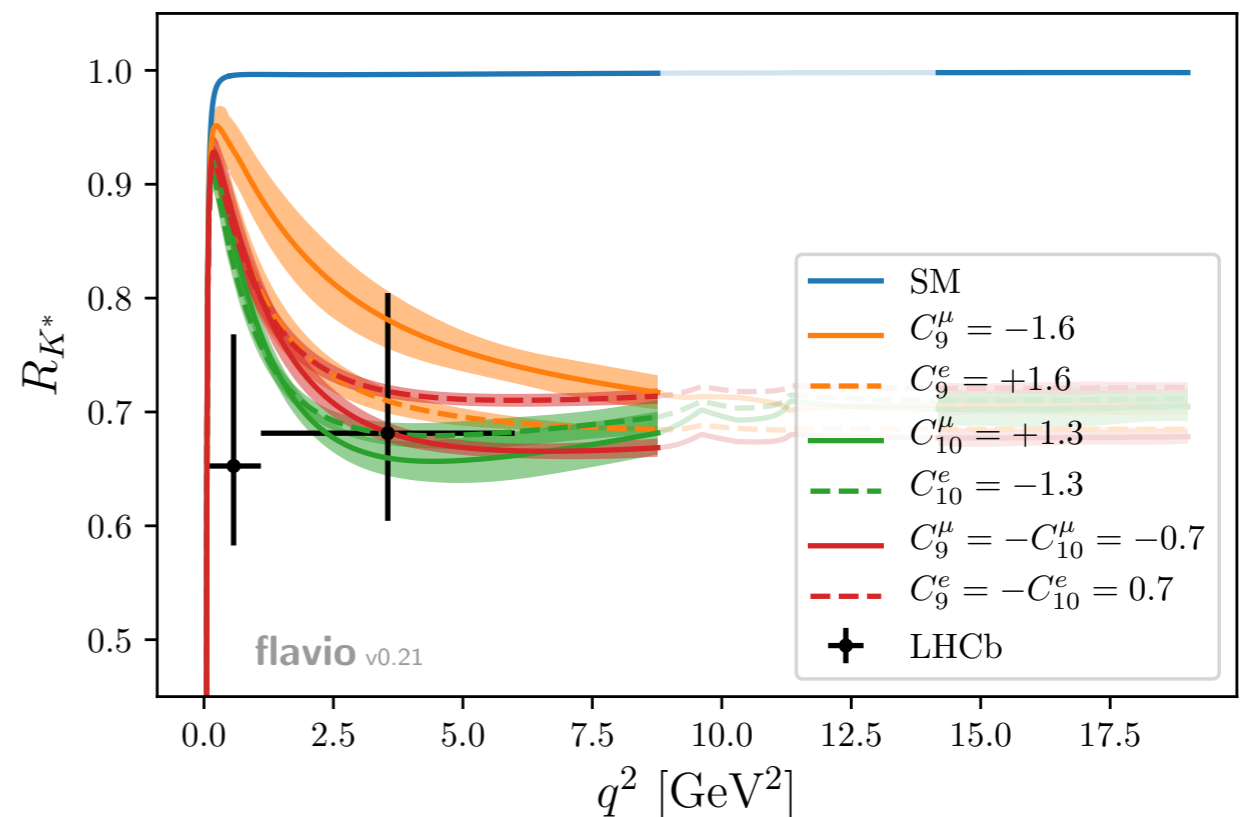
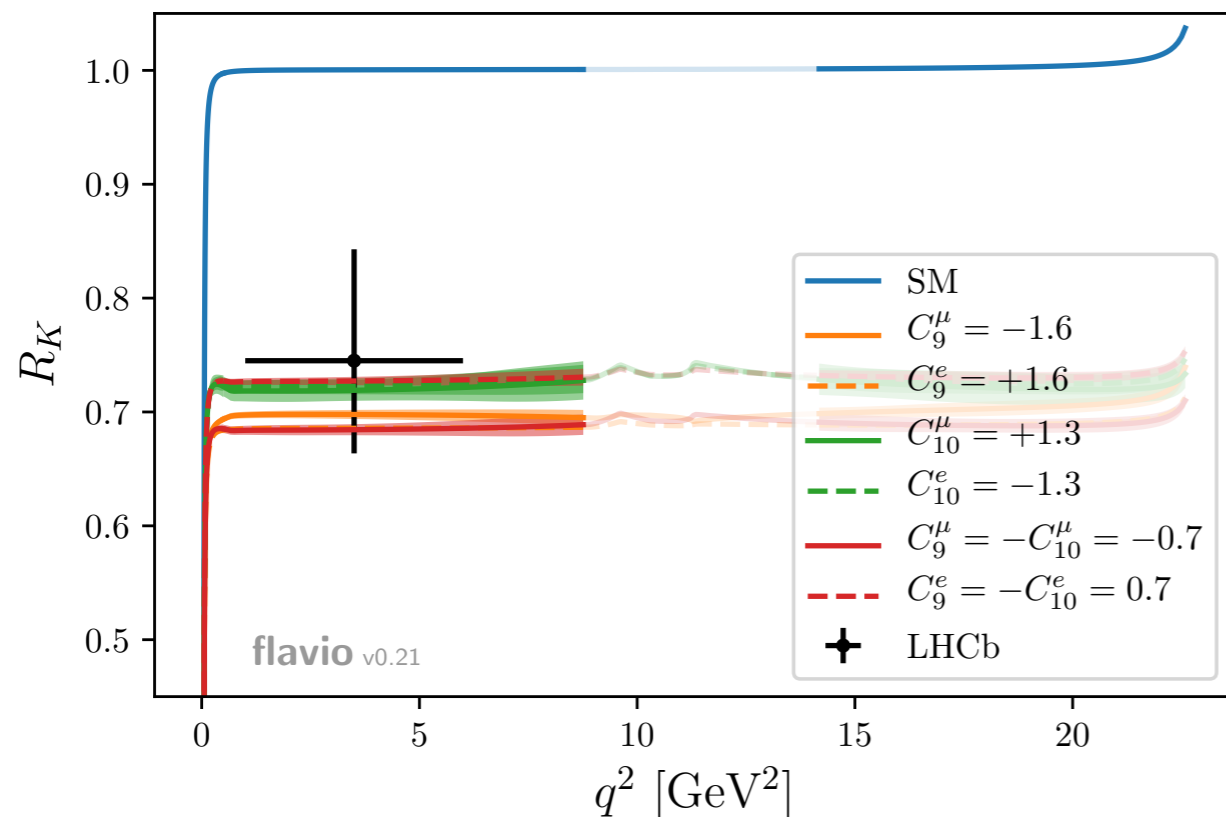
[<http://belle.kek.jp/belle/theses/doctor/2009/Nakayama.pdf>]

[from Haisch 2016]

Lepton Non-Universality in $b \rightarrow s$

$$R_K = \frac{\Gamma(\bar{B} \rightarrow \bar{K} \mu^+ \mu^-)}{\Gamma(\bar{B} \rightarrow \bar{K} e^+ e^-)} = 0.745^{+0.090}_{-0.074} \pm 0.036$$

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[Altmannshofer et al. 1704.05435]

Lepton Non-Universality in $b \rightarrow s$

Lepton flavour non-universality in R_K, R_{K^*}

$$R_K = 0.745^{+0.090}_{-0.074} \pm 0.036 \quad R_{K^*} = \begin{cases} 0.660^{+0.110}_{-0.070} \pm 0.024 \\ 0.685^{+0.113}_{-0.069} \pm 0.047 \end{cases} \quad R_{X_s} = 0.34 \pm 0.16$$

$$R_K \propto 1 + \text{Re}(C + C')$$

$$R_{K^*} \propto 1 + \text{Re}(C + C') - 2\text{Re}(C')$$

$$R_{X_s} \propto 1 + \text{Re}(C)$$

$$\frac{R_{K^*}}{R_K} \approx 1 \quad \Rightarrow \quad C' = 0$$

$$C \equiv C^\mu - C^e$$

killed by R_{K^*}

Coefficient	Best fit	1σ	3σ	Pull _{SM}
C_7^{NP}	-0.02	[-0.04, -0.00]	[-0.07, 0.04]	1.1
C_9^{NP}	-1.11	[-1.32, -0.89]	[-1.71, -0.40]	4.5
C_{10}^{NP}	0.58	[0.34, 0.84]	[-0.11, 1.41]	2.5
$C_{7'}^{\text{NP}}$	0.02	[-0.01, 0.04]	[-0.05, 0.09]	0.7
$C_{9'}^{\text{NP}}$	0.49	[0.21, 0.77]	[-0.33, 1.35]	1.8
$C_{10'}^{\text{NP}}$	-0.27	[-0.46, -0.08]	[-0.84, 0.28]	1.4
$C_9^{\text{NP}} = C_{10}^{\text{NP}}$	-0.21	[-0.40, 0.00]	[-0.74, 0.55]	1.0
$C_9^{\text{NP}} = -C_{10}^{\text{NP}}$	-0.69	[-0.88, -0.51]	[-1.27, -0.18]	4.1
$C_9^{\text{NP}} = C_{9'}^{\text{NP}}$	1.00	[-1.28, 0.88]	[-1.62, 0.42]	4.8

Lepton Non-Universality in $b \rightarrow s$

So... New Physics either in

$$C_9$$

or

$$C_9 = -C_{10}$$

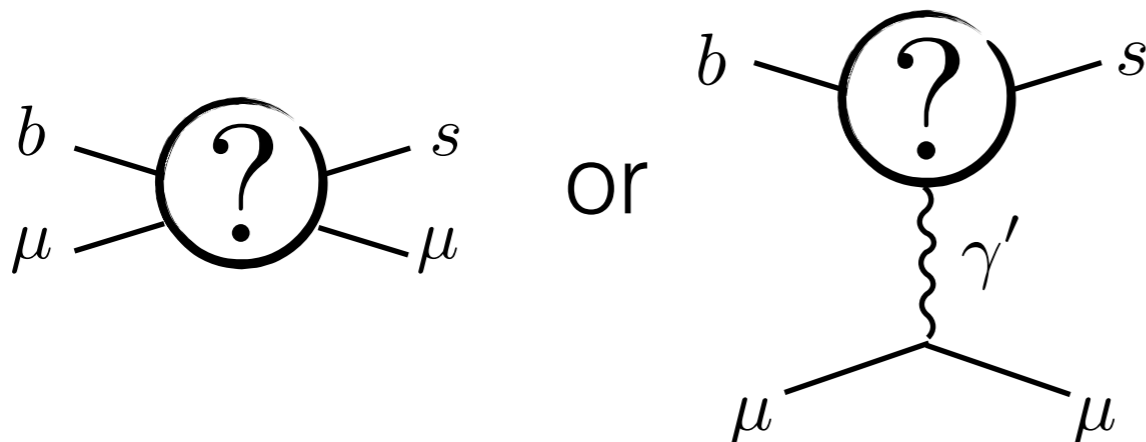
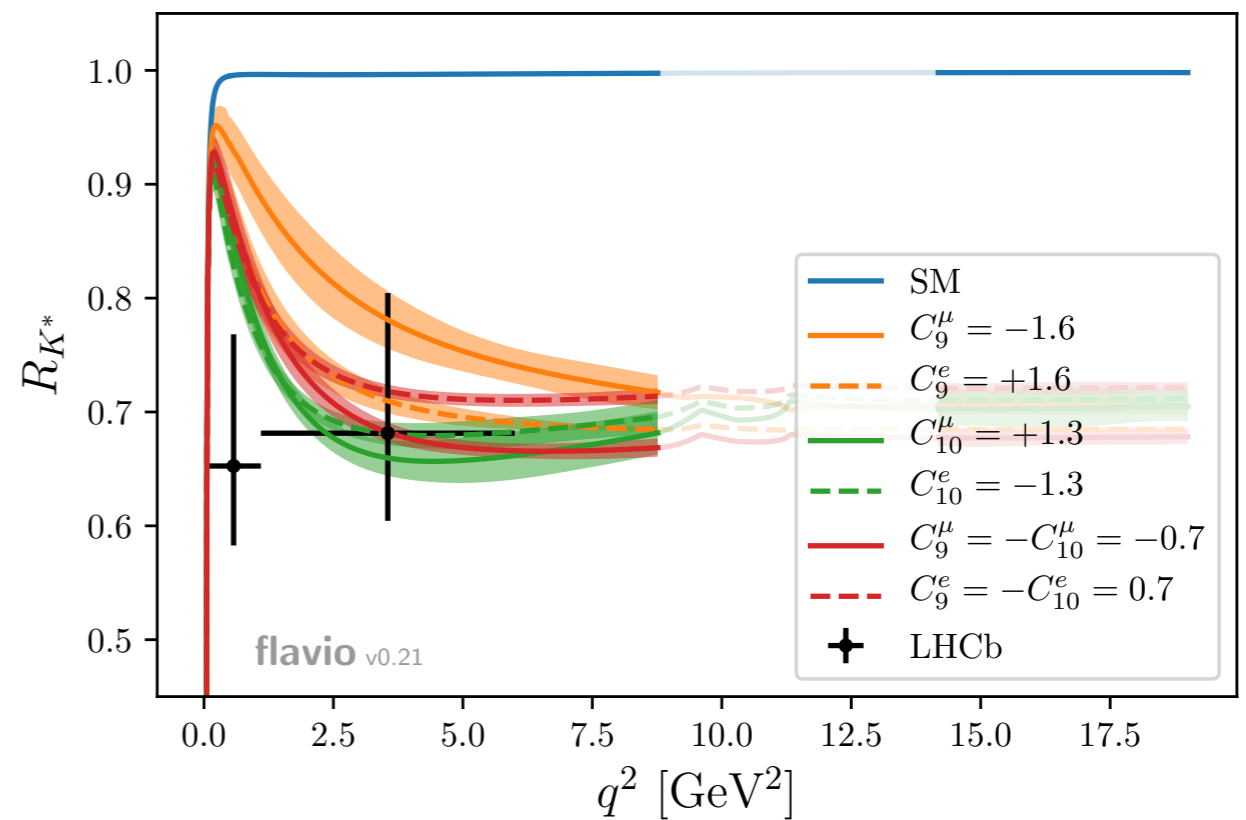
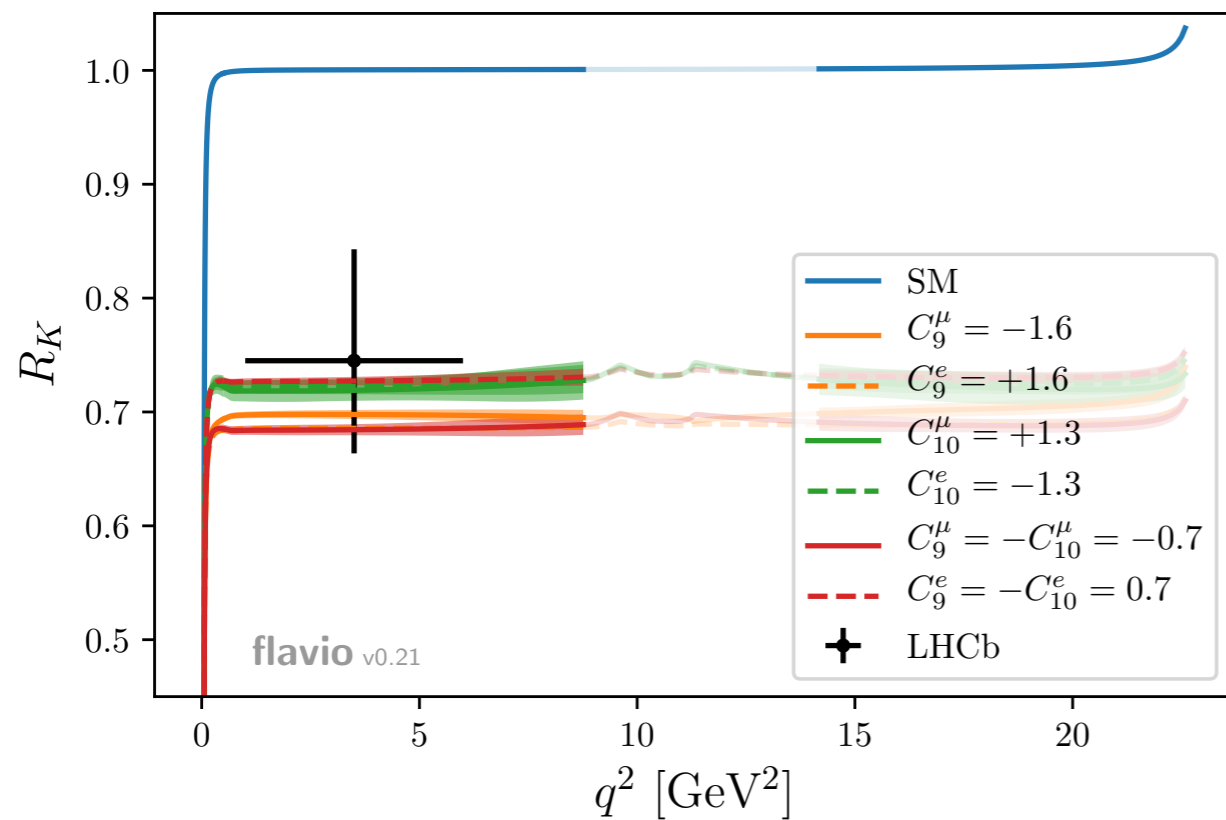
?



Lepton Non-Universality in $b \rightarrow s$

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[Altmannshofer et al. 1704.05435]

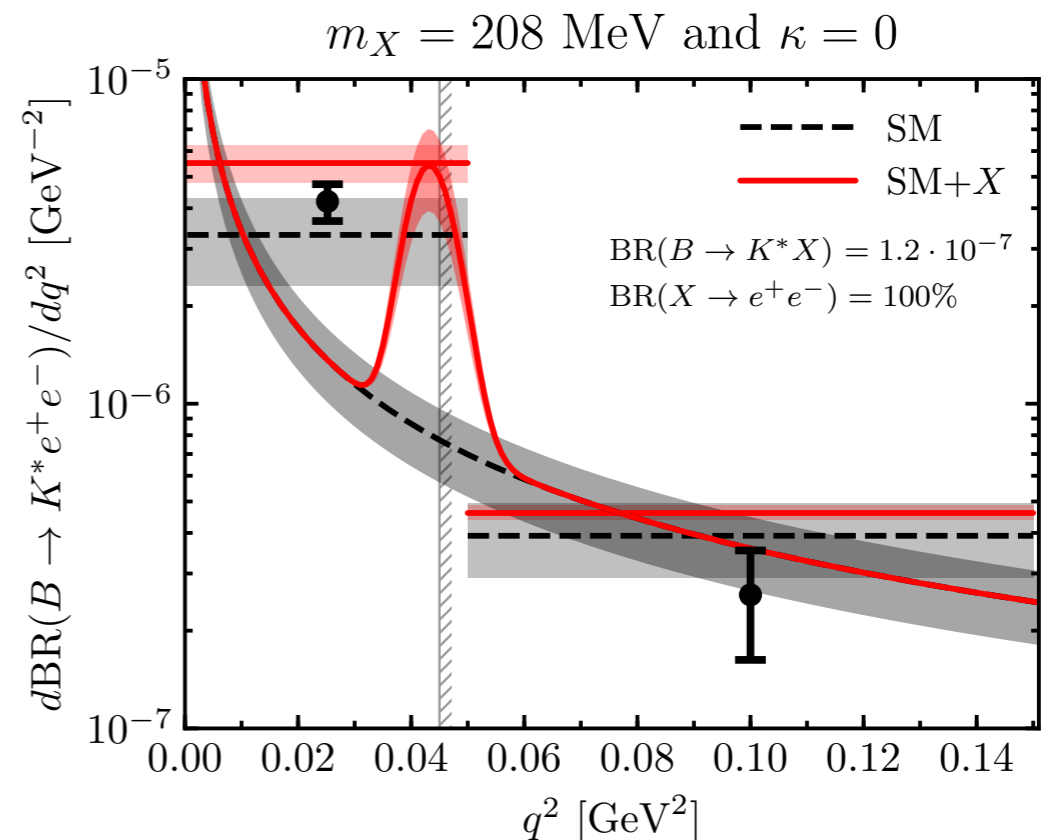
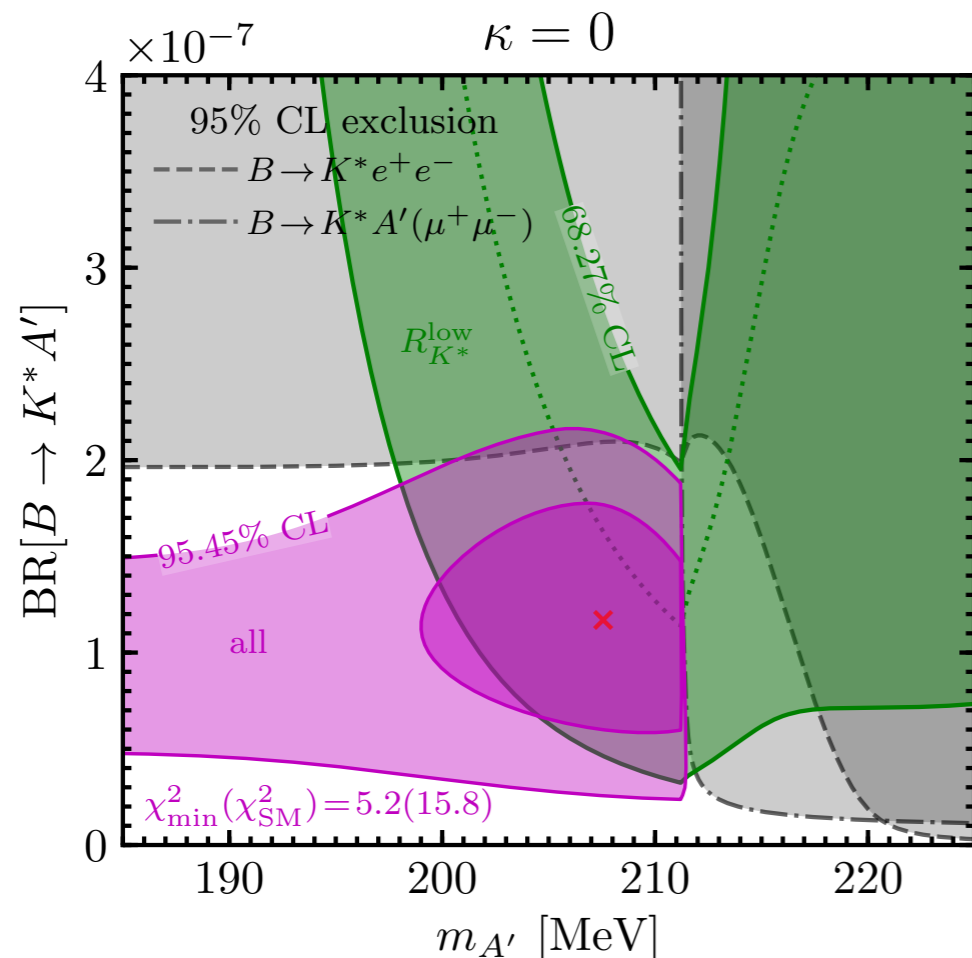
Lepton Non-Universality in $b \rightarrow s$

Any enhancement of the photon penguin is excluded by $B \rightarrow K^* \gamma$ and $B \rightarrow X_s \gamma$.

It cannot be an off-shell effect

$$\frac{\Gamma(B \rightarrow X_s X)}{\Gamma_{B,\text{tot}}^{\text{SM}}} \sim \frac{e^2}{4g_\ell^2} (\Delta R_{K^*})^2 \times \text{BR}(B \rightarrow X_s \gamma) \simeq 800\% \times \left(\frac{0.3 \cdot 10^{-3}}{g_\ell} \right)^2 \left(\frac{\Delta R_{K^*}}{0.3} \right)^2$$

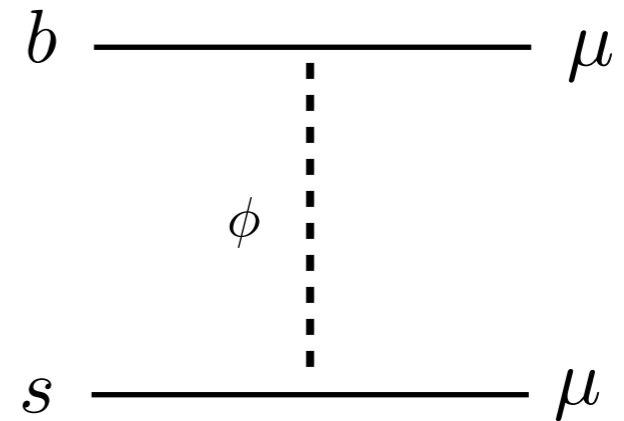
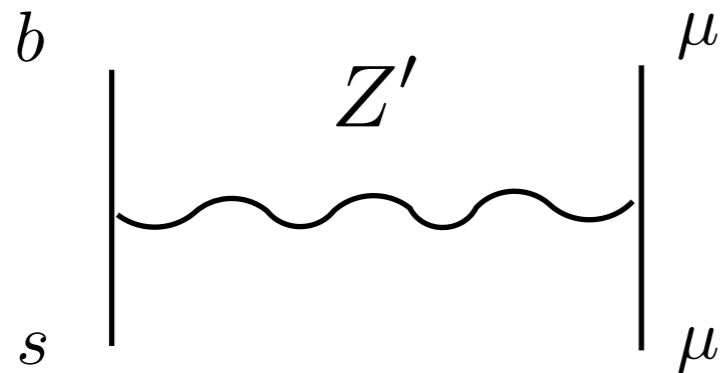
Needs an (additional) new on-shell resonance.



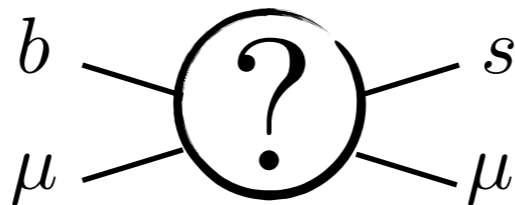
[Altmannshofer, Baker et al. 1711.07494]

Lepton Non-Universality in $b \rightarrow s$

What kind of new physics?



C_9



$C_9 = -C_{10}$



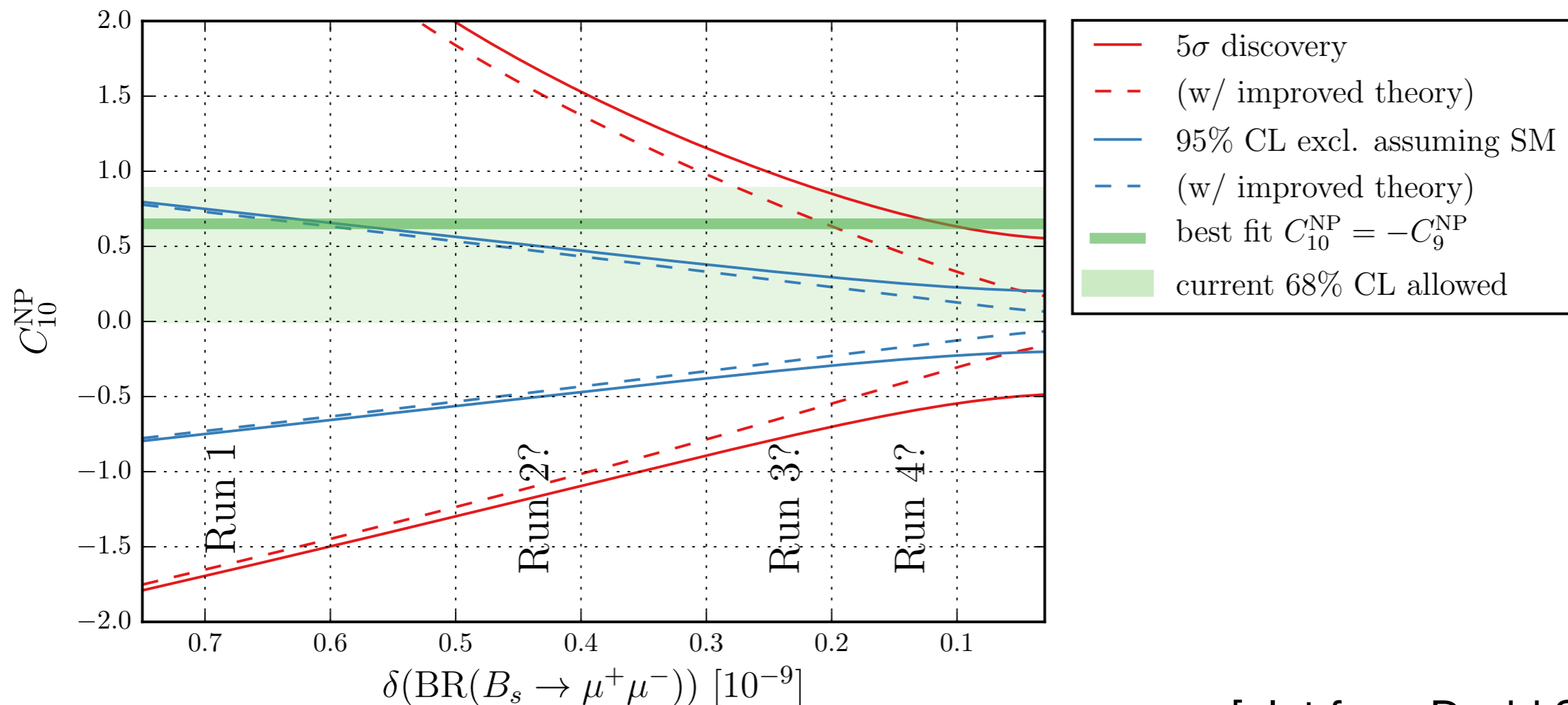
$$C_{9/10}^{\text{NP}} \approx C_{10}^{\text{SM}}/4 \Rightarrow \frac{1}{M^2} \left(\frac{2V_{tb}V_{ts}^*}{v^2} \frac{\alpha_e}{4\pi} \right)^{-1} = \frac{1}{4} \Rightarrow$$

$M \approx 35 \text{ TeV}$

Lepton Non-Universality in $b \rightarrow s$

Can we differentiate between leptoquarks and new Z' gauge bosons?

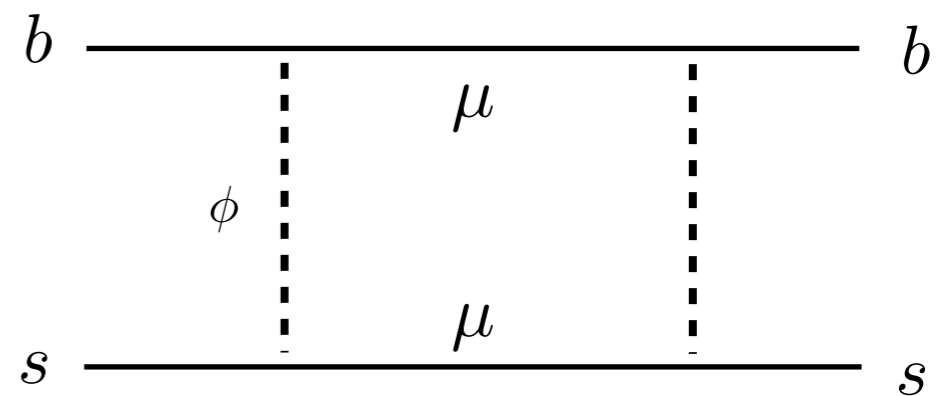
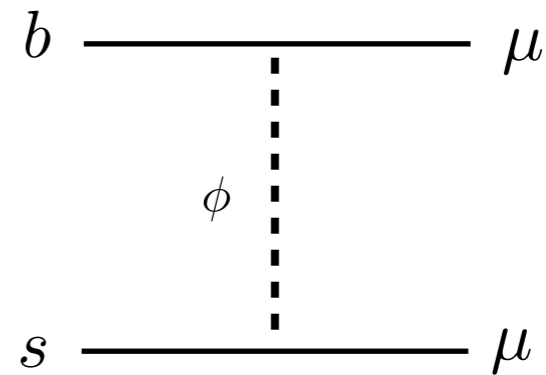
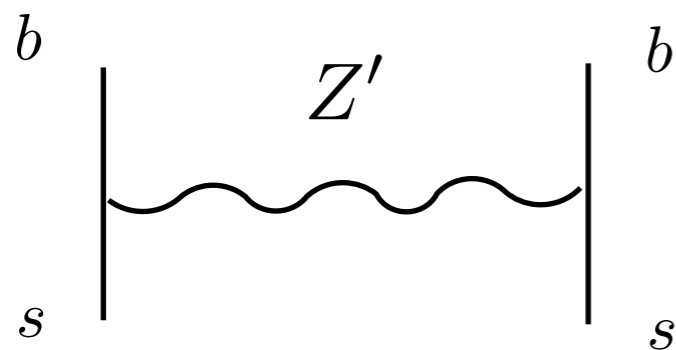
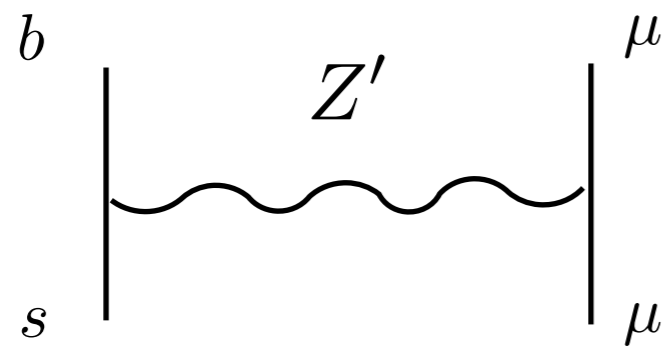
$$\frac{\text{Br}(B_s \rightarrow \mu^+ \mu^-)}{\text{Br}(B_s \rightarrow \mu^+ \mu^-)_{\text{SM}}} = \frac{|C_{10}^{\text{SM}} + C_{10}^{\text{NP}}|^2}{|C_{10}^{\text{SM}}|^2}$$



[plot from David Straub]

Lepton Non-Universality in $b \rightarrow s$

Can we differentiate between leptoquarks and new Z' gauge bosons?



Lepton Non-Universality in $b \rightarrow s$

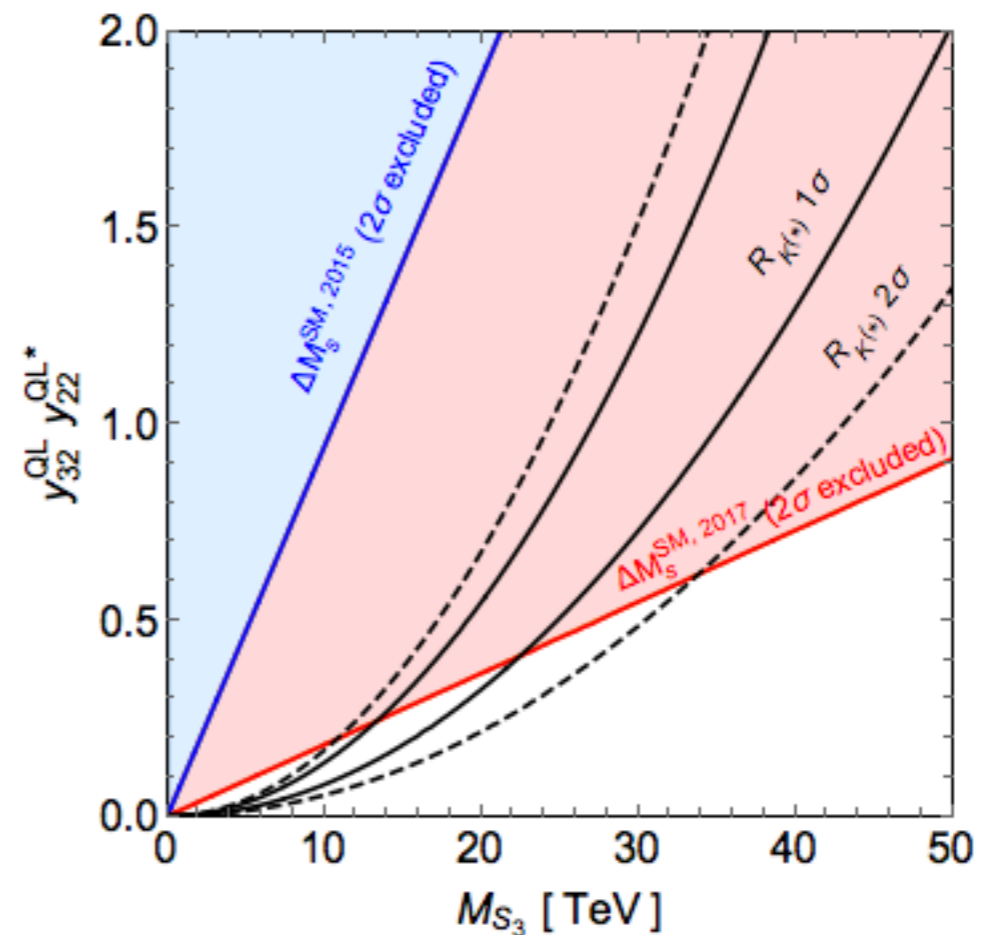
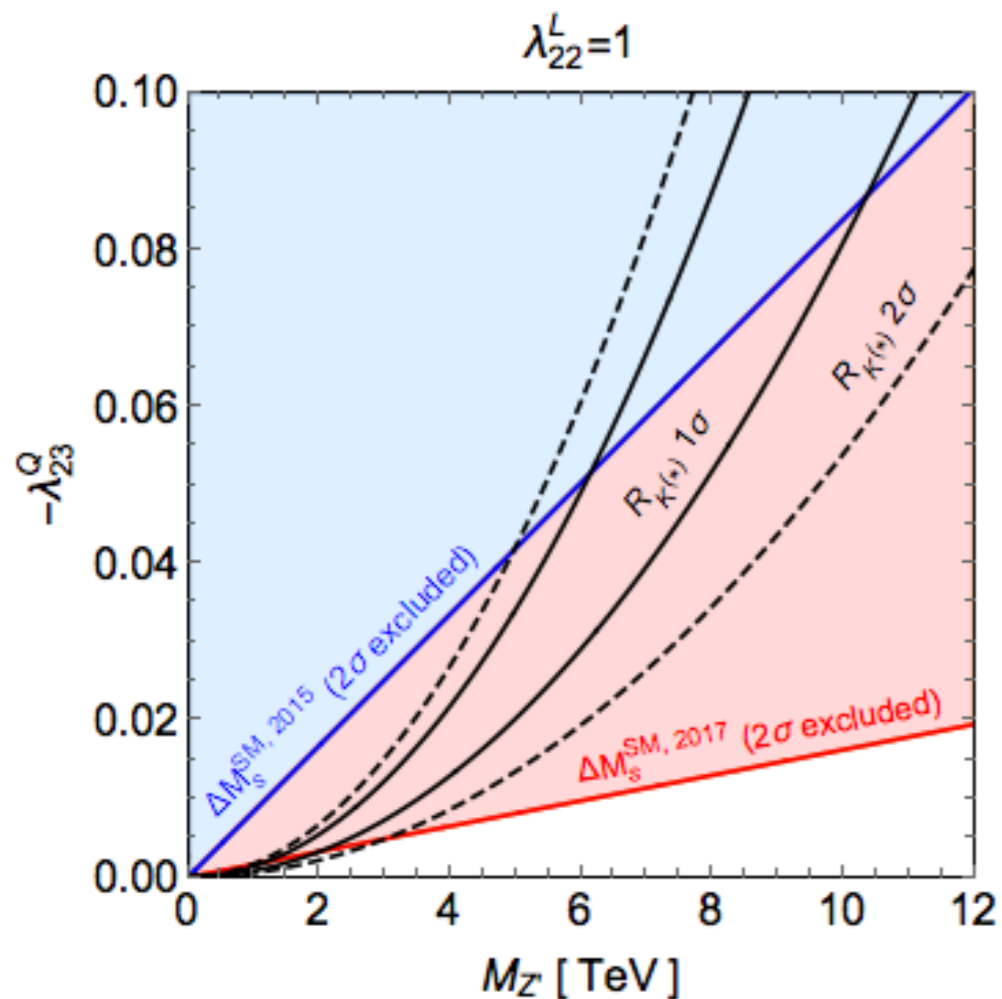
Can we differentiate between leptoquarks and new Z' gauge bosons?

$$\Delta M_s^{\text{SM}, 2015} = (18.3 \pm 2.7) \text{ ps}^{-1}$$



$$\Delta M_s^{\text{SM}, 2017} = (20.01 \pm 1.25) \text{ ps}^{-1}$$

$$\Delta M_s^{\text{Exp}} = (17.757 \pm 0.021) \text{ ps}^{-1}$$



Lepton Non-Universality in $b \rightarrow s$

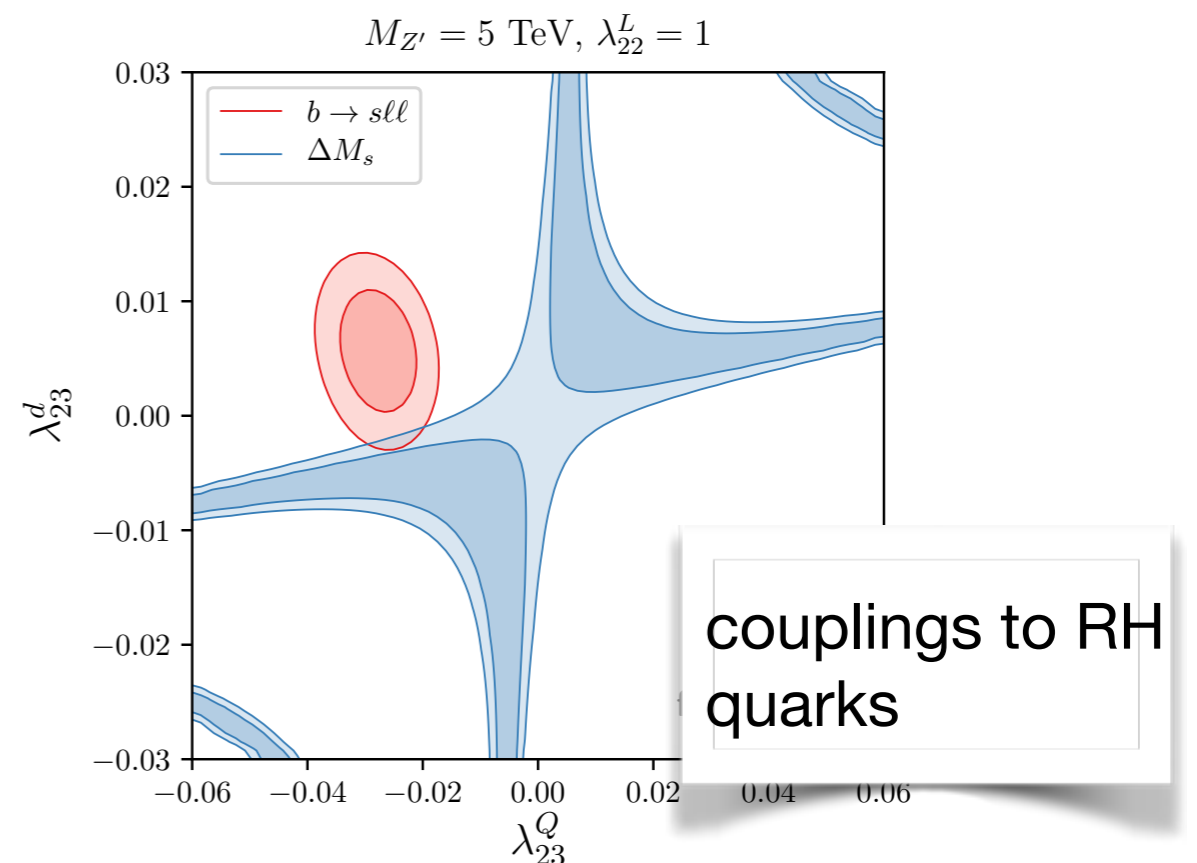
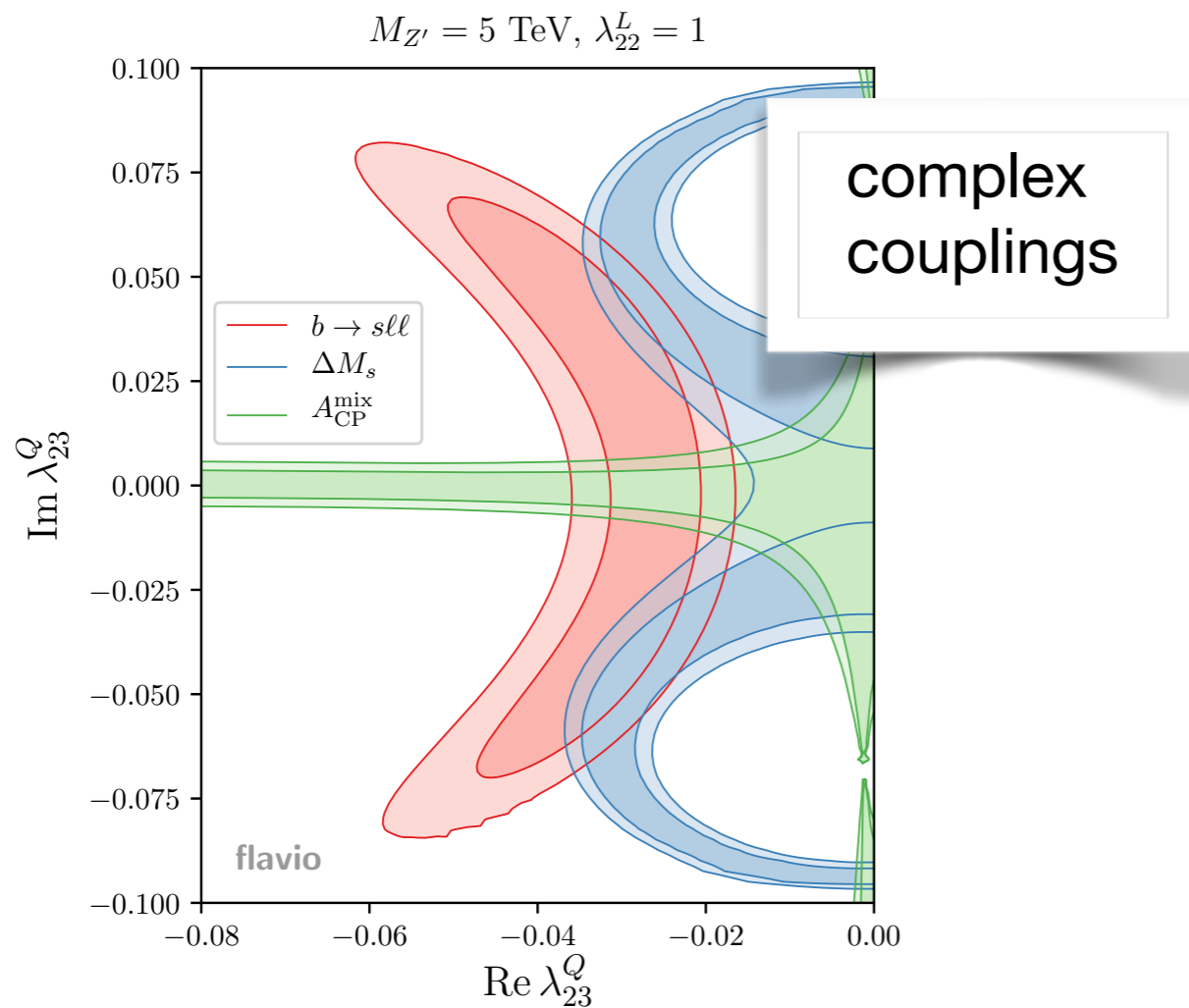
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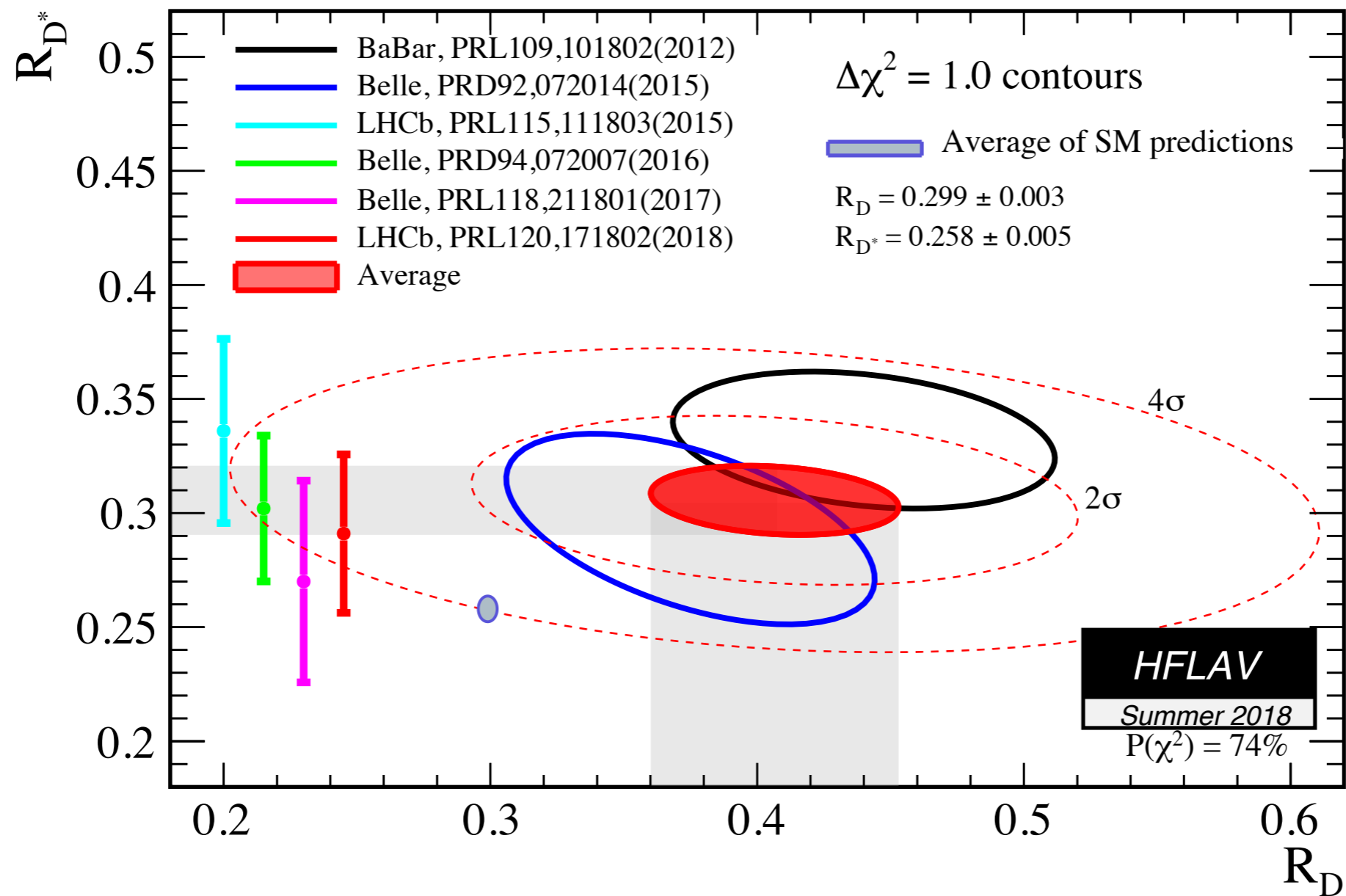
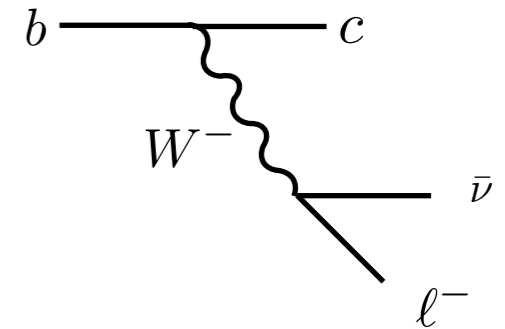
Z' needs to couple to electrons...

[di Luzio, Kirk, Lenz, 1811.12884]

Lepton Non-Universality in $b \rightarrow c$

Lepton Non-Universality in $b \rightarrow c$

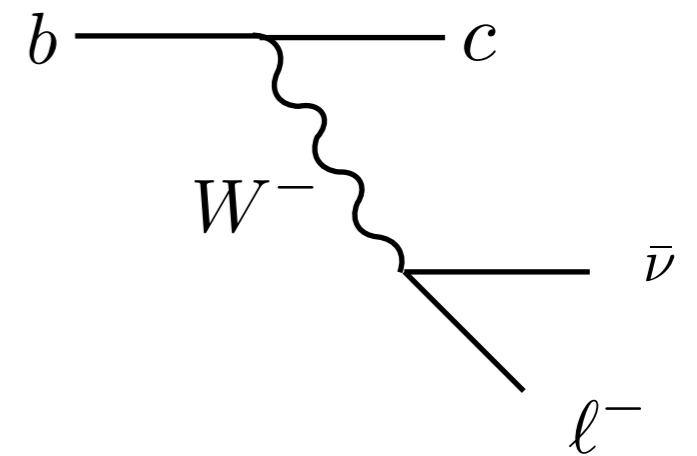
Anomaly in $R(D^{(*)}) = \frac{\bar{B} \rightarrow D^{(*)} \tau \bar{\nu}}{\bar{B} \rightarrow D^{(*)} \ell \bar{\nu}}$



Lepton Non-Universality in $b \rightarrow c$

Anomaly in $R(D^{(*)}) = \frac{\text{Br}(\bar{B} \rightarrow D^{(*)} \tau \nu)}{\text{Br}(\bar{B} \rightarrow D^{(*)} \ell \nu)}$

Anomaly in $R(J/\psi) = \frac{\text{Br}(B_c^+ \rightarrow J/\psi \tau^+ \nu)}{\text{Br}(B_c^+ \rightarrow J/\psi \mu^+ \nu)}$



Observable	SM prediction	Measurement
R_D	0.300 ± 0.008 [1]	0.407 ± 0.046 [3]
	0.299 ± 0.011 [2]	
	0.299 ± 0.003 [4]	
R_{D^*}	0.252 ± 0.003 [5]	0.304 ± 0.015 [3]
	0.260 ± 0.008 [6]	
$P_\tau(D^*)$	-0.47 ± 0.04 [6]	$-0.38 \pm 0.51(\text{stat.})^{+0.21}_{-0.16}(\text{syst.})$ [7, 8]
$R_{J/\psi}$	0.290	0.71 ± 0.25 [9]

[LHCb, 1711.05623]

$F_L(D^*) = 0.6 \pm 0.08 \pm 0.03$

D* polarization, Belle

[Nishida, CKM 2018]

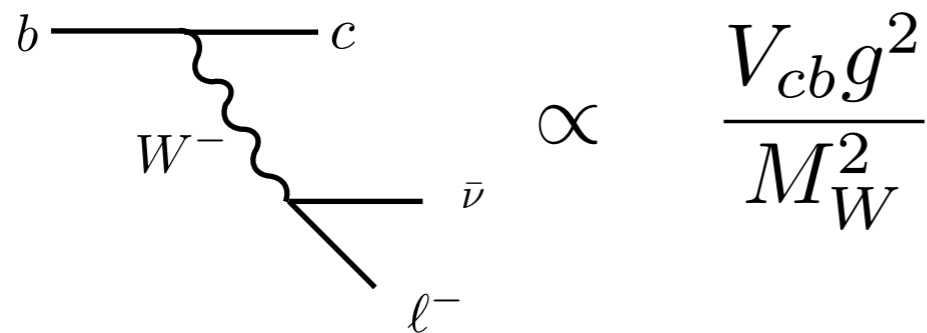
[Azatov et al., 1805.03209]

[Aebischer et al, 1810.07698]

Lepton Non-Universality in $b \rightarrow c$

	Measurement	SM Prediction
$R(D^{(*)}) = \frac{\bar{B} \rightarrow D^{(*)} \tau \bar{\nu}}{\bar{B} \rightarrow D^{(*)} \ell \bar{\nu}}$	$0.388 \pm 0.047, \quad D$	$0.300 \pm 0.010, \quad D$
	$0.321 \pm 0.021, \quad D^*$	$0.252 \pm 0.005, \quad D^*$

SM contribution is tree-level...

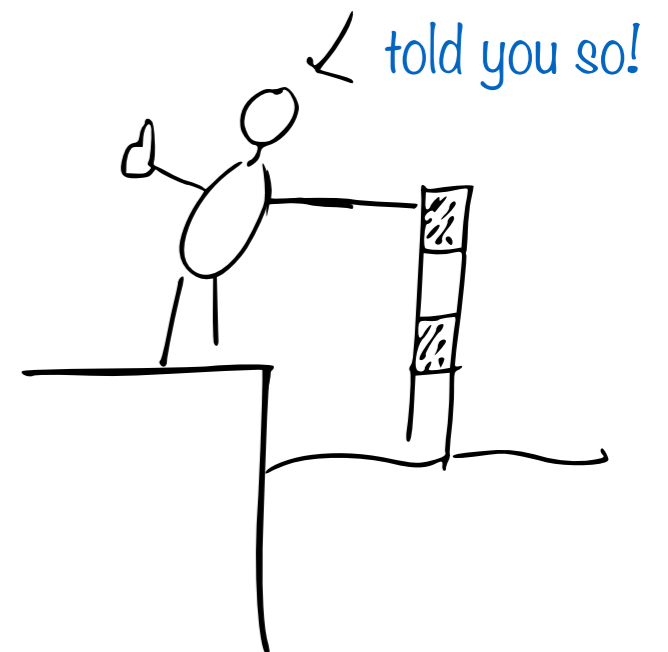


...and we want a 10-20% shift

Needs a large new physics contribution:

$$C_{NP} \approx C_{SM}/10 \quad \Rightarrow \quad \frac{1}{V_{cb}} \left(\frac{v}{M} \right)^2 = \frac{1}{10}$$

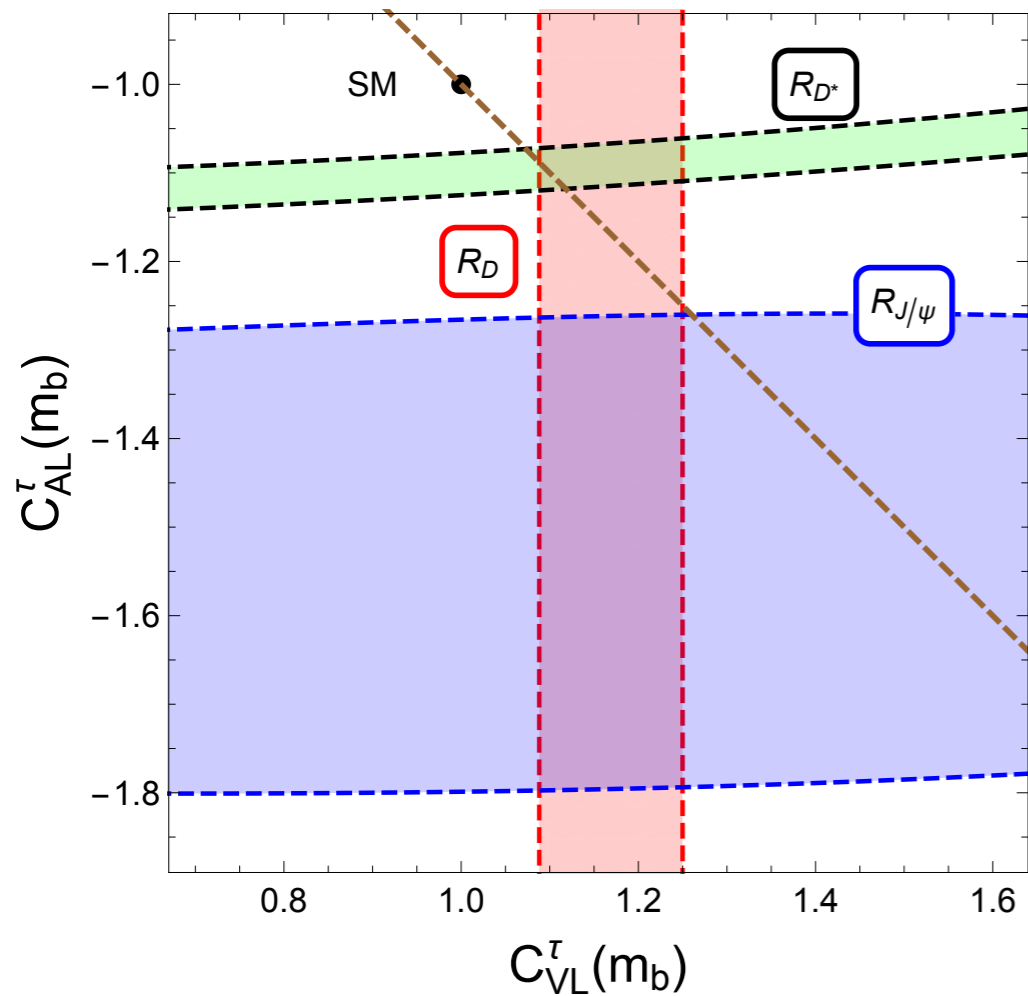
$$M = 1 - 5 \text{ TeV}$$



Lepton Non-Universality in $b \rightarrow c$

Rescaling the SM operator gives a good fit.

A new TeV scale vector boson? Needs

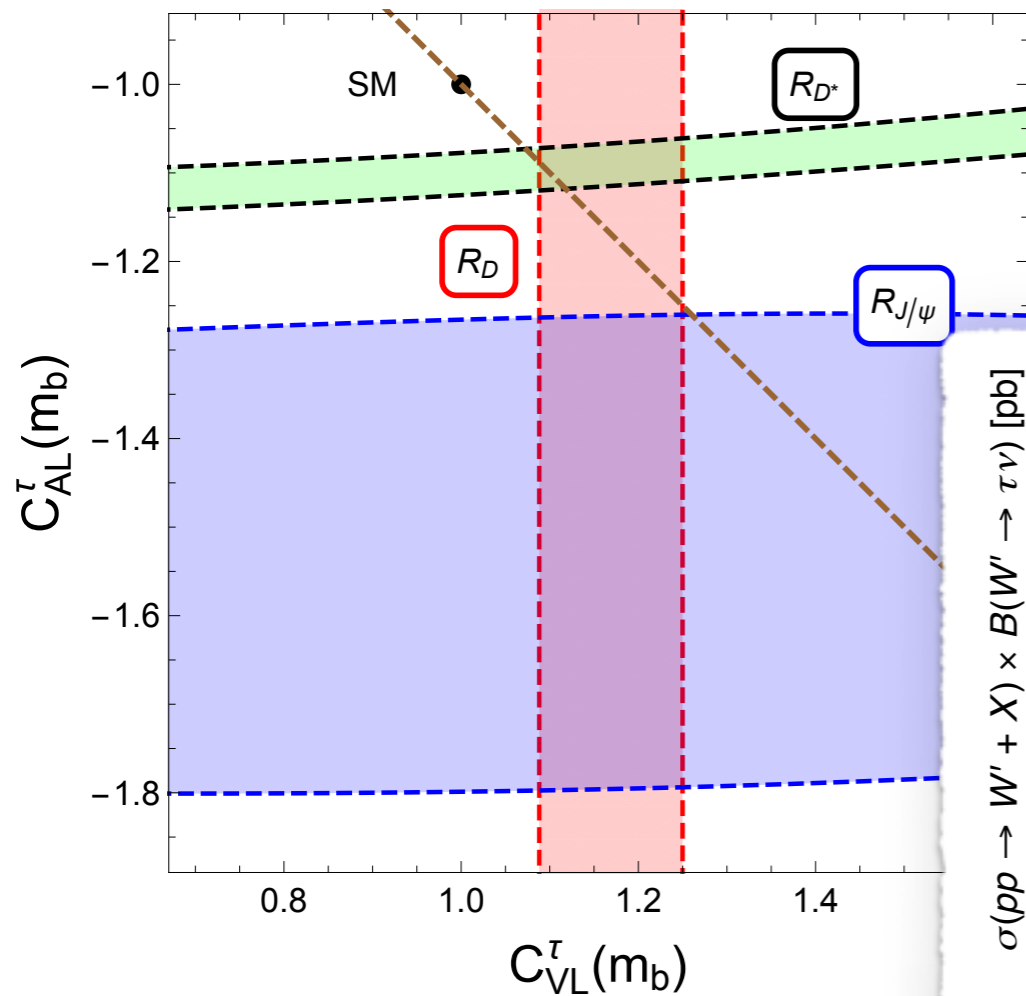


$$0.2 \approx g^2 |V_{cb}|^2 \left(\frac{\text{TeV}}{M_{W'}} \right)^2$$

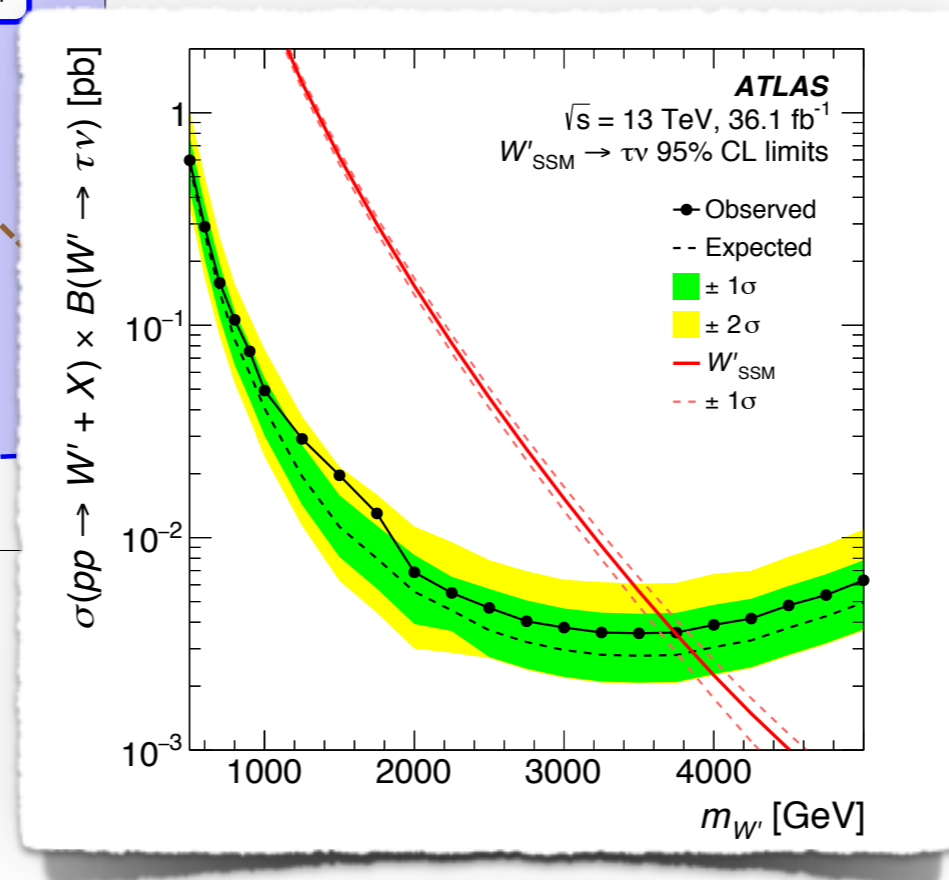
Lepton Non-Universality in $b \rightarrow c$

Rescaling the SM operator gives a good fit.

A new TeV scale vector boson? Needs



$$0.2 \approx g^2 |V_{cb}|^2 \left(\frac{\text{TeV}}{M_{W'}} \right)^2$$



Excluded by LHC searches

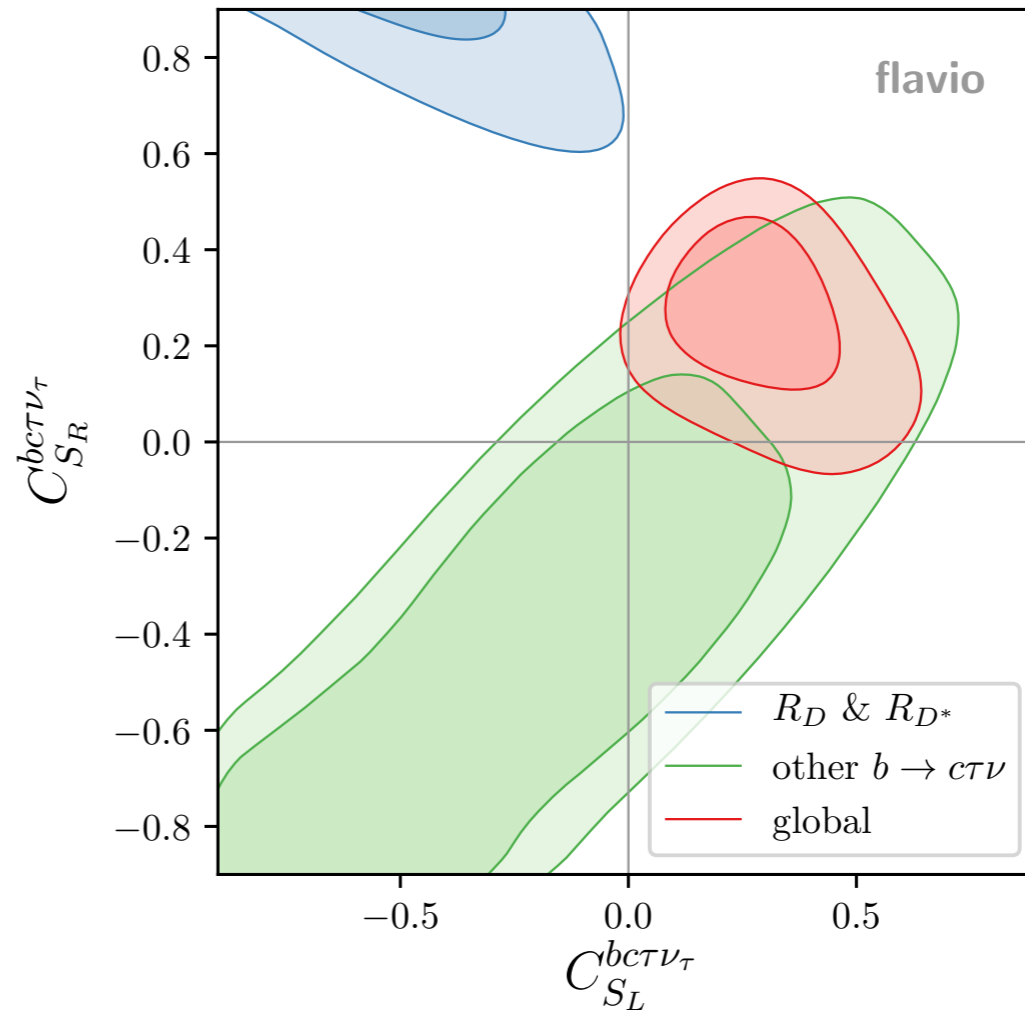
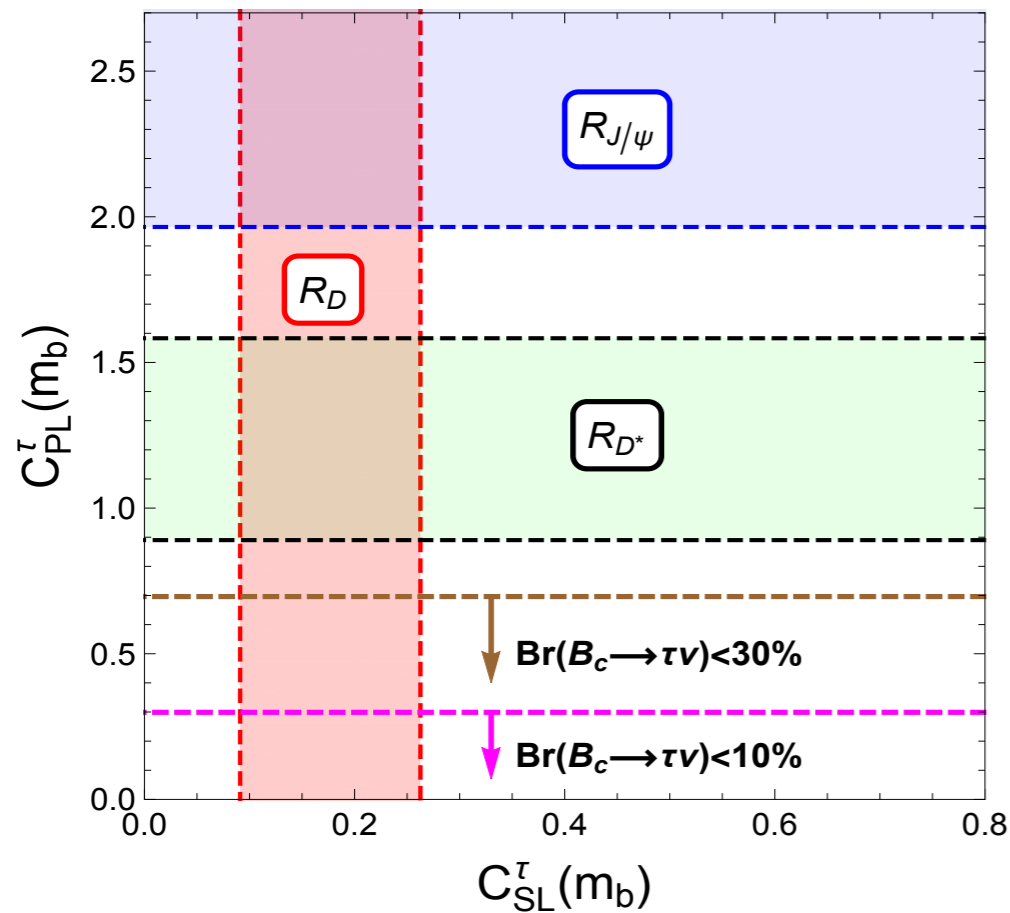
[Atlas et al. , 1801.06992]

[Azatov et al. , 1805.03209]

Lepton Non-Universality in $b \rightarrow c$

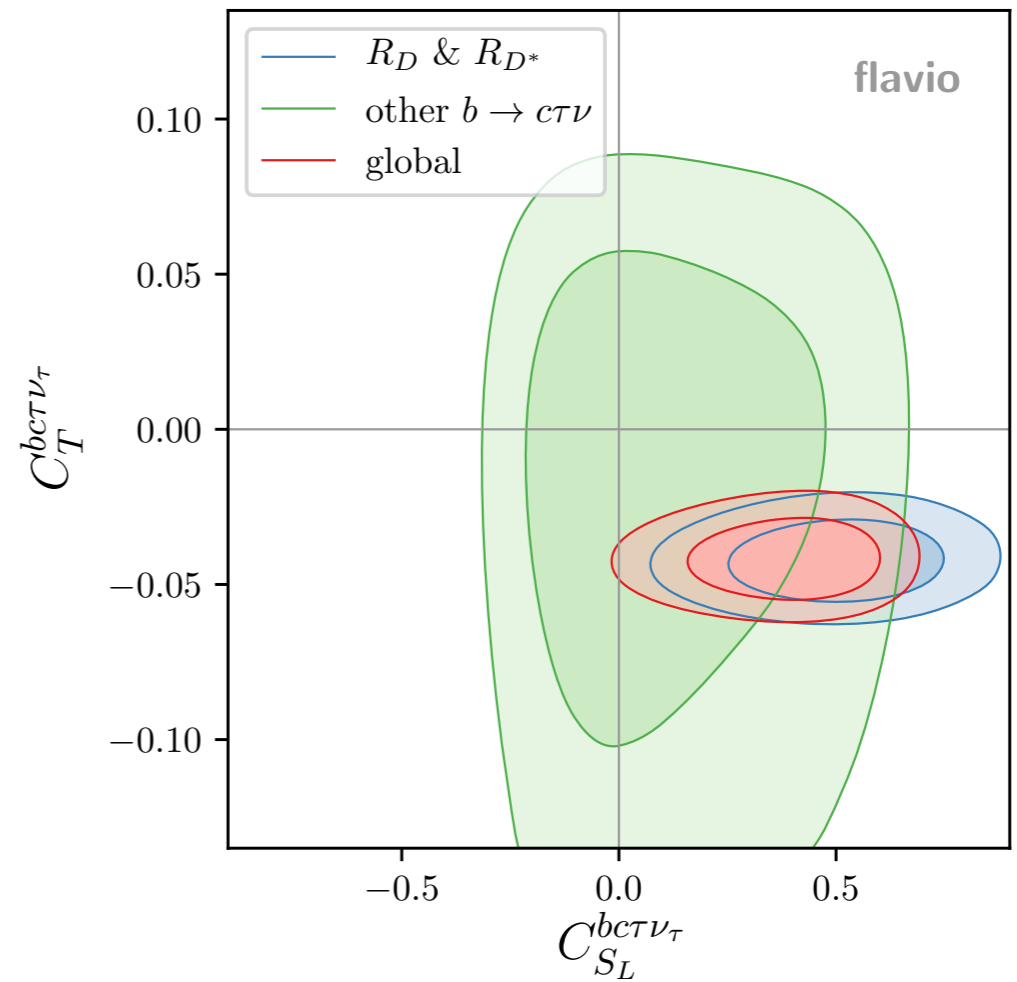
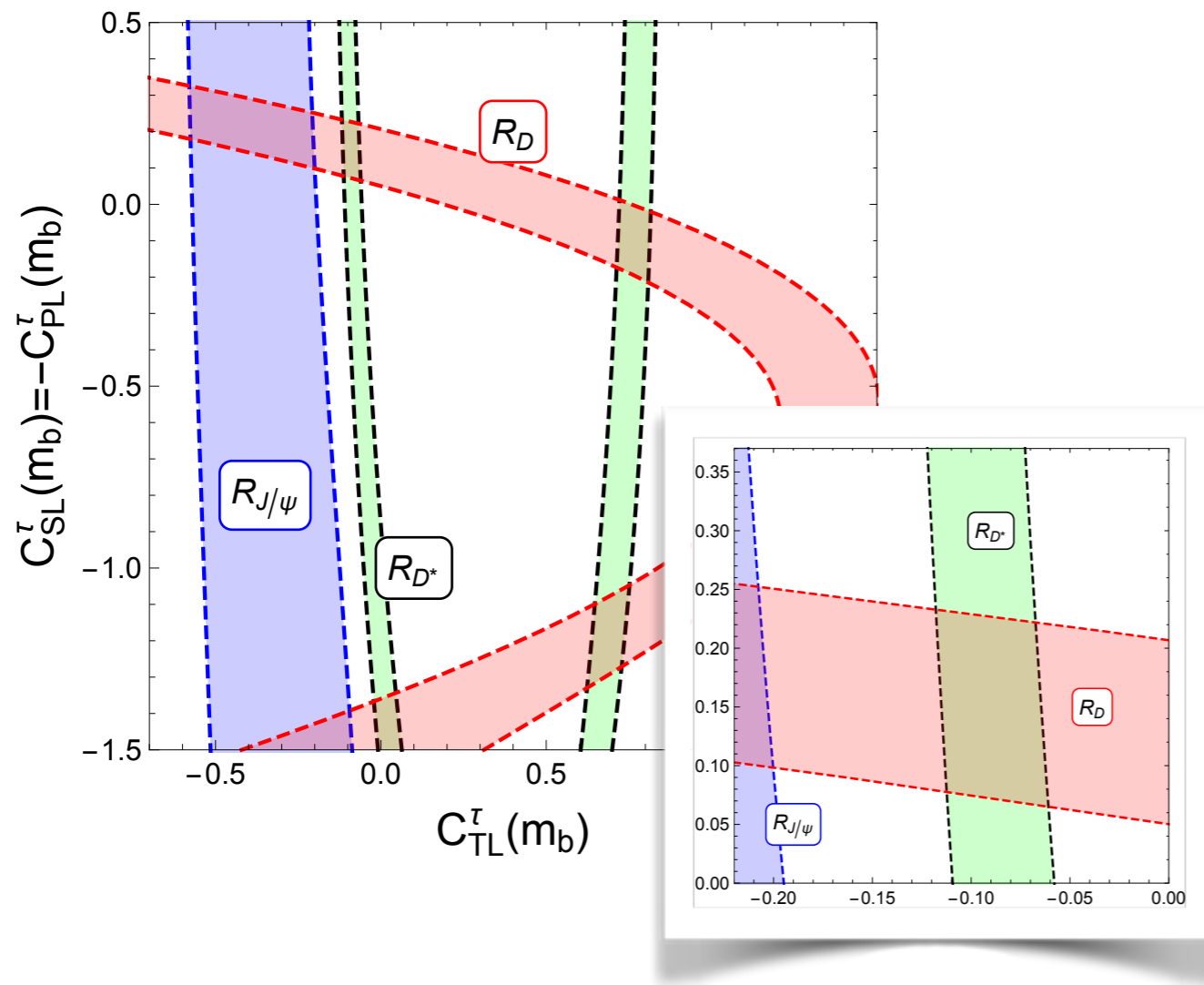
A new TeV-scale scalar?

In tension with $\text{Br}(B_c \rightarrow \tau\nu)$ [Akeroyd, Chen, 1708.04072]



Lepton Non-Universality in $b \rightarrow c$

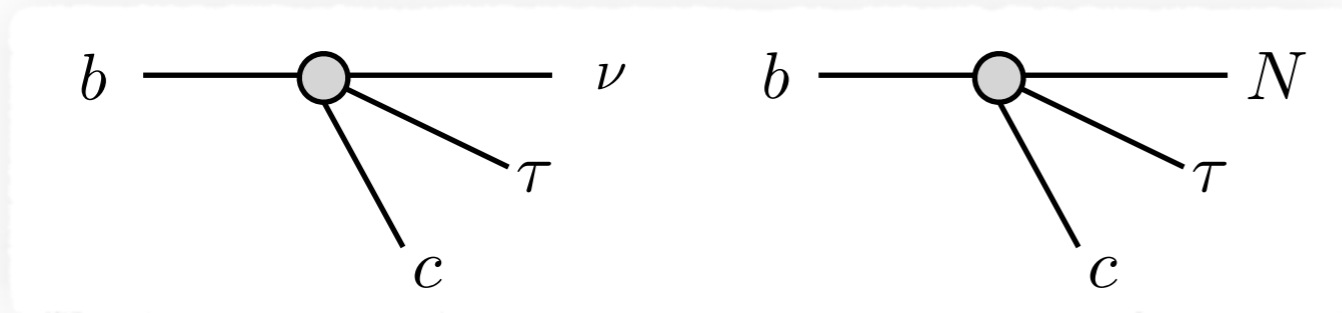
Leptoquarks? $(\bar{c}P_L\nu)(\bar{\tau}P_Lb) = -\frac{1}{8} \left[2(\mathcal{O}_{SL}^\tau - \mathcal{O}_{PL}^\tau) + \mathcal{O}_{TL}^\tau \right]$



An unconventional solution

If there are light right-handed Neutrinos,

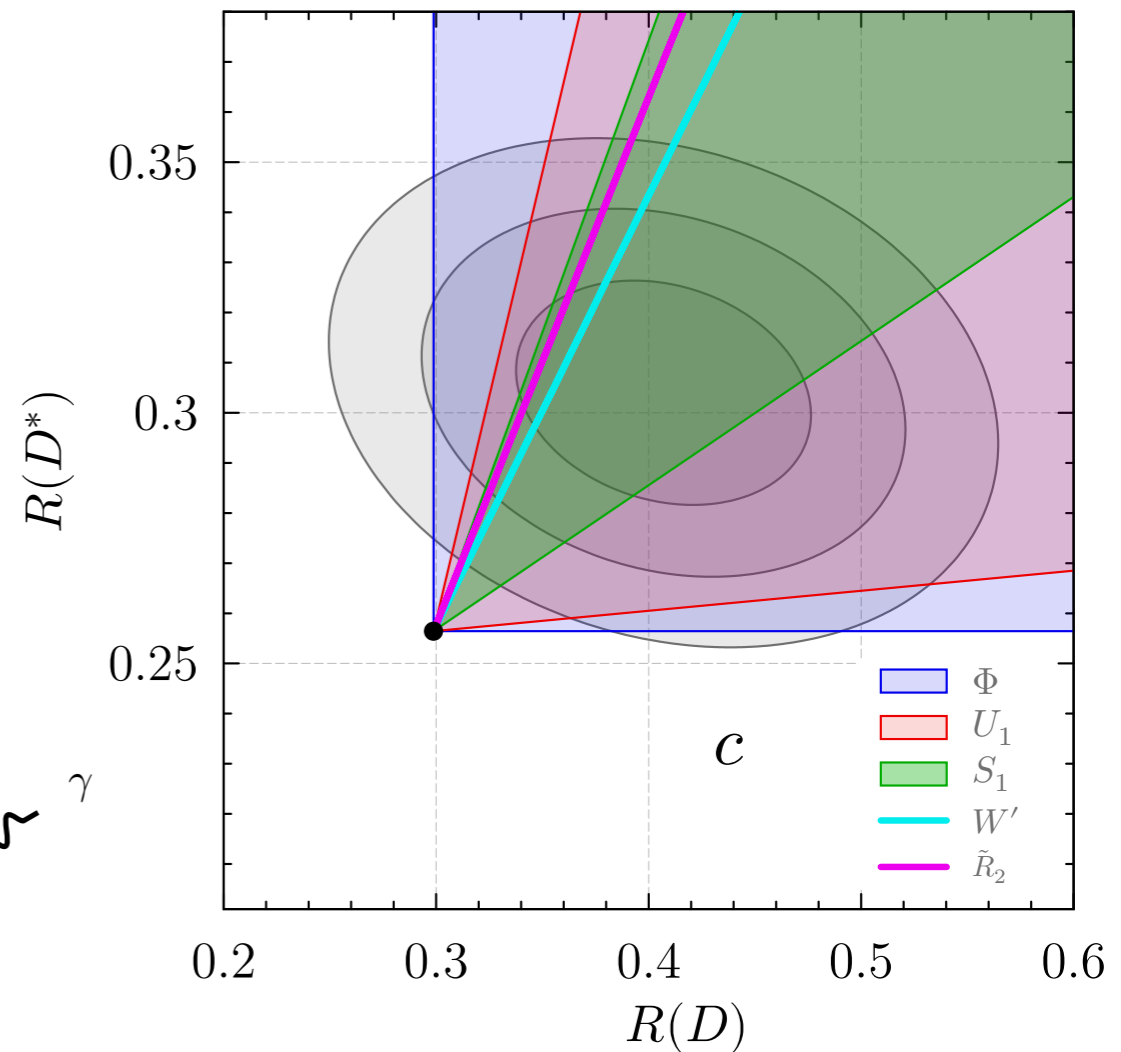
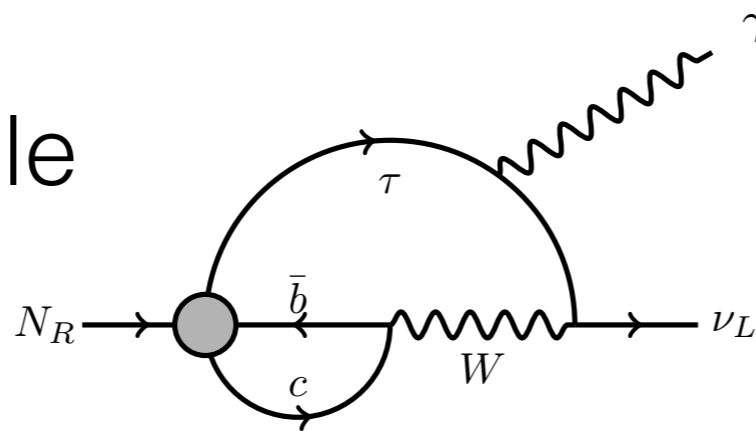
$$m_N < m_{B_s} - m_{D^*} - m_\tau \approx 1.5 \text{ GeV}$$



Experimentally indistinguishable

they are not stable

$$\tau_N = 1 - 10^{13} \text{ s}$$



Are we sure this time?



Are we sure this time?

The most recent calculation of the inclusive cross section...

	SM	Experiment
$\text{Br}(B^+ \rightarrow D^0 \tau^+ \nu_\tau)$	$(0.75 \pm 0.13) \%$	$(0.91 \pm 0.11) \%$
$\text{Br}(B^+ \rightarrow D^{*0} \tau^+ \nu_\tau)$	$(1.25 \pm 0.09) \%$	$(1.77 \pm 0.11) \%$
$\text{Br}(B^+ \rightarrow X_c \tau^+ \nu_\tau)$	$(2.37 \pm 0.08) \%$	$(2.41 \pm 0.23) \%$

[Mannel, Rusov, Shahriaran, 1702.01089]

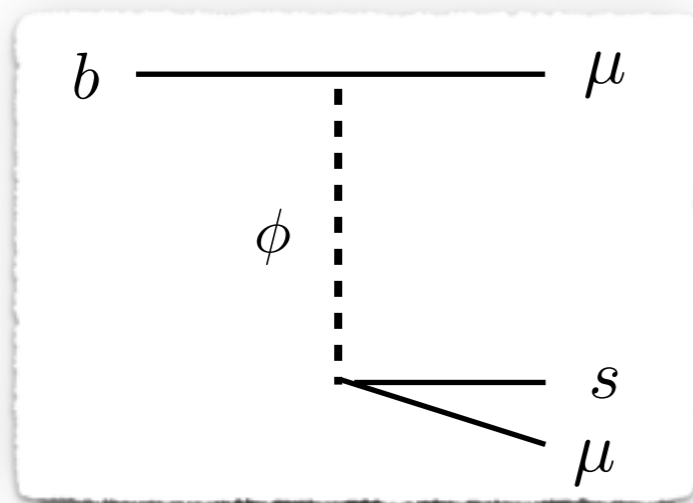
$$0.91 + 1.77 = 2.68$$

A combined explanation?

A combined explanation?

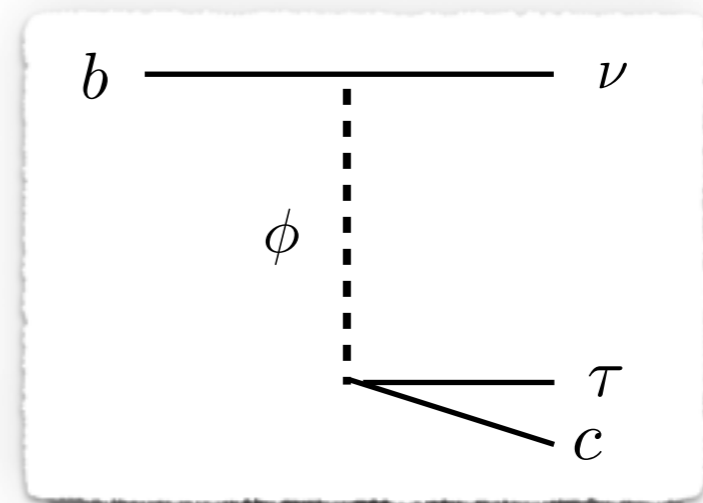
- Anomalies in neutral and charged $b \rightarrow 2\text{nd}$ generation transition can be described by leptoquark currents
- However, one needs leptoquarks with different properties

$b \rightarrow s$



$$M_\phi = 35 \text{ TeV} \times \sqrt{g_{s\mu}g_{b\mu}}$$

$b \rightarrow c$



$$M_\phi = 1 \text{ TeV} \times \sqrt{g_{b\nu}g_{c\tau}}$$

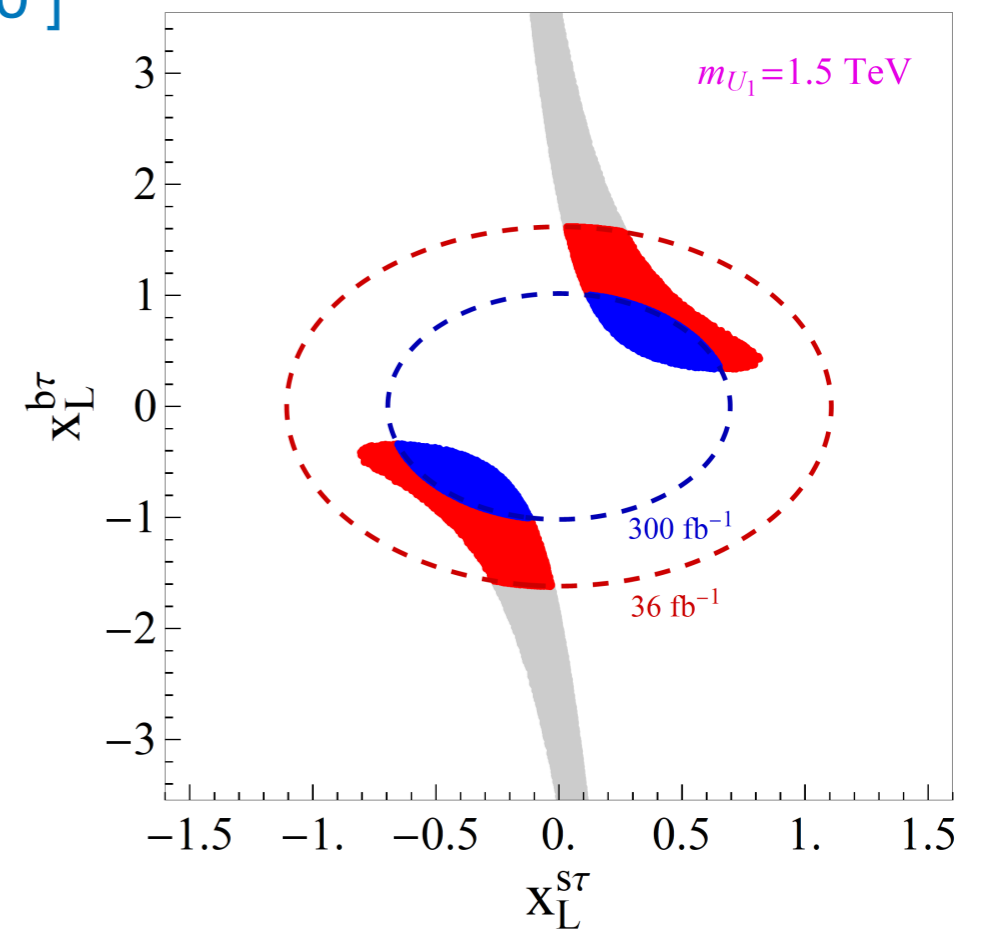
A combined explanation?

- What are the quantum numbers of a successful candidate

[MB, Neubert, 1511.01900]

Model	$R_{K^{(*)}}$	$R_{D^{(*)}}$	$R_{K^{(*)}} \& R_{D^{(*)}}$
S_1	\times^*	\checkmark	\times^*
R_2	\times^*	\checkmark	\times
\widetilde{R}_2	\times	\times	\times
S_3	\checkmark	\times	\times
U_1	\checkmark	\checkmark	\checkmark
U_3	\checkmark	\times	\times

$$U_1 = (\mathbf{3}, \mathbf{1})_{2/3}$$



[Angelescu et al, 1808.08179]

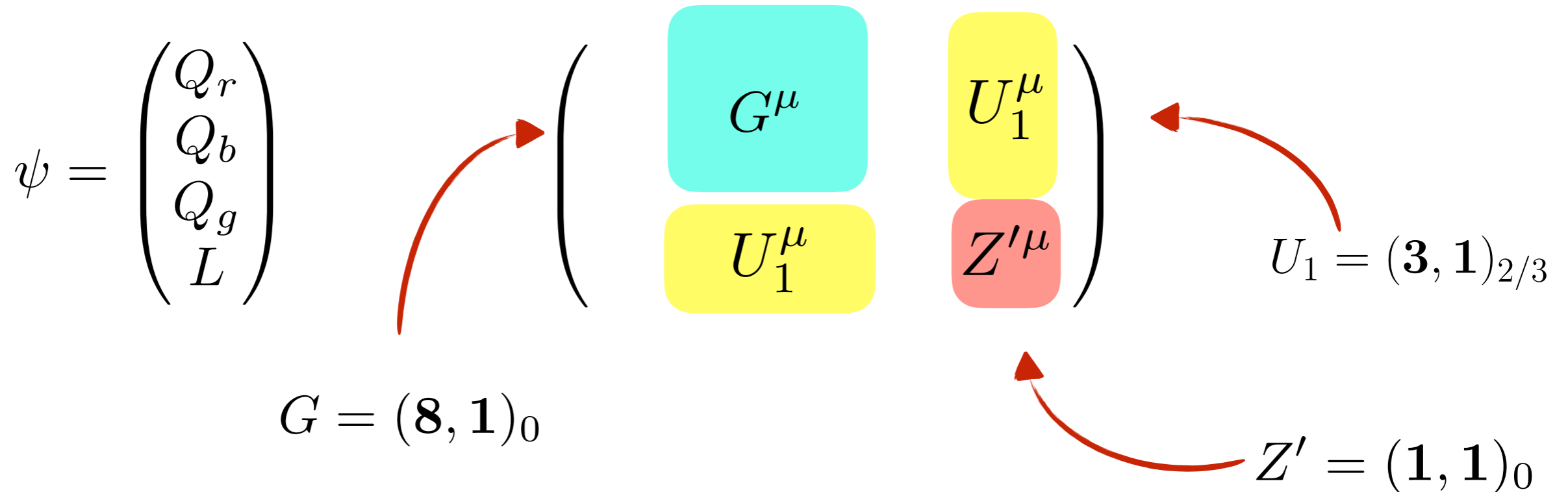
- A vector LQ at the TeV scale?

A combined explanation?

$U_1 = (\mathbf{3}, \mathbf{1})_{2/3}$ is the Pati-Salam Leptoquark ! [Pati, Salam, 1974]

Pati and Salam proposed to combine Lepton number and color in a single gauge group $SU(4)_C \times SU(2)_L \times SU(2)_R$

[Barbieri, Murphy, Senza 1611.04930]



Problematic because $K \rightarrow \mu e \rightarrow M \gtrsim 100 \text{ TeV}$

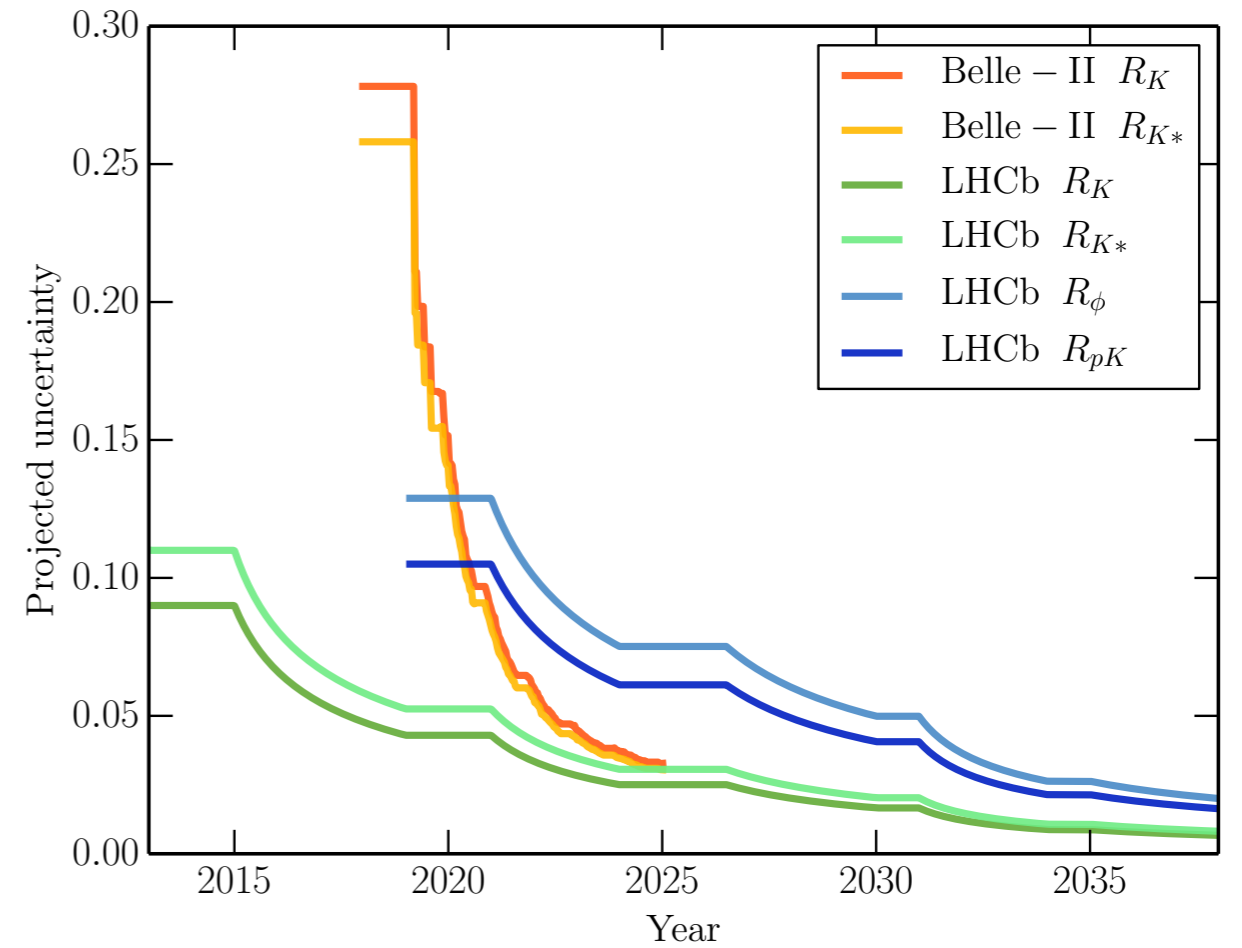
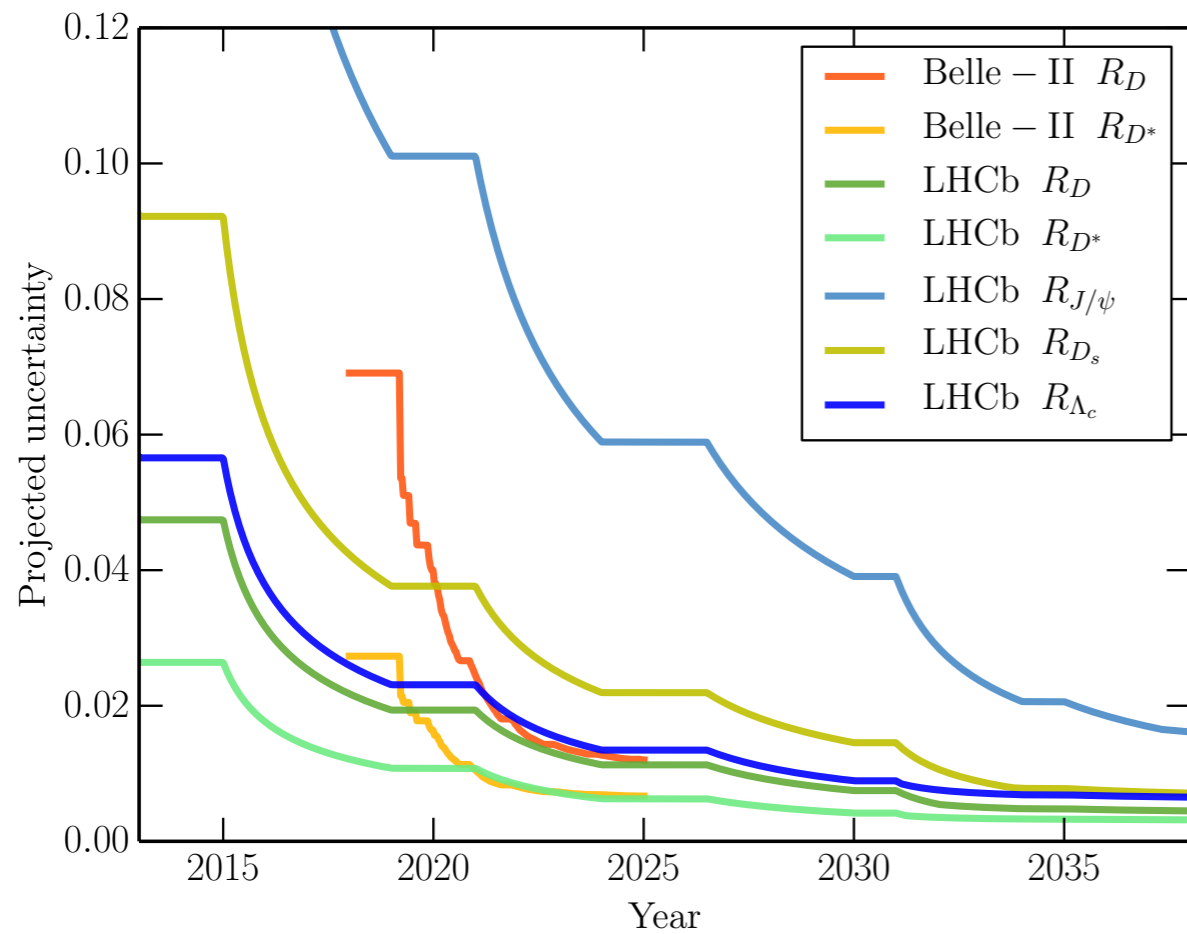
A combined explanation?

$U_1 = (\mathbf{3}, \mathbf{1})_{2/3}$ is the Pati-Salam Leptoquark ! [Pati, Salam, 1974]

Needs more work

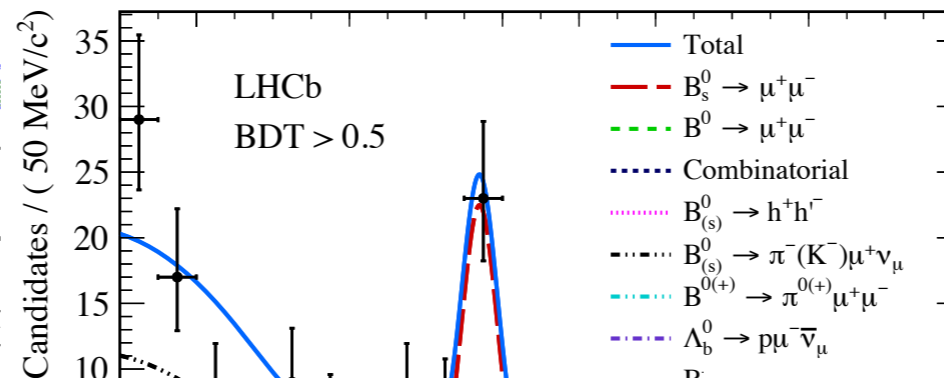
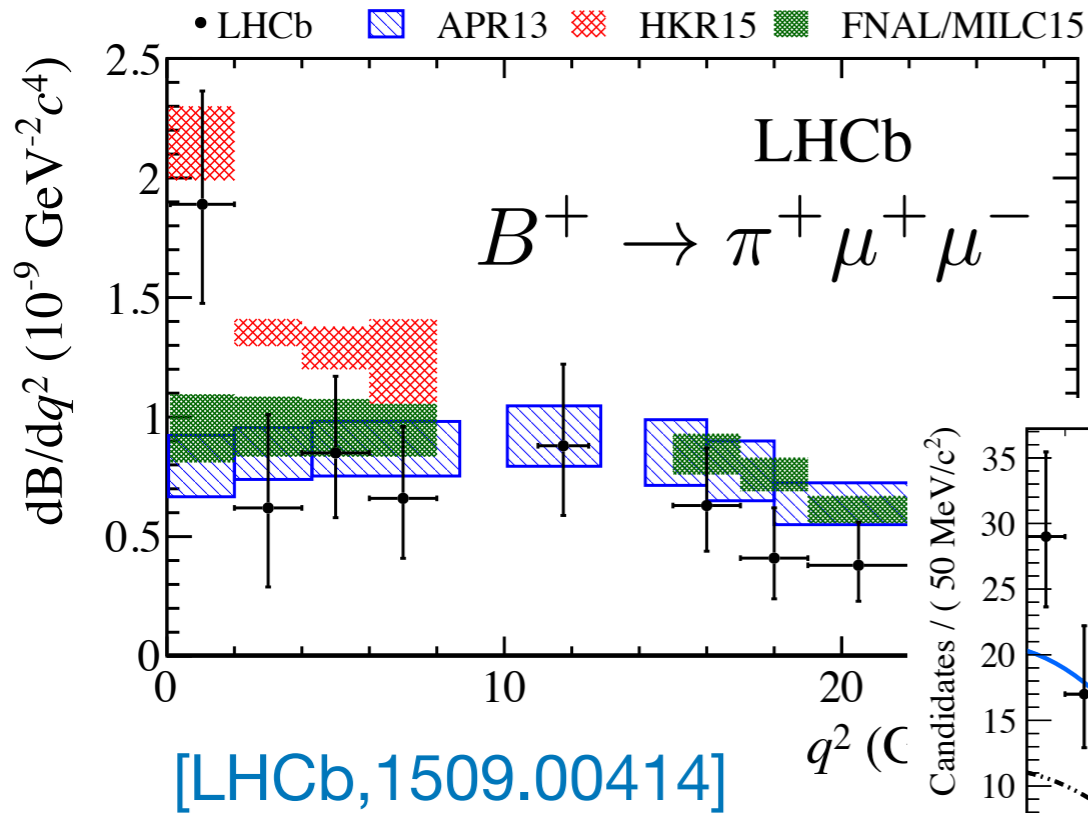
- $\left[SU(4)_C \times SU(2)_L \times SU(2)_R \right]^3$ [Bordone, Cornella, Fuentes-Martin, Isidori, 1712.01368]
- $SU(4)_C \times SU(3)' \times SU(2)_L \times U(1)'$ [Greljo, Stefanel 1802.04274]
- $SU(4)_C \times SU(2)_L \times SU(2)_R$ [Blanke, Crivellin 1801.07256]
in warped extra dimension

Future Prospects



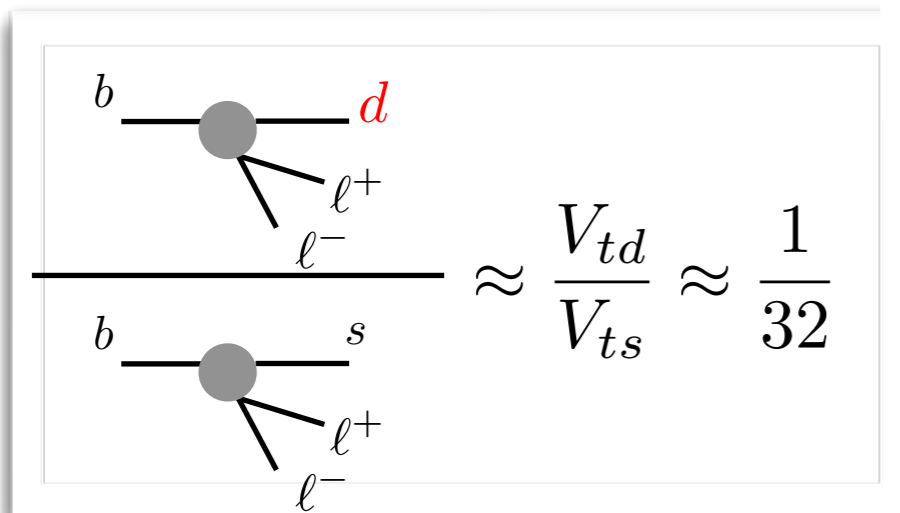
Future Prospects

Lepton Non-Universality in $b \rightarrow d$ transitions?

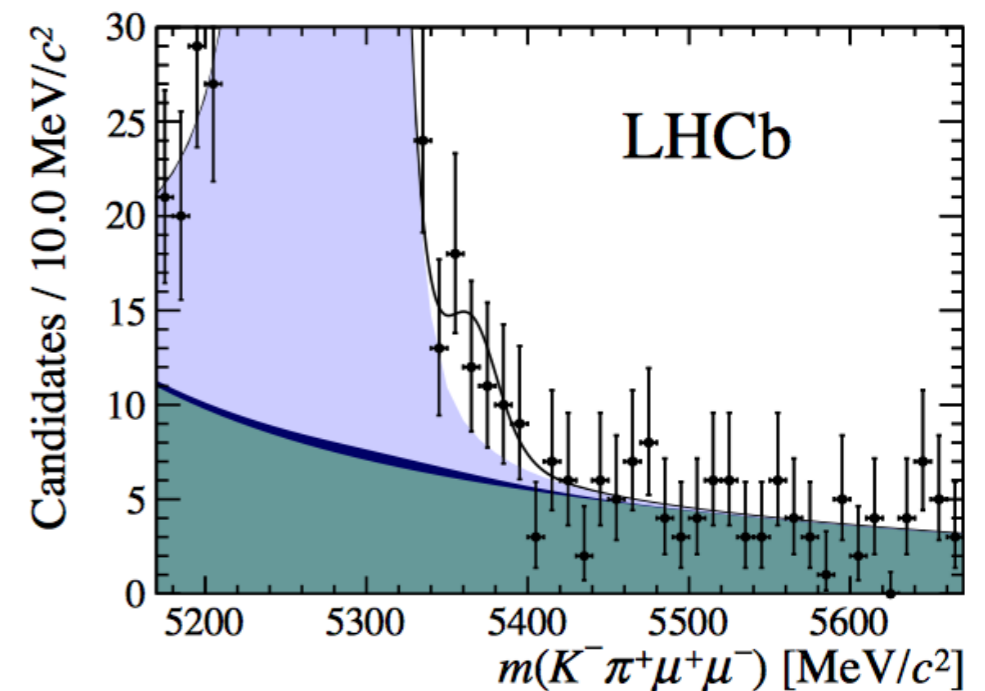


[LHCb, 1804.07167]

$$\mathcal{B}(B_s^0 \rightarrow \bar{K}^* \mu^+ \mu^-) =$$



[LHCb, 1703.05747]



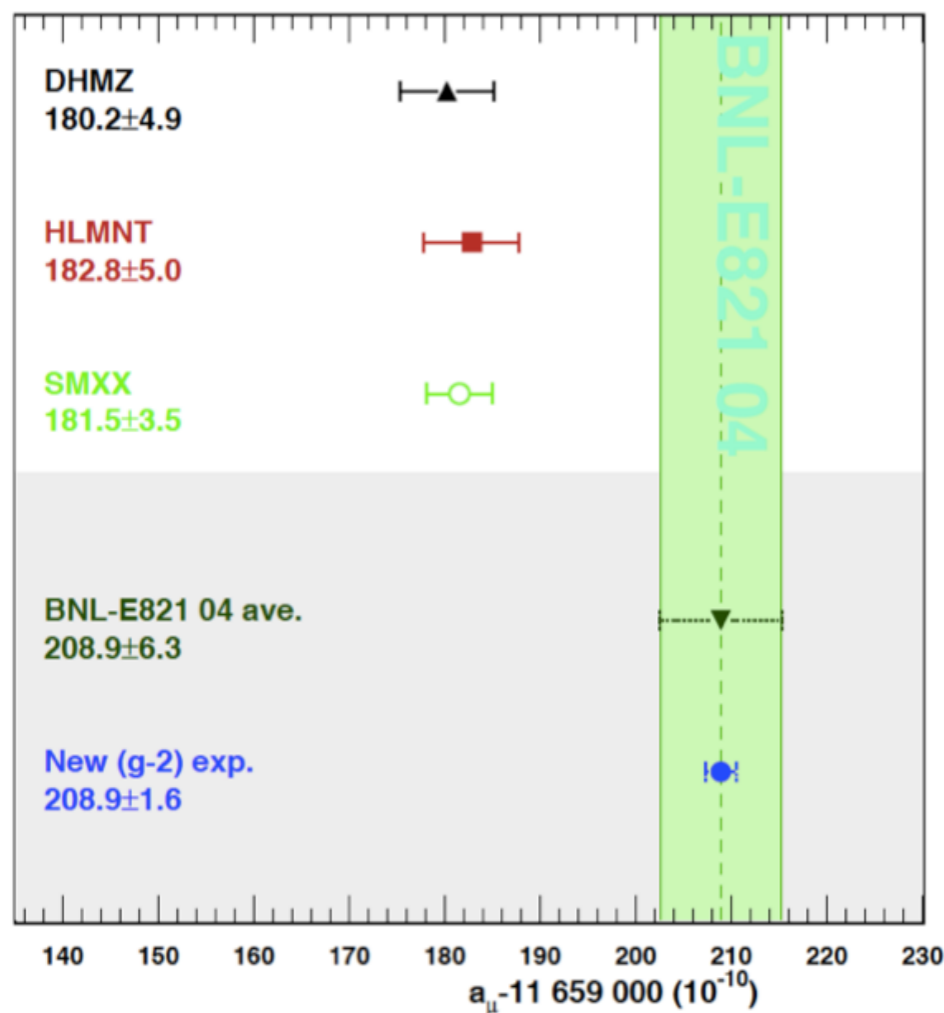
Lepton Flavour

Lepton Flavour $(g - 2)_\mu$

The anomalous magnetic moment of the muon

$$a_\mu = (g - 2)_\mu / 2$$

$$a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (288 \pm 63 \pm 49) \cdot 10^{-11}$$



Currently: 3.6σ discrepancy

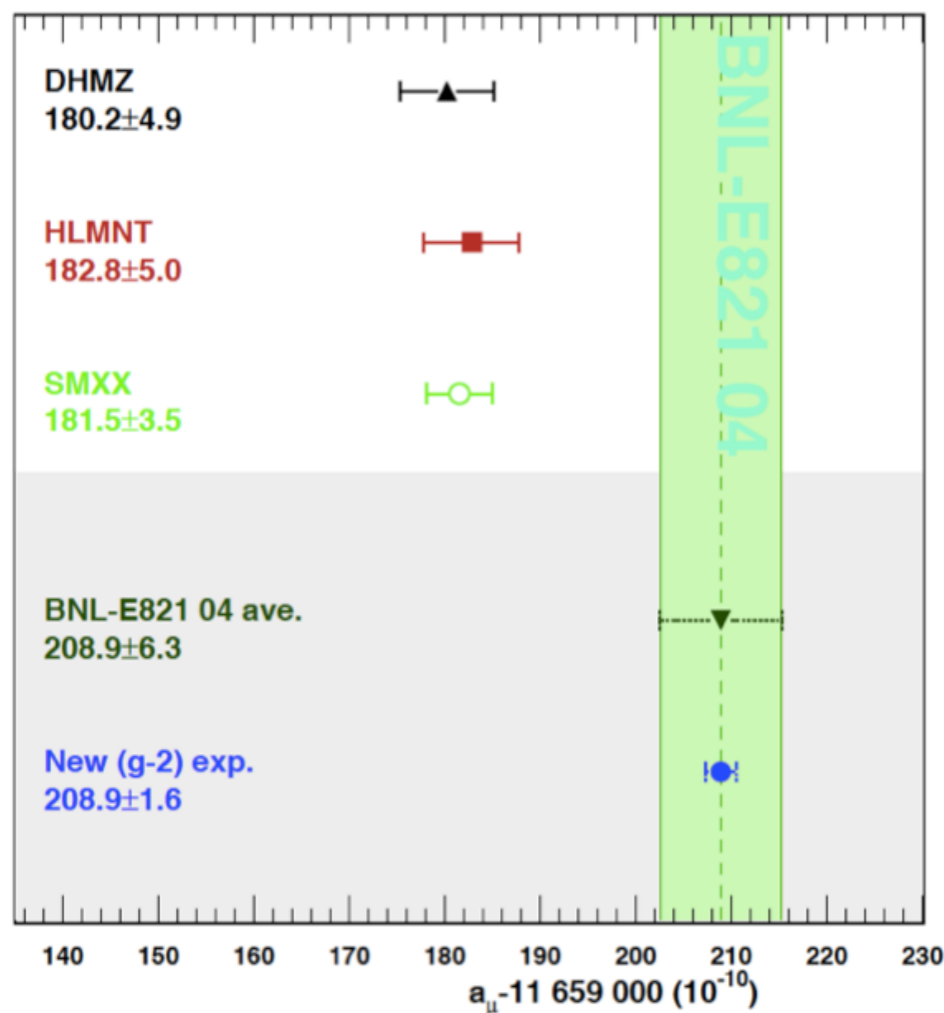
Future: $\gtrsim 5 \sigma$?

Lepton Flavour $(g - 2)_\mu$

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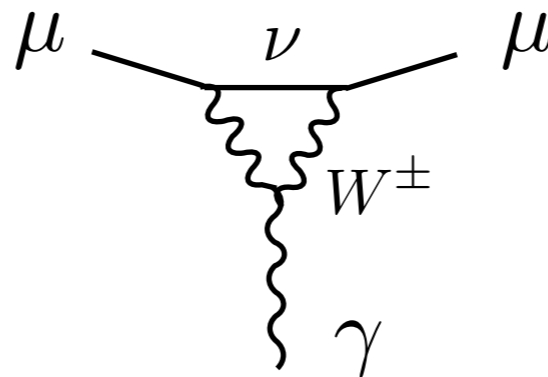


Currently: 3.6σ discrepancy

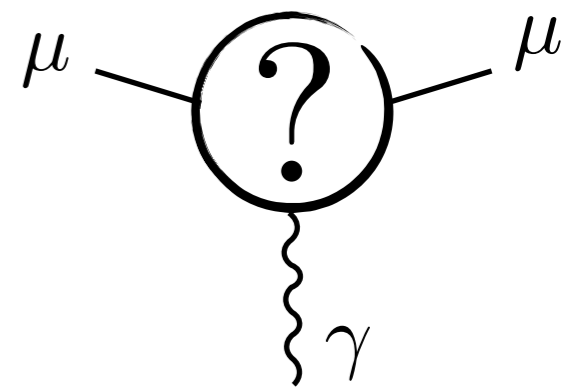
Future: $\gtrsim 5 \sigma$?

SM

$$\delta a_\mu^W \approx \frac{g^2}{20\pi^2} \frac{m_\mu^2}{M_W^2} \approx 400 \times 10^{-11}$$

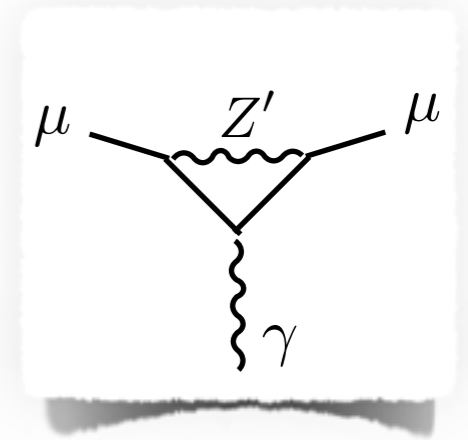
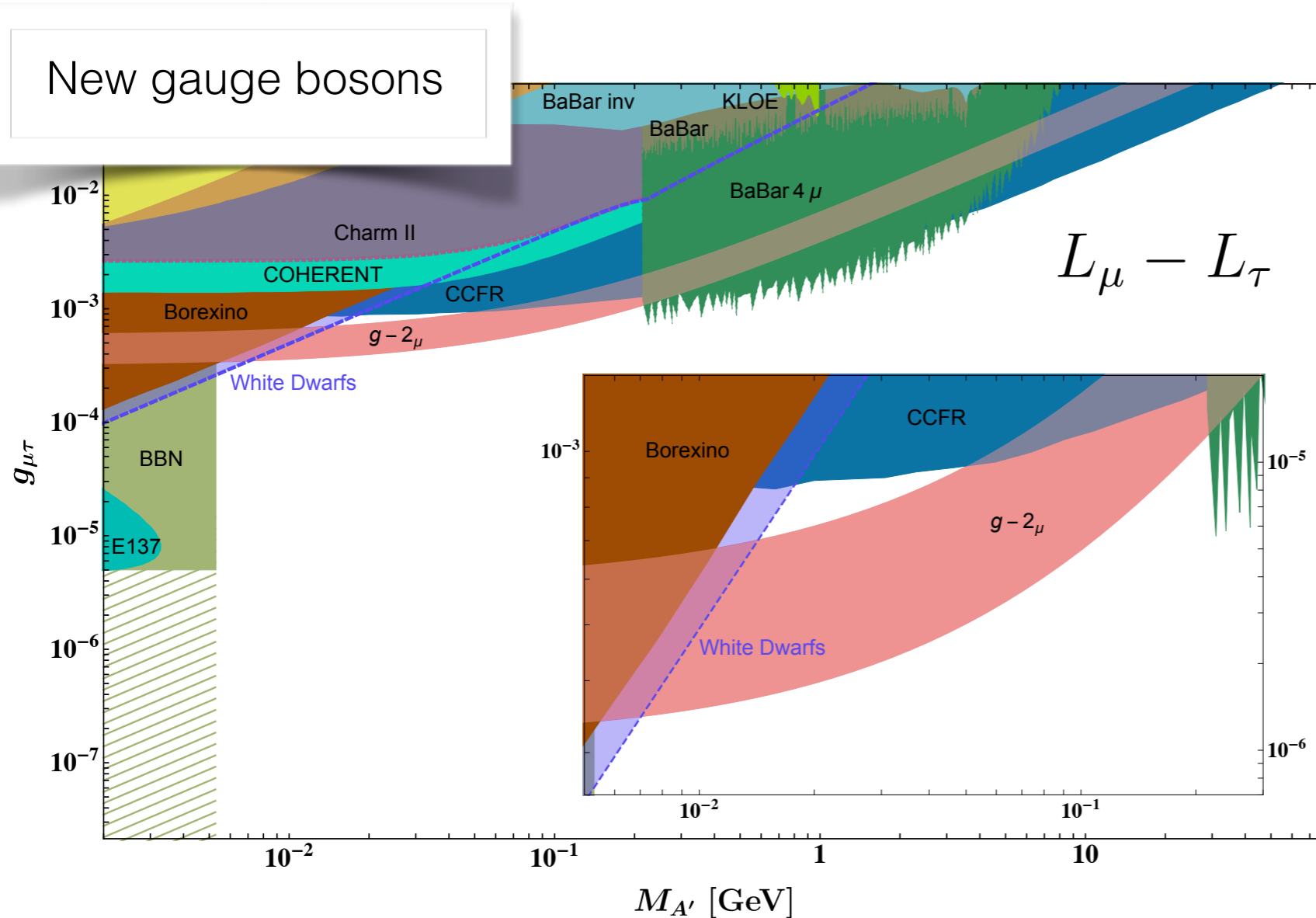


NP



$$M \approx 1 - 10 \text{ TeV}$$

New Physics ?



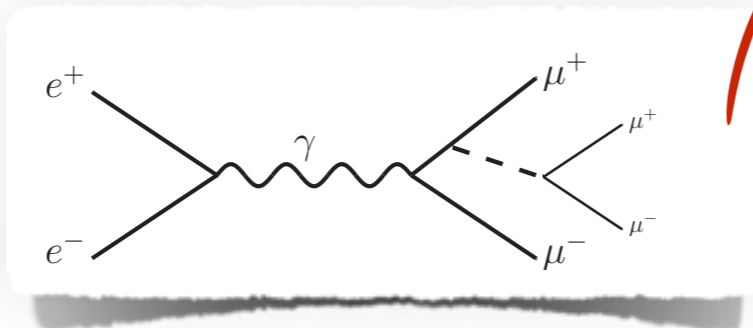
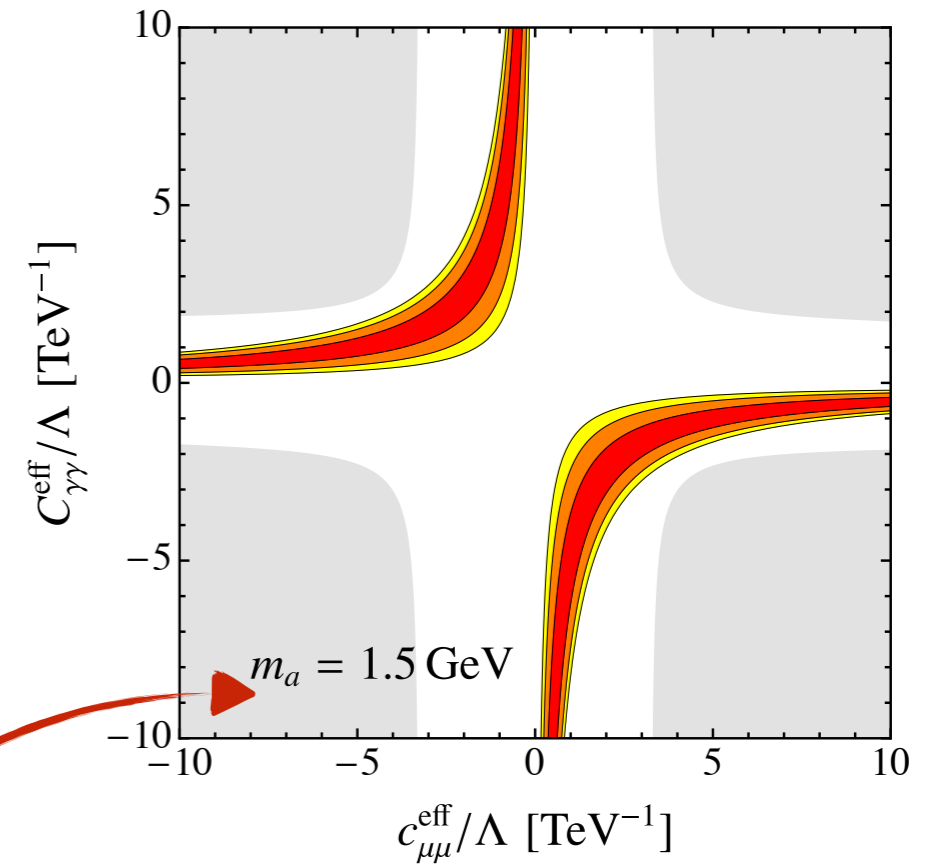
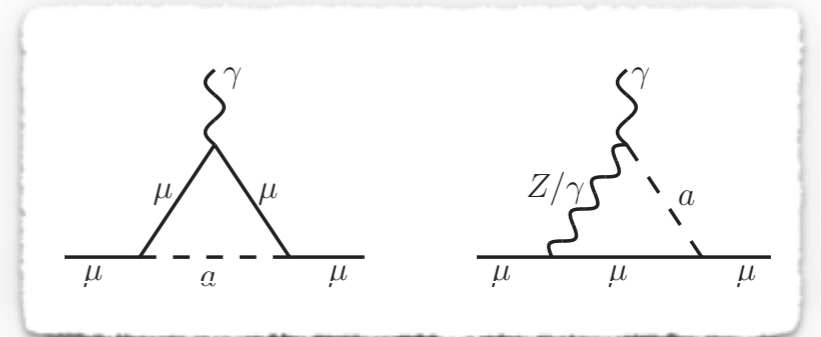
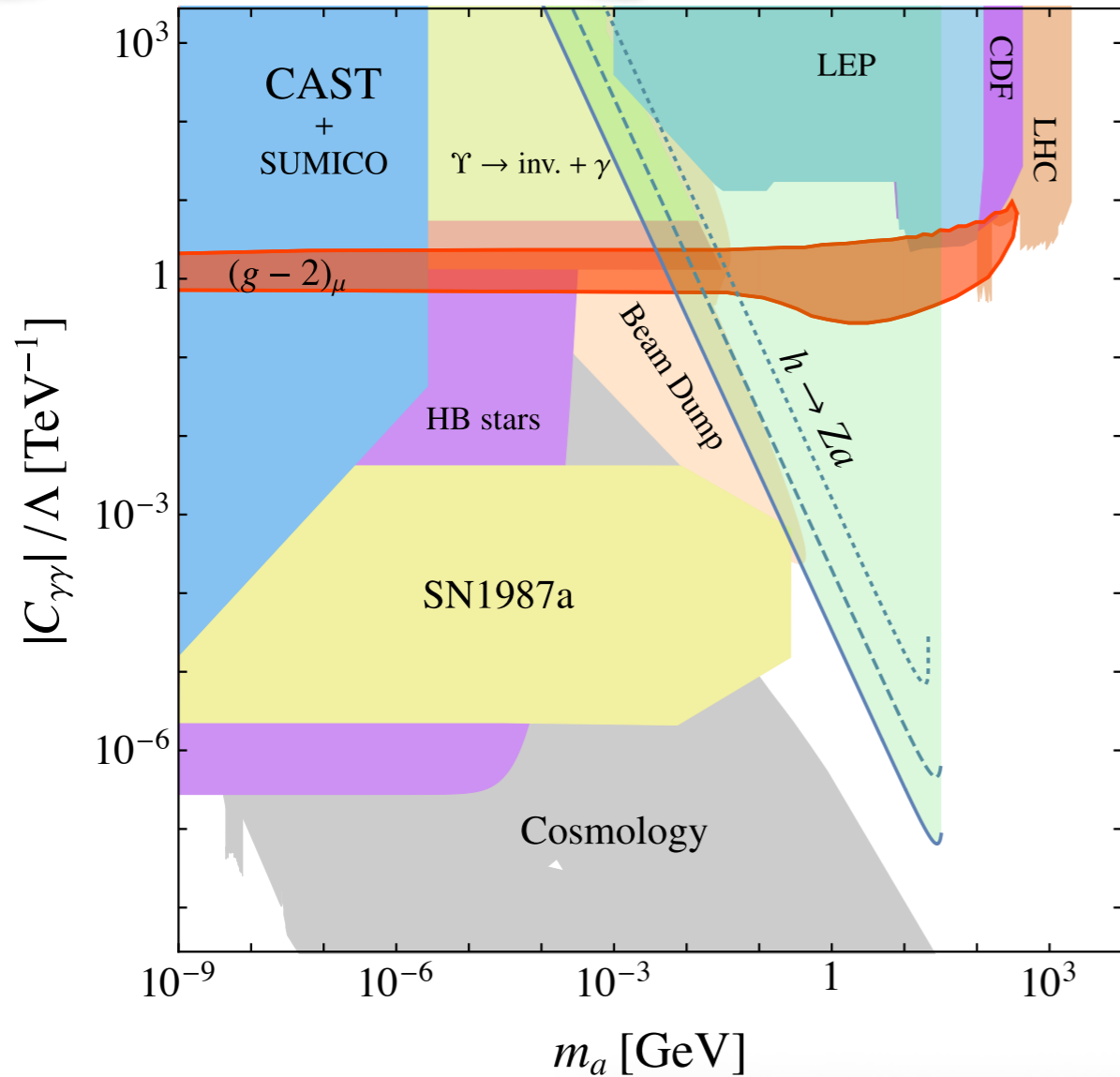
This gauge group is special, because it is anomaly-free and predicts no FCNCs at tree-level.

Because mass matrices are diagonal already!

$$\mathcal{L}_{Z'} = \bar{\ell} g' \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix} \gamma^\mu Z'_\mu \ell + \begin{pmatrix} m_e & 0 & 0 \\ 0 & m_\mu & 0 \\ 0 & 0 & m_\tau \end{pmatrix} \bar{\ell} \ell$$

New Physics ?

An axion-like particle



[Marciano et al., PRD 94 (2016) 115033]

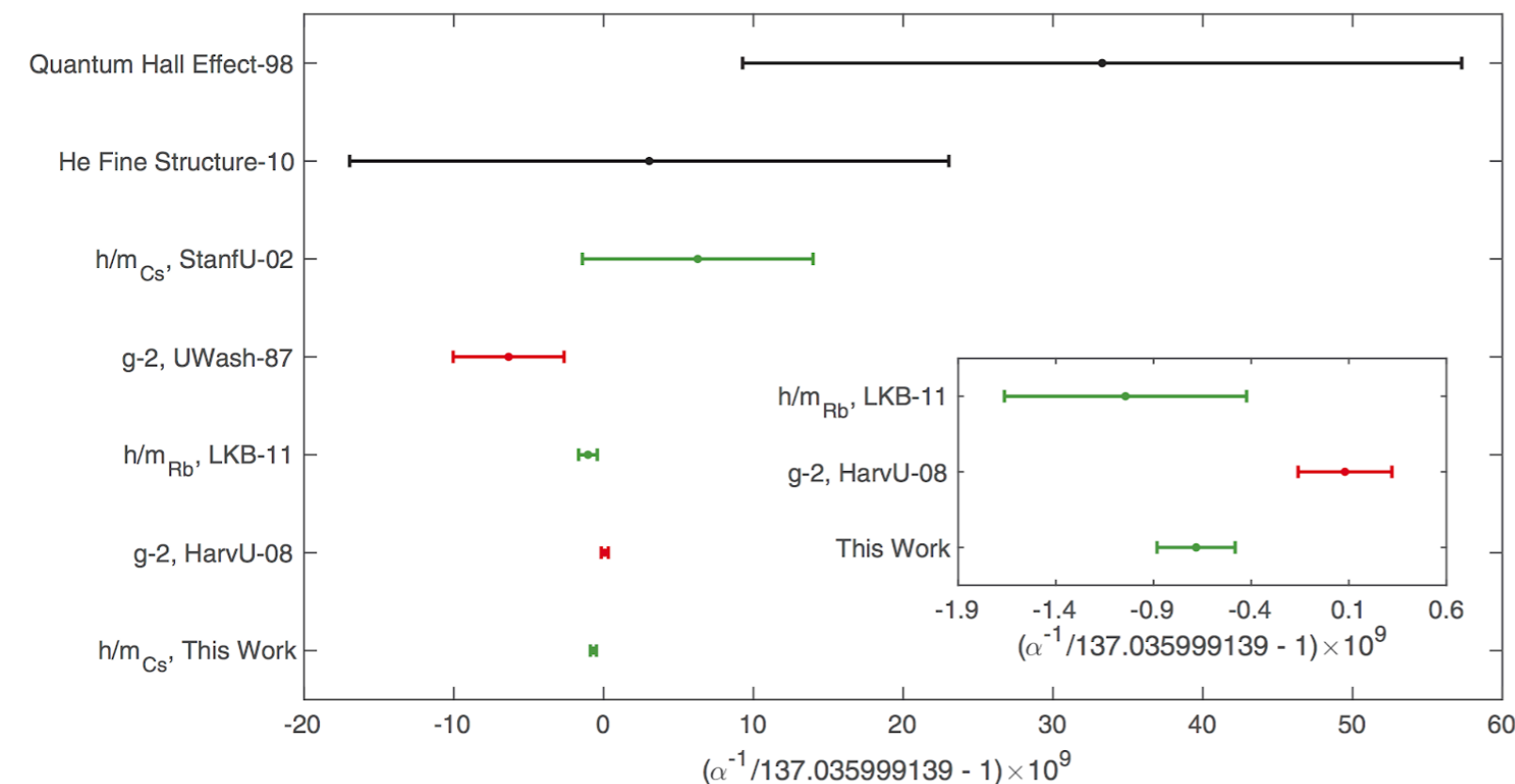
[MB, Neubert, Thamm 1704.08207]

Lepton Flavour $(g - 2)_e$

The anomalous magnetic moment of the electron

$$\alpha^{-1}(\text{Cs}) = 137.035999046(27) \quad \Delta a_e = (-87 \pm 36) \times 10^{-14}$$

deviates from the SM prediction by 2.5σ



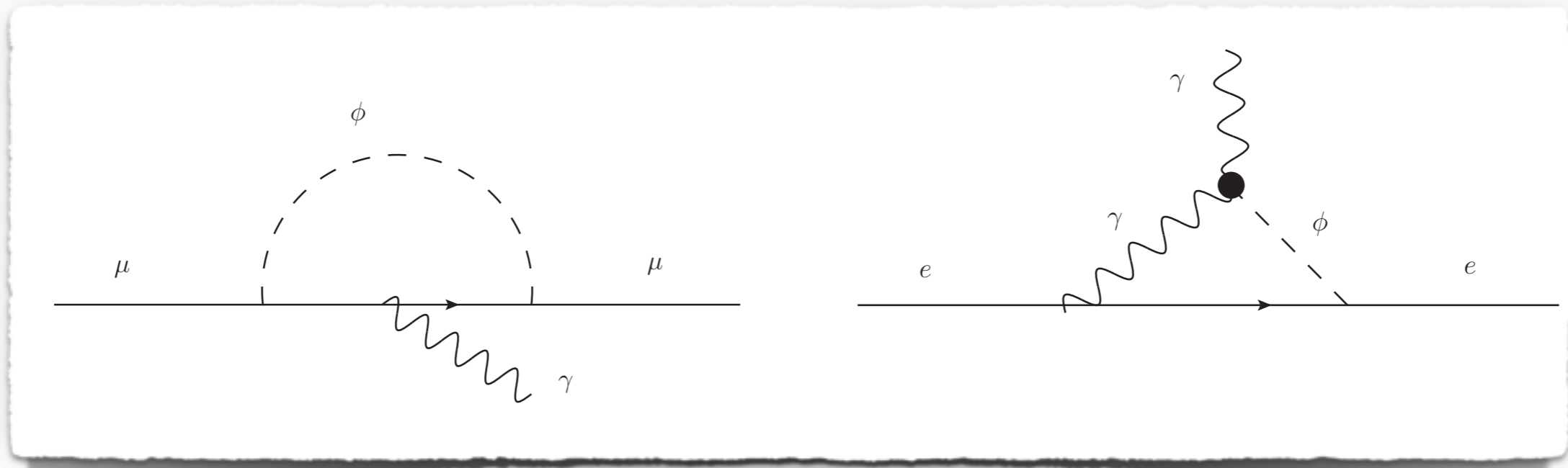
...with the opposite sign.

Taking both seriously excludes an explanation by gauge bosons.

[Parker 1812.04130]

A combined explanation?

$$\mathcal{L}_\phi = -\frac{1}{2}m_\phi^2\phi^2 - \sum_f \lambda_f \phi \bar{f}f - \frac{\kappa_\gamma}{4} \phi F_{\mu\nu}F^{\mu\nu}.$$



New scalar with ~ 100 MeV mass and couplings to muons and electrons of order 10^{-3} to 10^{-4} . Coupling to photons loop-induced.

The future of Lepton flavour is golden

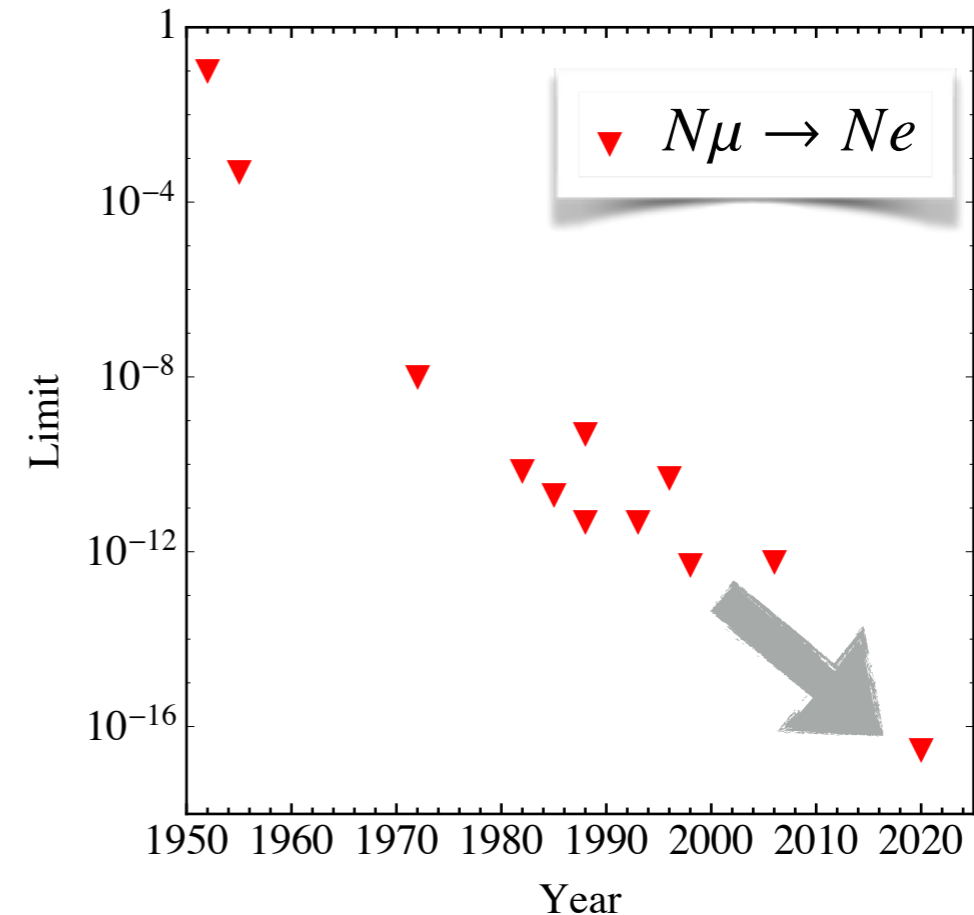
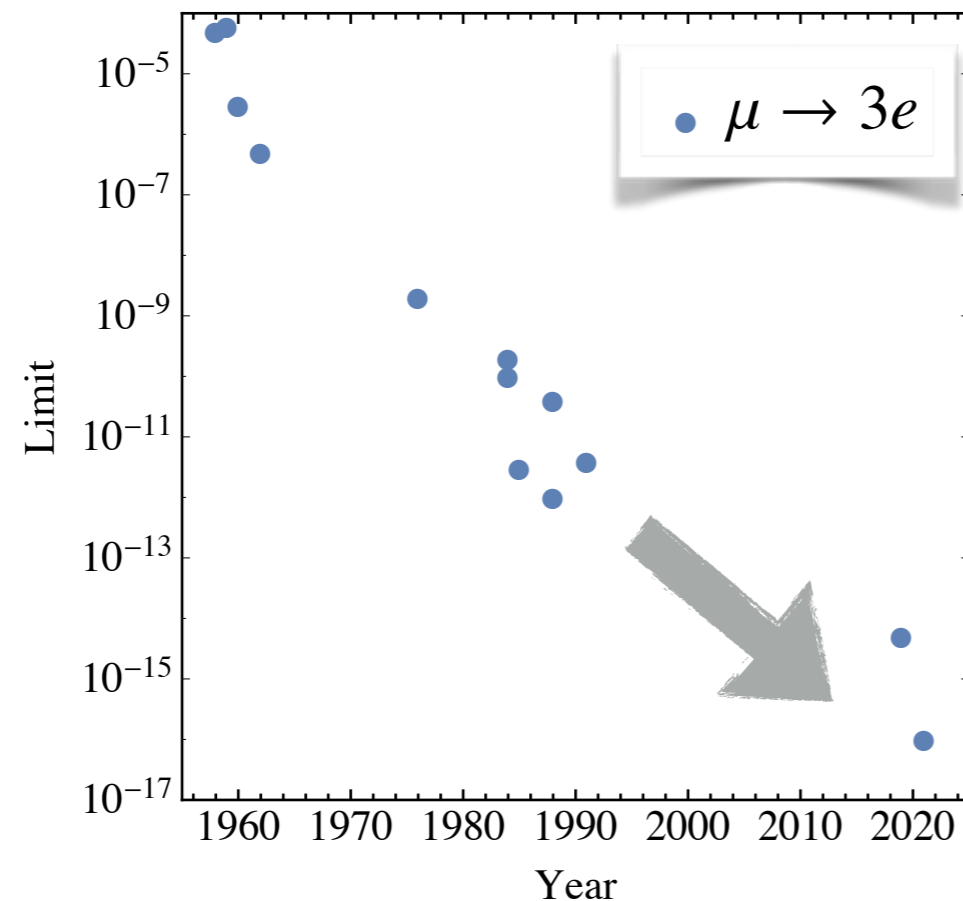
In the next years we will enter a new golden age for high precision lepton experiments

- Electron EDM $d_e \lesssim 10^{-27}$ e cm \longrightarrow $d_e \lesssim 10^{-29} - 10^{-31}$ e cm
- Muon g-2 $\delta a_\mu = 7.2 \times 10^{-9}$ \longrightarrow $\delta a_\mu = 1.4 \times 10^{-9}$
- $\mu \rightarrow e\gamma$ $BR(\mu \rightarrow e\gamma) < 4.2 \times 10^{-13}$ \longrightarrow $BR(\mu \rightarrow e\gamma) < 5 \times 10^{-14}$
- $N\mu \rightarrow Ne$ $BR(N\mu \rightarrow Ne) < 6 \times 10^{-13}$ \longrightarrow $BR(N\mu \rightarrow Ne) < 3 \times 10^{-17}$
- $\mu \rightarrow eee$ $BR(\mu \rightarrow eee) < 4 \times 10^{-12}$ \longrightarrow $BR(\mu \rightarrow eee) < 1 \times 10^{-16}$

and plans for more...

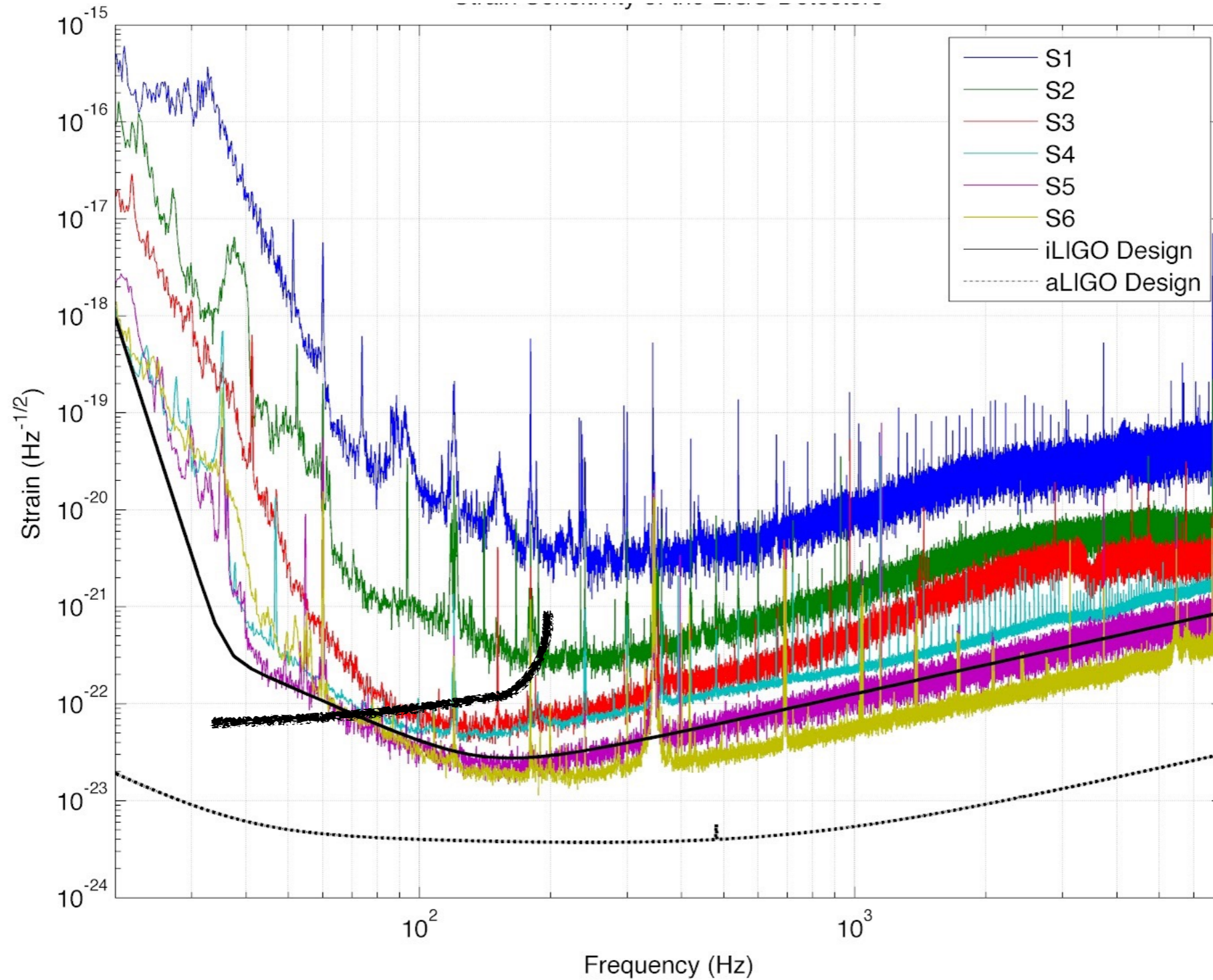
The future of Lepton flavour is golden

This is an improvement hardly found in modern physics...



...these experiments will allow us to look at the muon with a resolution $\sim 10\,000$ times better than ever before.

The future of Lepton flavour is golden



Conclusions

Several anomalies in flavour physics continue to question the validity of the SM.

Some point to scales expected from generic flavour structures! Some point to surprisingly low scales.

But future data will improve uncertainties by ~ 1 order of magnitude and increase sensitivity in lepton observables by up to 4 orders of magnitude.

We are designing the first probes of the multi-PeV scale.

Executive summary

$b \rightarrow s$ transitions: Clean LFV observables agree with dirty angular observables. The low-mass bin in R_{K^*} does not look like NP. NP: leptoquark (30 TeV)

$b \rightarrow c$ transitions: Large deviation in a charged current process. In question by LEP(?). NP: leptoquark (1 TeV)

Combined explanations need gauge-unification at the TeV scale.

g-2: Both muon and electron in tension with the SM, but opposite direction.
NP: axion ($< \text{GeV}$) or hidden photon (for the muon).



Backup



A pattern in $b \rightarrow s$ transitions

Simple example: A single resonance

$$\Pi(q^2) = \frac{f^2}{q^2 - M^2 + iM\Gamma}$$

$$\text{Im } \Pi(q^2) = \frac{f^2 M\Gamma}{(q^2 - M^2)^2 + M^2\Gamma^2}$$

$$\Gamma \rightarrow 0$$

$$\approx \pi f^2 \delta(q^2 - M^2)$$

$$\int_0^{m^2} dq^2 \text{Im } \Pi(q^2) \approx \pi f^2 \ll m^2$$

small compared to the non-res contribution. Duality holds!

$$|\Pi(q^2)|^2 = \frac{f^4}{(q^2 - M^2)^2 + M^2\Gamma^2}$$

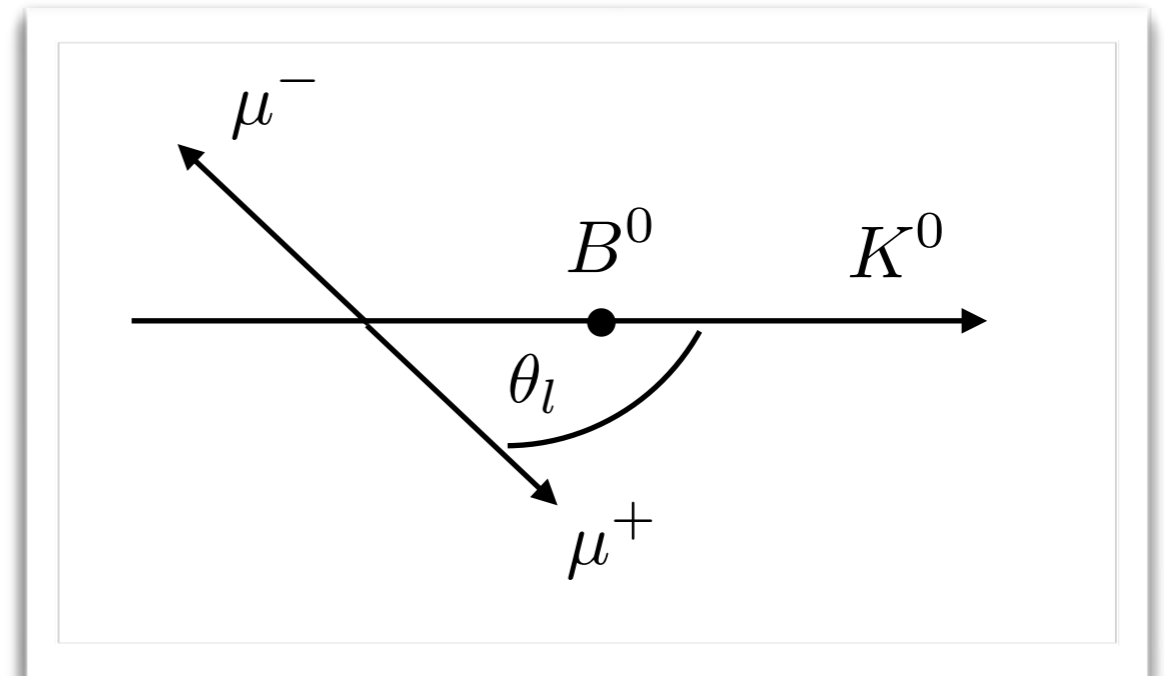
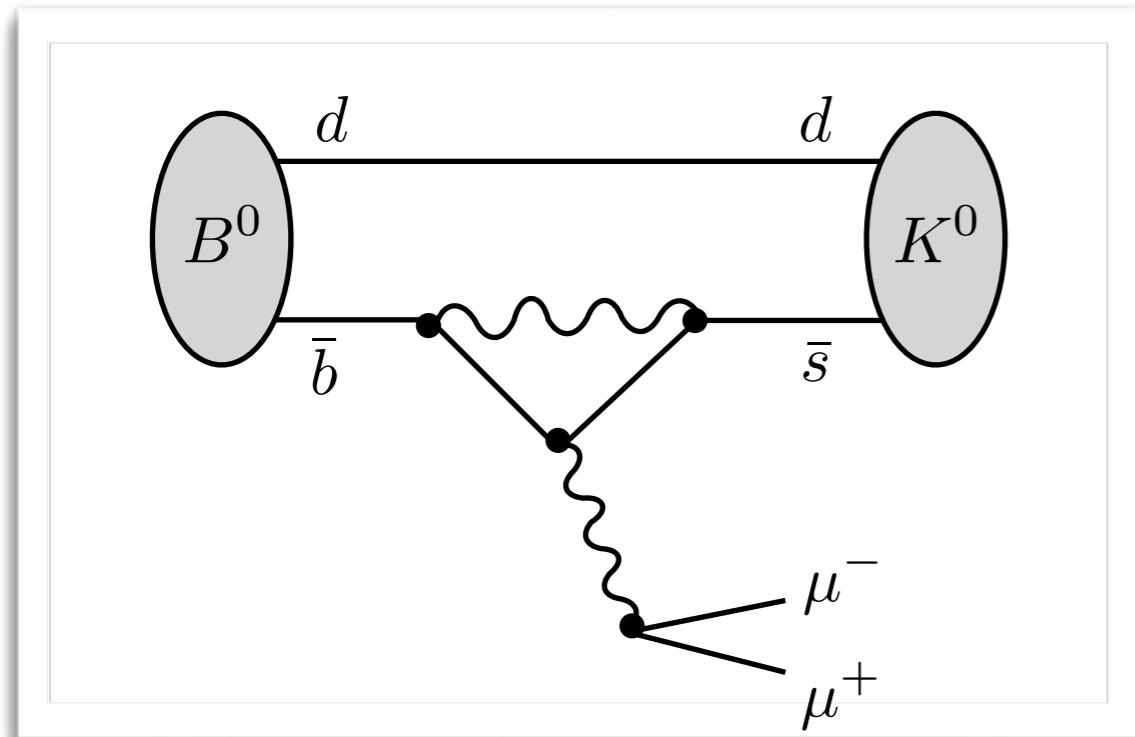
$$= \frac{f^2}{M\Gamma} \text{Im } \Pi(q^2)$$

$$\approx \frac{\pi f^4}{M\Gamma} \delta(q^2 - M^2)$$

$$\int_0^{m^2} dq^2 |\Pi(q^2)|^2 \approx \frac{\pi f^4}{M\Gamma}$$

singular!

A pattern in $b \rightarrow s$ transitions



$$\frac{1}{\Gamma} \frac{d\Gamma}{d \cos \theta_l} = \frac{3}{4} (1 - F_H) (1 - \cos^2 \theta_l) + \frac{1}{2} F_H + A_{FB} \cos \theta_l$$

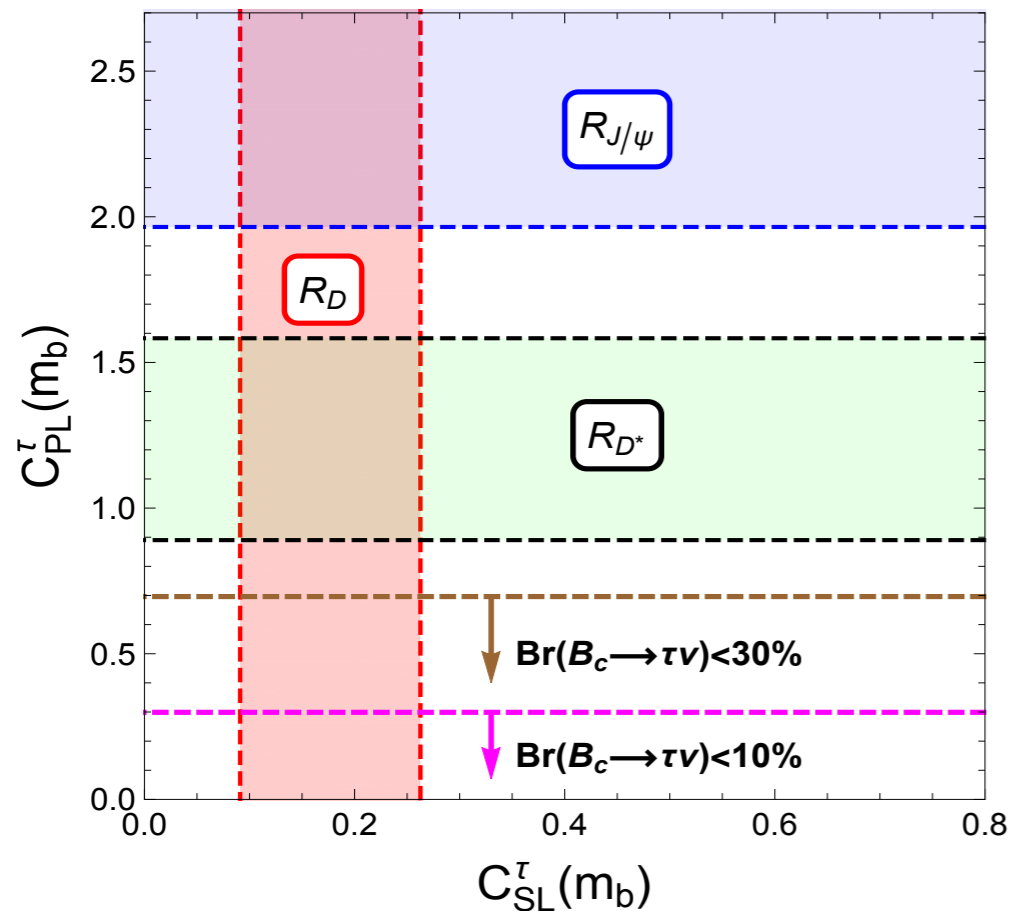
$$\frac{d\Gamma^{\text{SM}}}{d \cos \theta_l} \propto \sin^2 \theta_l + \mathcal{O}(m_l^2)$$

Helicity suppressed
 $\propto m_l^2$

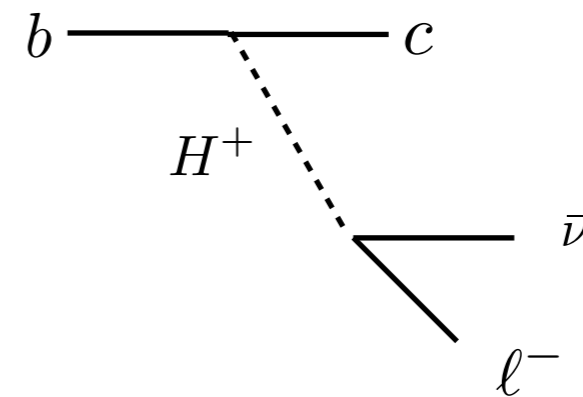
Lepton Non-Universality in $b \rightarrow c$

A new TeV-scale scalar?

In tension with $\text{Br}(B_c \rightarrow \tau \nu)$ [Akeroyd, Chen, 1708.04072]



Hard to get two sizable coefficients

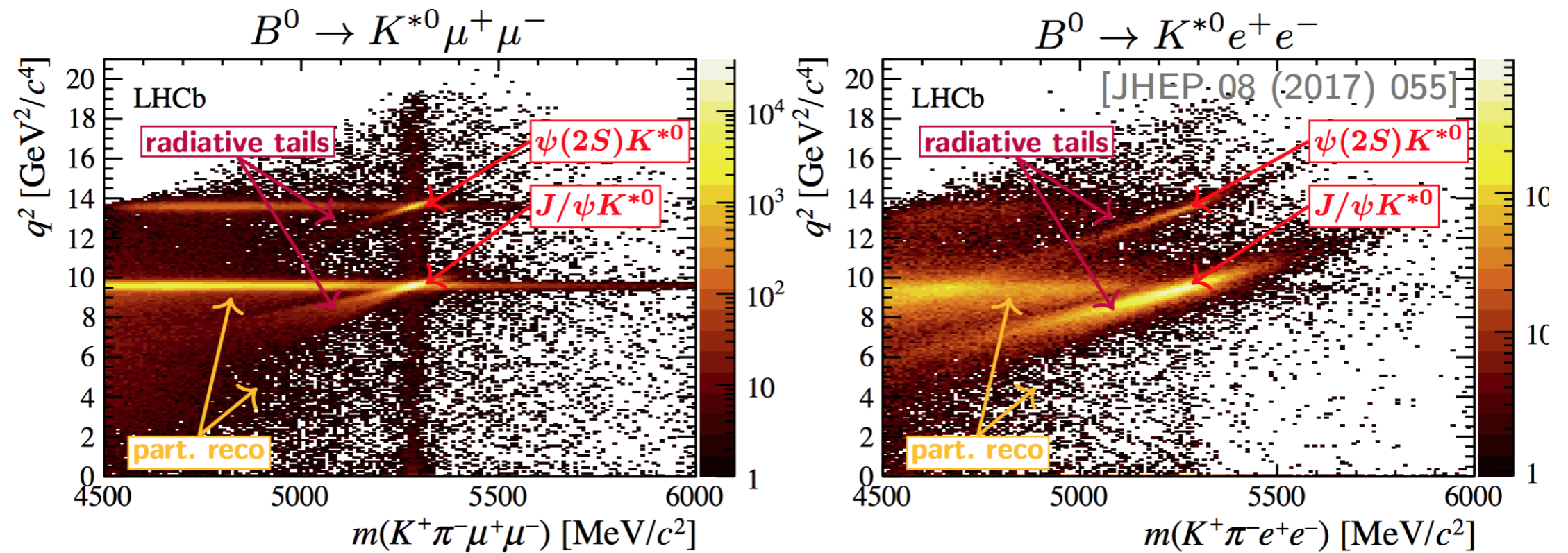


$$C_{SR} = \frac{-2\sqrt{2}G_F}{M_{H^+}^2} V_{cb} m_b m_\tau \tan \beta^2$$

$$C_{SL} = \frac{-2\sqrt{2}G_F}{M_{H^+}^2} V_{cb} m_c m_\tau \frac{1}{\tan \beta^2}$$

Experimental challenge

[LHCb, JHEP 08 (2017) 055]



Models for bs transitions

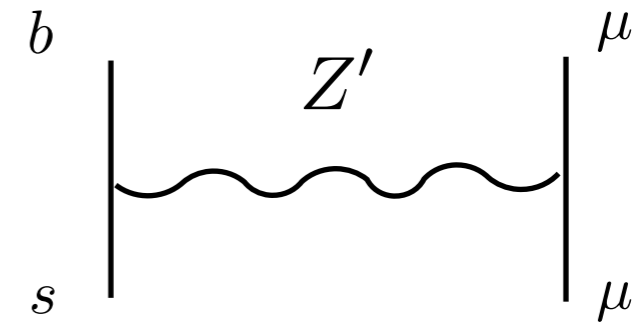
$\mu \neq e$

C_9 : Vector Currents

Gauld, Goetz, Haisch, 1310.1082

Altmannshofer, Gori, Pospelov, Yavin, 1403.1269

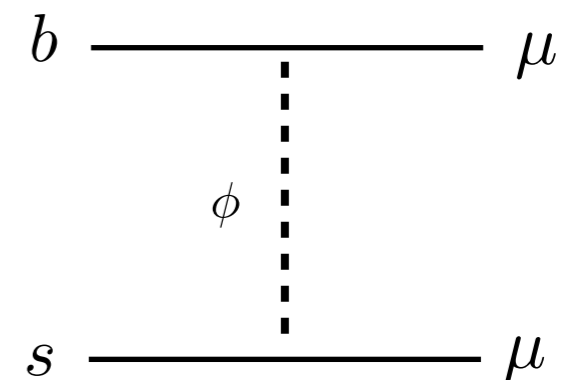
Crivellin, D'Ambrosio, Heeck 1501.00993 many more!



$C_9 = -C_{10}$: Leptoquarks

$(3, 3)_{-1/3} (3, 2)_{1/6}$ Hiller, Schmaltz 1408.1627
Becirevic et al. 1608.08501

$(3, 3)_{2/3}$ Fajfer, Kosnik 1511.06024

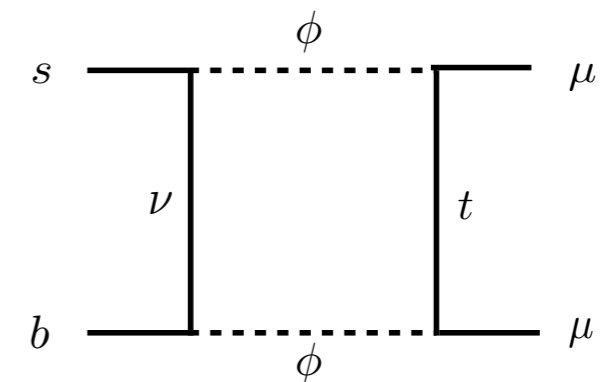


$C_9, C_9 = -C_{10}$: Loop Induced

Gripaios, Nardecchia, Renner 1509.05020

Arnan, Crivellin et al. 1608.07832

MB, Neubert 1511.01900



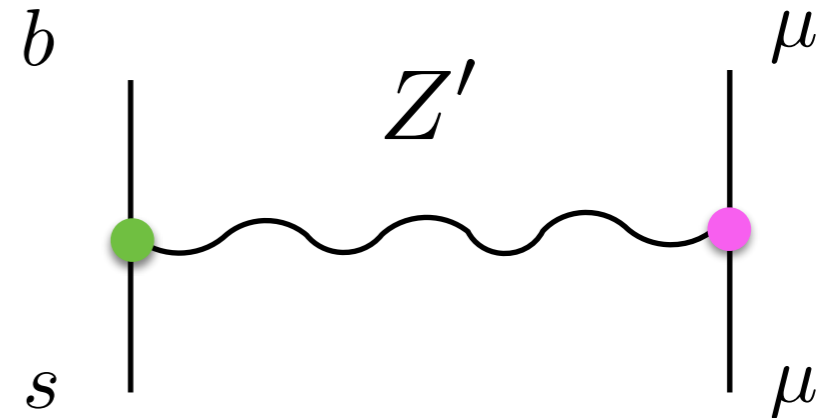
Models for bs transitions

$$\mu \neq e$$

C_9 : Vector Currents

Altmannshofer, Gori, Pospelov, Yavin, 1403.1269

- LFV diagonal couplings
- QFV off-diagonal couplings



Models for bs transitions

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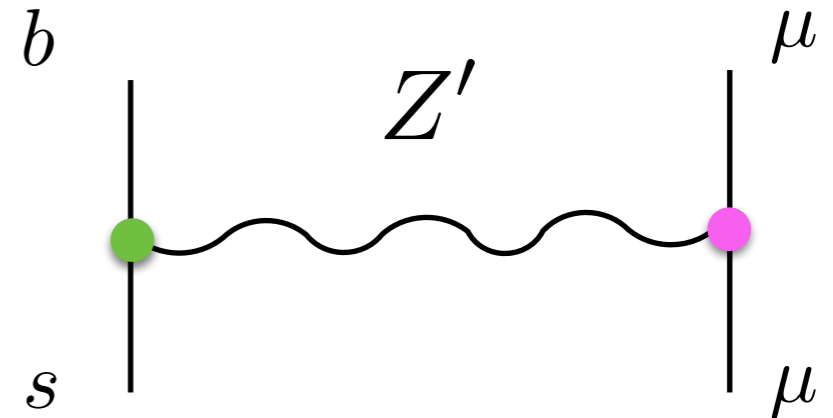
Altmannshofer, Gori, Pospelov, Yavin, 1403.1269

- LFV diagonal couplings

Beautiful solution: gauged $L_\mu - L_\tau$ symmetry!

Anomaly free gauge group. No need for new fermions :)

- QFV off-diagonal couplings

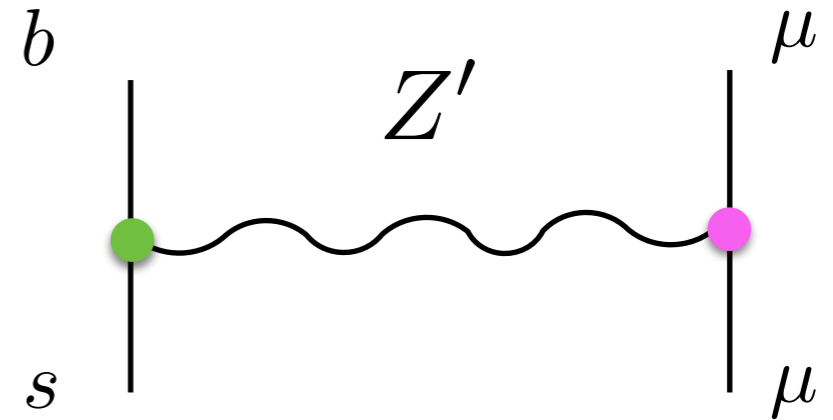


Models for bs transitions

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Altmannshofer, Gori, Pospelov, Yavin, 1403.1269



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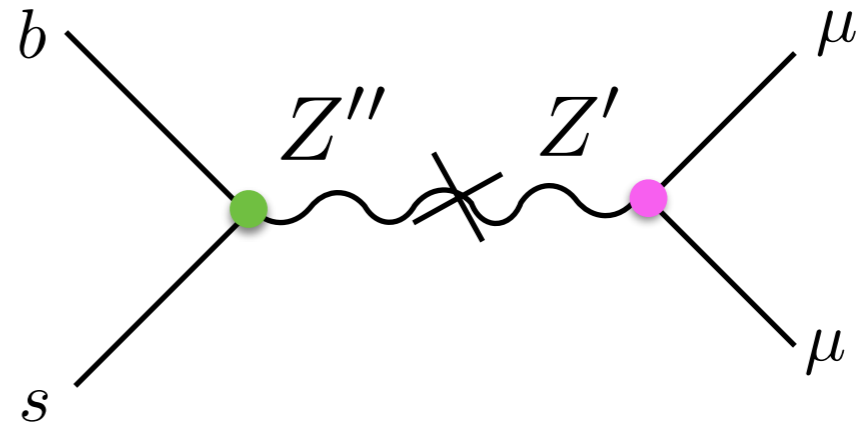
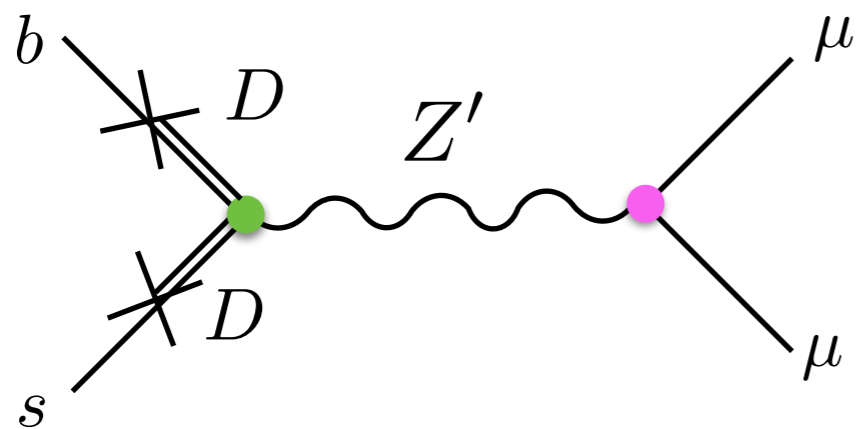
Charging b and s -> anomalies. Needs new fermions :/

Models for bs transitions

$\mu \neq e$

C_9 : Vector Currents

Altmannshofer, Gori, Pospelov, Yavin, 1403.1269



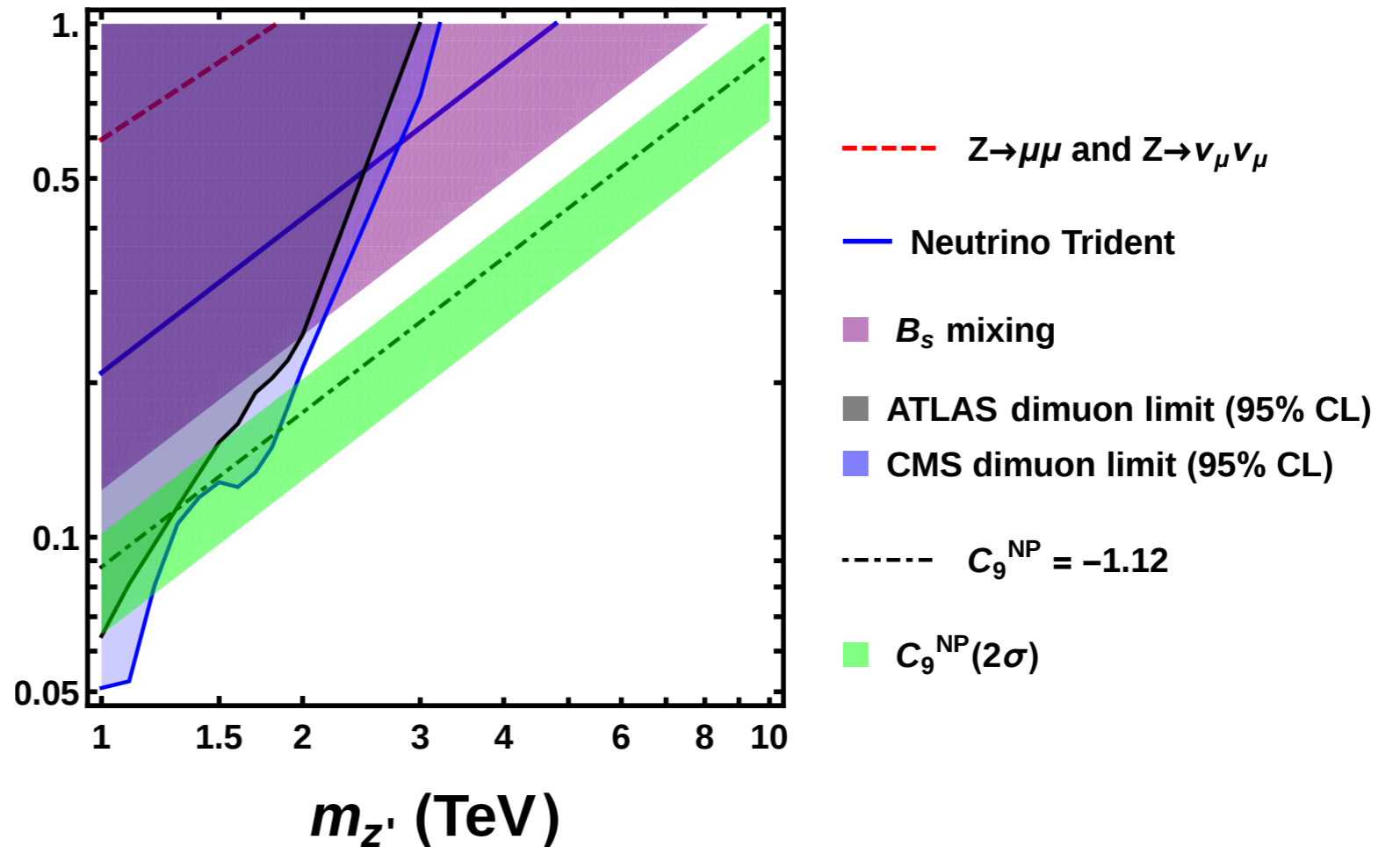
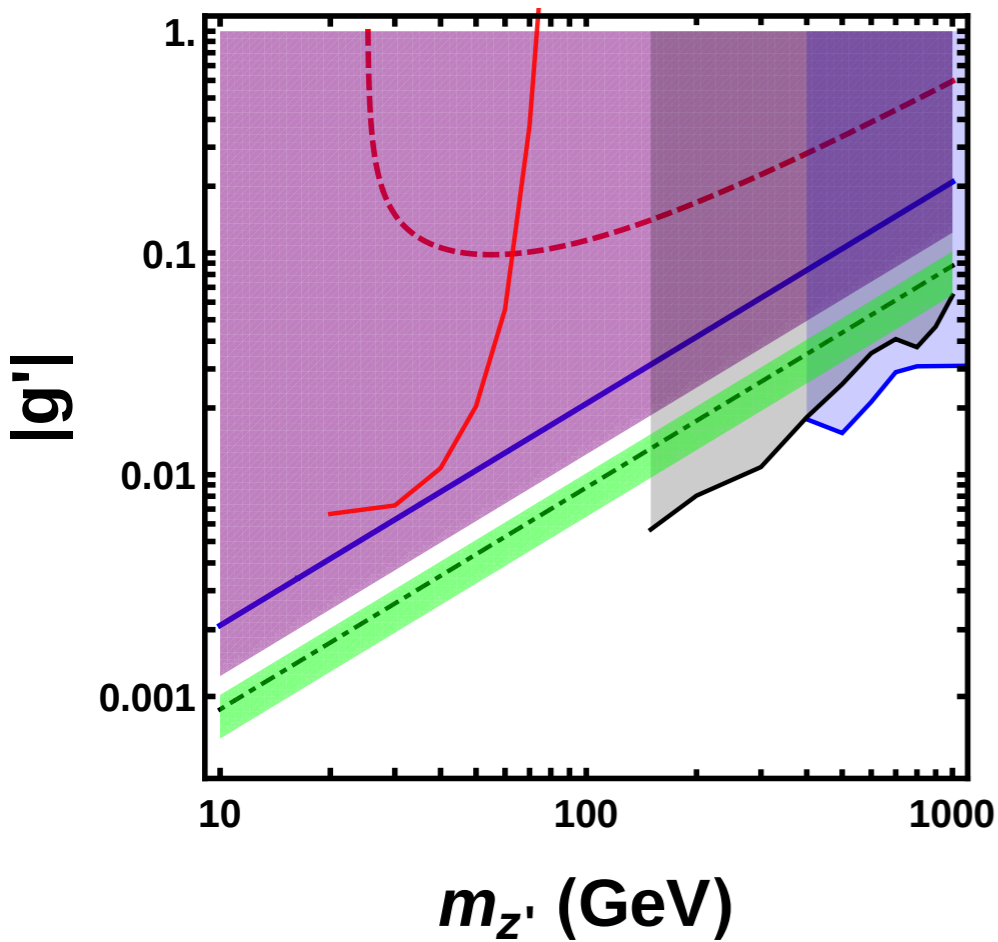
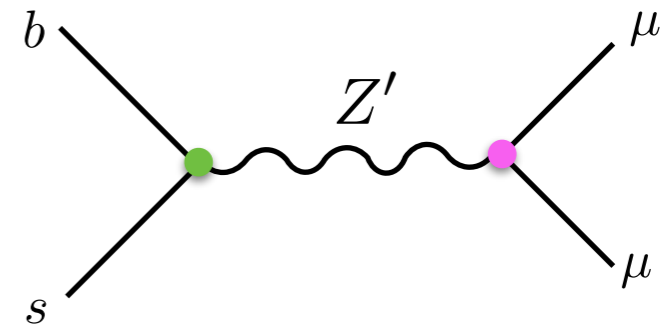
Horizontal Charges

Crivellin, D'Ambrosio, Heeck 1503.03477
Bonilla et al. 1705.00915

Models for bs transitions

$\mu \neq e$

Anomaly free group: $U(1)_{B_3-3L_3}$



Models for bs transitions

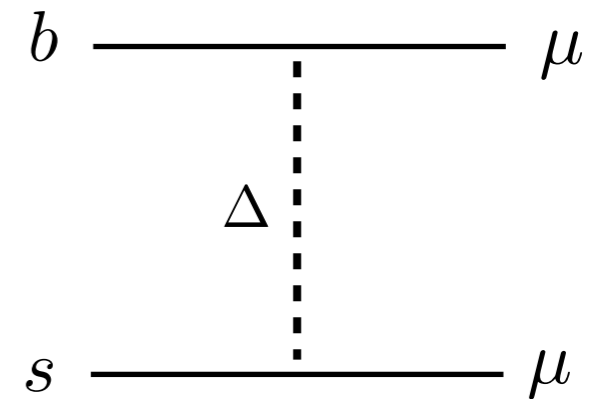
$\mu \neq e$

$$C_9 = -C_{10} :$$

Leptoquarks

Hiller, Schmaltz 1408.1627 Becirevic et al. 1608.08501

$$\Delta = \begin{pmatrix} \Delta^{2/3} \\ \Delta^{-1/3} \end{pmatrix} \sim (3, 2)_{1/6}$$



$$\mathcal{L}_\Delta = \bar{d}'_R Y_L (\tilde{\Delta})^\dagger L' = \bar{d}_R (Y_L U_{\text{PMNS}}) \nu_L \Delta^{(-1/3)} - \bar{d}_R Y_L \ell_L \Delta^{(2/3)}$$

Contribution to b- \rightarrow s transitions

$$\mathcal{L}_{\text{eff}}^{d_k \rightarrow d_i \ell \ell} = \frac{1}{m_\Delta^2} Y_L^{ij} Y_L^{*kl} \bar{d}_i P_L \ell_j \bar{\ell}_l P_R d_k = -\frac{Y_L^{ij} Y_L^{*kl}}{2m_\Delta^2} \bar{d}_i \gamma_\mu P_R d_k \bar{\ell}_l \gamma^\mu P_L \ell_j$$

works for

$$C_9 = -C_{10} = \frac{Y_L^{12} Y_L^{*32}}{2m_\Delta^2} (24\text{TeV})^2$$

Models for bs transitions

$\mu \neq e$

$$C_9 = -C_{10} :$$

Leptoquarks

Becirevic et al. 1608.08501

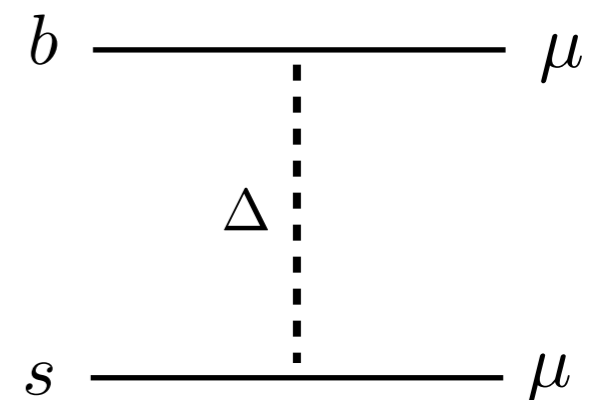
$$\Delta = \begin{pmatrix} \Delta^{2/3} \\ \Delta^{-1/3} \end{pmatrix} \sim (3, 2)_{1/6}$$

$$\mathcal{L}_\Delta = \bar{d}'_R Y_L (\tilde{\Delta})^\dagger L' + \bar{Q}' Y_R \Delta \nu'_R$$

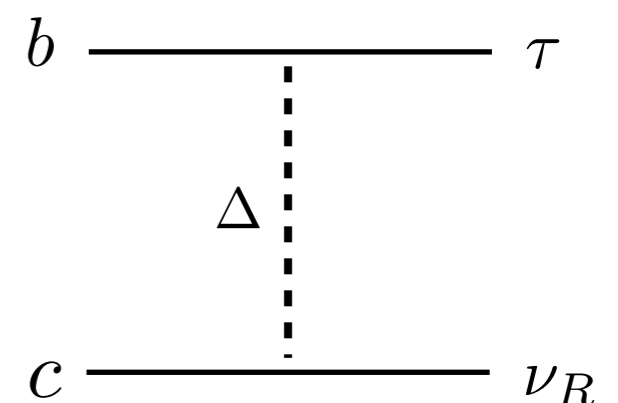
$$= \bar{d}_R (Y_L U_{\text{PMNS}}) \nu_L \Delta^{(-1/3)} - \bar{d}_R Y_L \ell_L \Delta^{(2/3)}$$

$$+ \bar{u}_L (V_{\text{CKM}} Y_R) \nu_R \Delta^{(2/3)} + \bar{d}_L Y_R \nu_R \Delta^{(-1/3)}$$

induces $b \rightarrow c$ transitions!



$\tau \neq \mu, e$



Models for bs transitions

$\mu \neq e$

$$C_9 = -C_{10} :$$

Leptoquarks

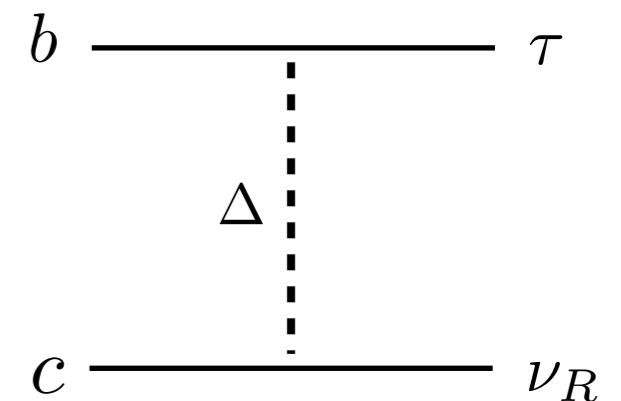
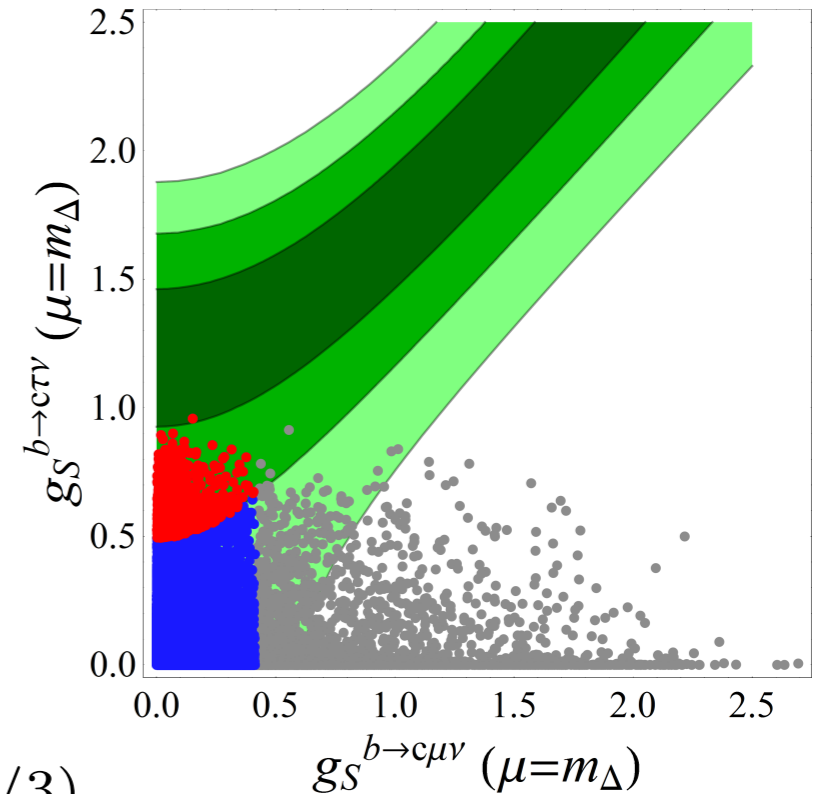
Becirevic et al. 1608.08501

$$\Delta = \begin{pmatrix} \Delta^{2/3} \\ \Delta^{-1/3} \end{pmatrix} \sim (3, 2)_{1/6}$$

$$\mathcal{L}_\Delta = \bar{d}'_R Y_L (\tilde{\Delta})^\dagger L' + \bar{Q}' Y_R \Delta \nu'_R$$

$$= \bar{d}_R (Y_L U_{\text{PMNS}}) \nu_L \Delta^{(-1/3)} - \bar{d}_R Y_L \ell_L \Delta^{(2/3)}$$

$$+ \bar{u}_L (V_{\text{CKM}} Y_R) \nu_R \Delta^{(2/3)} + \bar{d}_L Y_R \nu_R \Delta^{(-1/3)}$$



induces b -> c transitions!

$$M = 0.7 - 1 \text{ TeV}$$

One LQ to rule them all



Idea: Explain $R(D^{(*)})$ at tree-level and R_K, R_{K^*} at loop-level

MB, Neubert 1511.01900

Add a single leptoquark $\phi \sim (\mathbf{3}, \mathbf{1})_{-1/3}$

$$\begin{aligned} \mathcal{L}_\phi = & (D_\mu \phi)^\dagger D_\mu \phi - M_\phi^2 |\phi|^2 - g_{h\phi} |\Phi|^2 |\phi|^2 \\ & + \bar{Q}^c \boldsymbol{\lambda}^L i\tau_2 L \phi^* + \bar{u}_R^c \boldsymbol{\lambda}^R e_R \phi^* + \text{h.c.} \end{aligned}$$

Rotation to mass eigenstates

$$\mathcal{L}_\phi \ni \bar{u}_L^c \boldsymbol{\lambda}_{ue}^L e_L \phi^* - \bar{d}_L^c \boldsymbol{\lambda}_{d\nu}^L \nu_L \phi^* + \bar{u}_R^c \boldsymbol{\lambda}_{ue}^R e_R \phi^* + \text{h.c.}$$

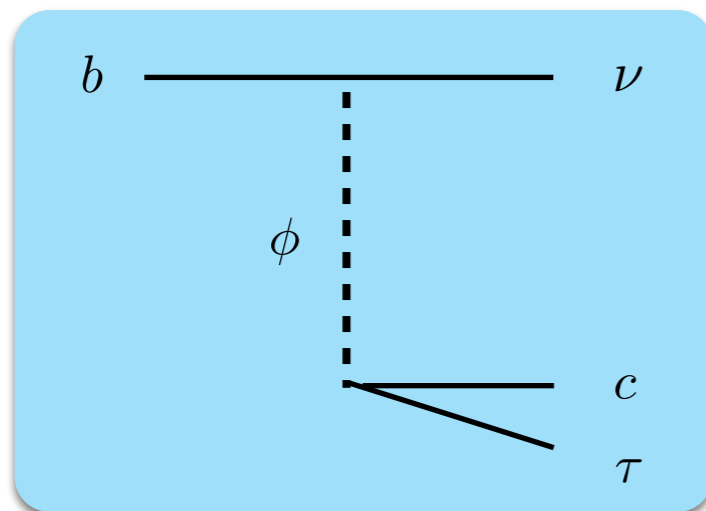
One LQ to rule them all



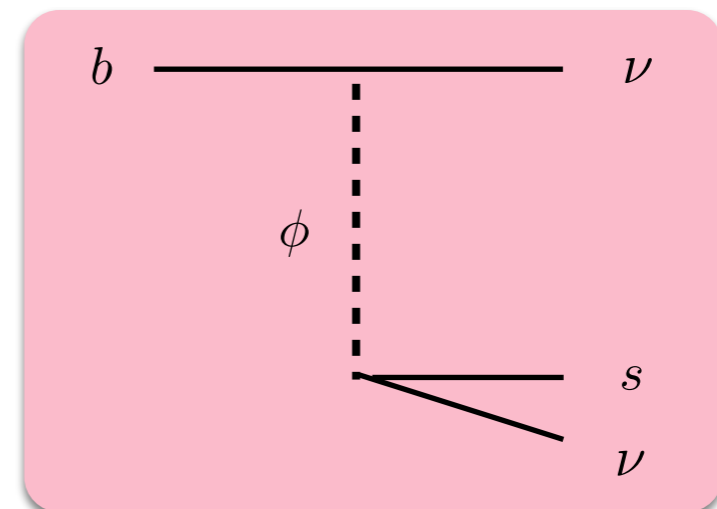
$$\mathcal{L}_\phi \ni \bar{u}_L^c \lambda_{ue}^L e_L \phi^* - \bar{d}_L^c \lambda_{d\nu}^L \nu_L \phi^* + \bar{u}_R^c \lambda_{ue}^R e_R \phi^* + \text{h.c.}$$

at tree level gives rise to

up-quark -
charged lepton
couplings



down-quark -
neutrino
couplings



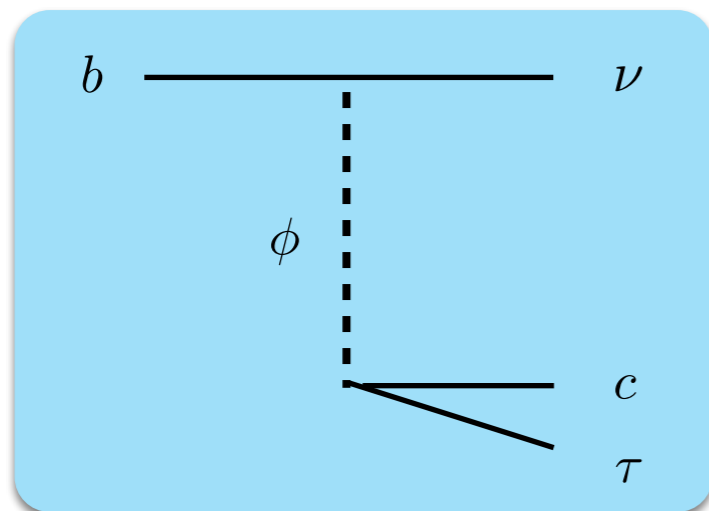
One LQ to rule them all



$$\mathcal{L}_\phi \ni \bar{u}_L^c \lambda_{ue}^L e_L \phi^* - \bar{d}_L^c \lambda_{d\nu}^L \nu_L \phi^* + \bar{u}_R^c \lambda_{ue}^R e_R \phi^* + \text{h.c.}$$

at tree level gives rise to

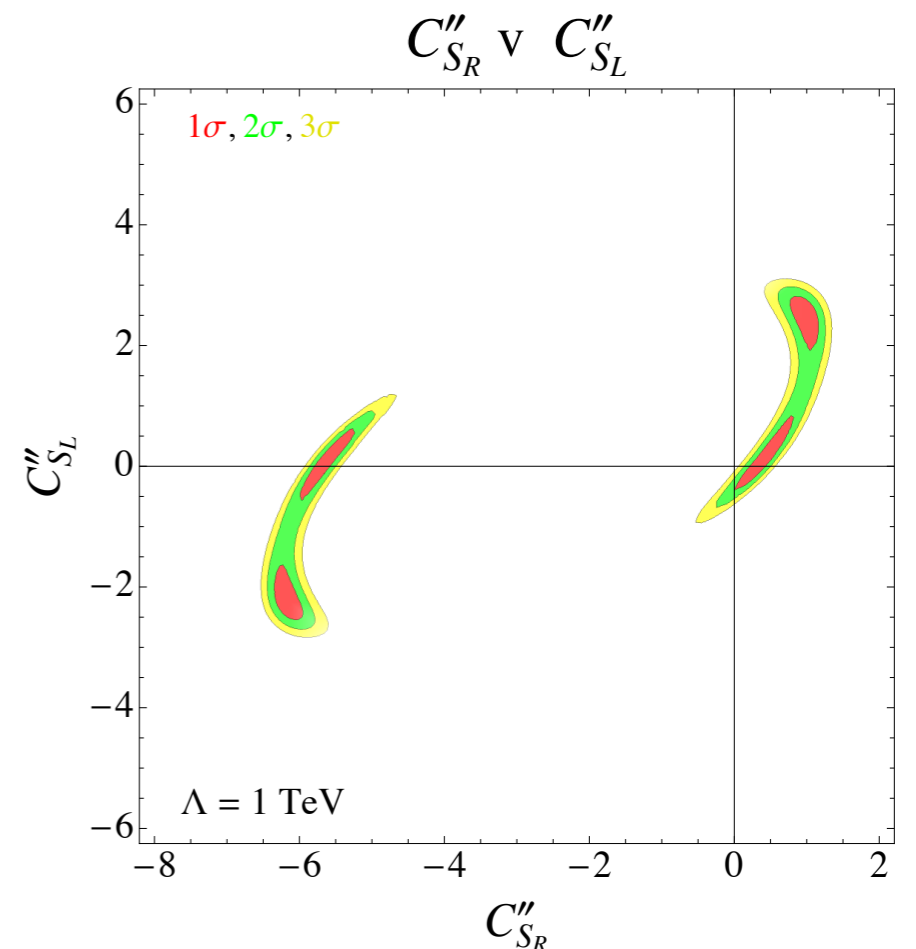
up-quark -
charged lepton
couplings



$R(D^{(*)})$ needs

$$\frac{\lambda_{c\tau}^{L*} \lambda_{b\nu\tau}^L}{M_\phi^2} \approx \frac{0.35}{\text{TeV}^2},$$

$$\frac{\lambda_{c\tau}^{R*} \lambda_{b\nu\tau}^L}{M_\phi^2} \approx -\frac{0.03}{\text{TeV}^2}$$

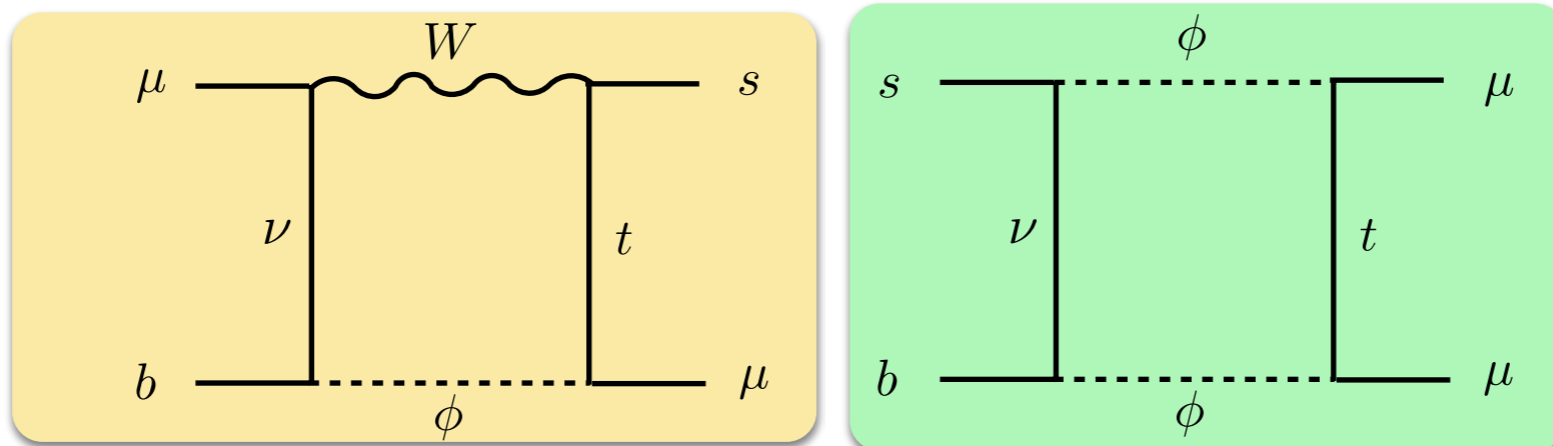


One LQ to rule them all



$$\mathcal{L}_\phi \ni \bar{u}_L^c \lambda_{ue}^L e_L \phi^* - \bar{d}_L^c \lambda_{d\nu}^L \nu_L \phi^* + \bar{u}_R^c \lambda_{ue}^R e_R \phi^* + \text{h.c.}$$

at loop level gives rise to

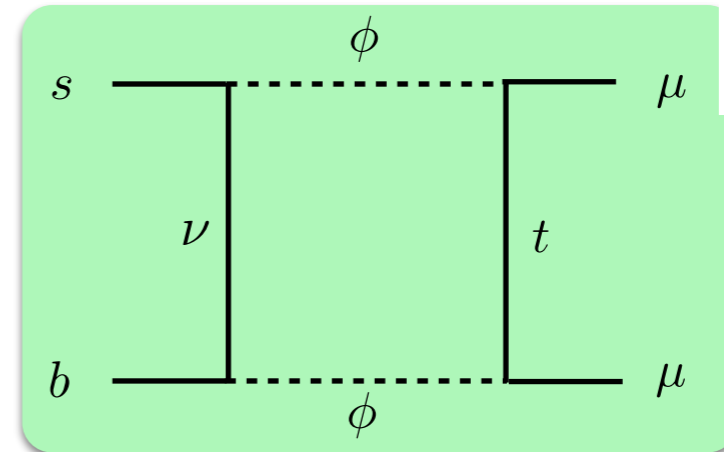
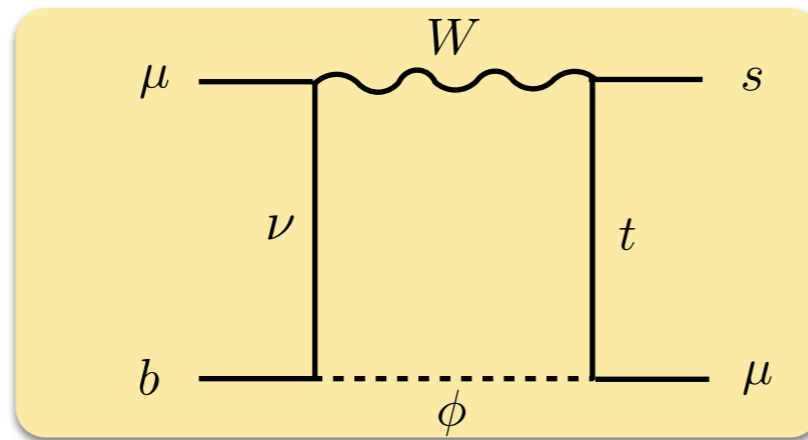


can this explain RK with a $M = \text{few TeV}$ leptoquark?

One LQ to rule them all



We have



$$C_{LL}^{\mu(\phi)} = \frac{m_t^2}{8\pi\alpha M_\phi^2} |\lambda_{t\mu}^L|^2 - \frac{1}{64\pi\alpha} \frac{\sqrt{2}}{G_F M_\phi^2} \frac{(\lambda^L \lambda^{L\dagger})_{bs}}{V_{tb} V_{ts}^*} (\lambda^{L\dagger} \lambda^L)_{\mu\mu},$$

$$C_{LR}^{\mu(\phi)} = \frac{m_t^2}{16\pi\alpha M_\phi^2} |\lambda_{t\mu}^R|^2 \left[\ln \frac{M_\phi^2}{m_t^2} - f(x_t) \right] - \frac{1}{64\pi\alpha} \frac{\sqrt{2}}{G_F M_\phi^2} \frac{(\lambda^L \lambda^{L\dagger})_{bs}}{V_{tb} V_{ts}^*} (\lambda^{R\dagger} \lambda^R)_{\mu\mu},$$

The $W - \phi$ box contributions have the wrong sign, but they are chirally suppressed and inherit a partial GIM-suppression. Penguins cancel!

$$C_{LL} = C_9^{\mu\mu} - C_{10}^{\mu\mu}$$

One LQ to rule them all



$$C_{LL}^{\mu(\phi)} = \frac{m_t^2}{8\pi\alpha M_\phi^2} |\lambda_{t\mu}^L|^2 - \frac{1}{64\pi\alpha} \frac{\sqrt{2}}{G_F M_\phi^2} \frac{(\lambda^L \lambda^{L\dagger})_{bs}}{V_{tb} V_{ts}^*} (\lambda^{L\dagger} \lambda^L)_{\mu\mu},$$

$$C_{LR}^{\mu(\phi)} = \frac{m_t^2}{16\pi\alpha M_\phi^2} |\lambda_{t\mu}^R|^2 \left[\ln \frac{M_\phi^2}{m_t^2} - f(x_t) \right] - \frac{1}{64\pi\alpha} \frac{\sqrt{2}}{G_F M_\phi^2} \frac{(\lambda^L \lambda^{L\dagger})_{bs}}{V_{tb} V_{ts}^*} (\lambda^{R\dagger} \lambda^R)_{\mu\mu},$$

For the Benchmark $C_{LL}^\mu \simeq -1$, $C_{ij}^\mu = 0$ otherwise, we need

$$\sum_i |\lambda_{u_i\mu}^L|^2 \operatorname{Re} \frac{(\lambda^L \lambda^{L\dagger})_{bs}}{V_{tb} V_{ts}^*} - 1.74 |\lambda_{t\mu}^L|^2 \approx 12.5 \frac{M_\phi^2}{\text{TeV}^2}$$

Constrained to be
< 2.3 by $R_{\nu\nu}$

$$\Rightarrow \sqrt{|\lambda_{u\mu}^L|^2 + |\lambda_{c\mu}^L|^2 + \left(1 - \frac{0.77}{\hat{M}_\phi^2}\right) |\lambda_{t\mu}^L|^2} > 2.36$$

One LQ to rule them all



For the Benchmark $C_{LL}^\mu \simeq -1$, $C_{ij}^\mu = 0$ otherwise, we need

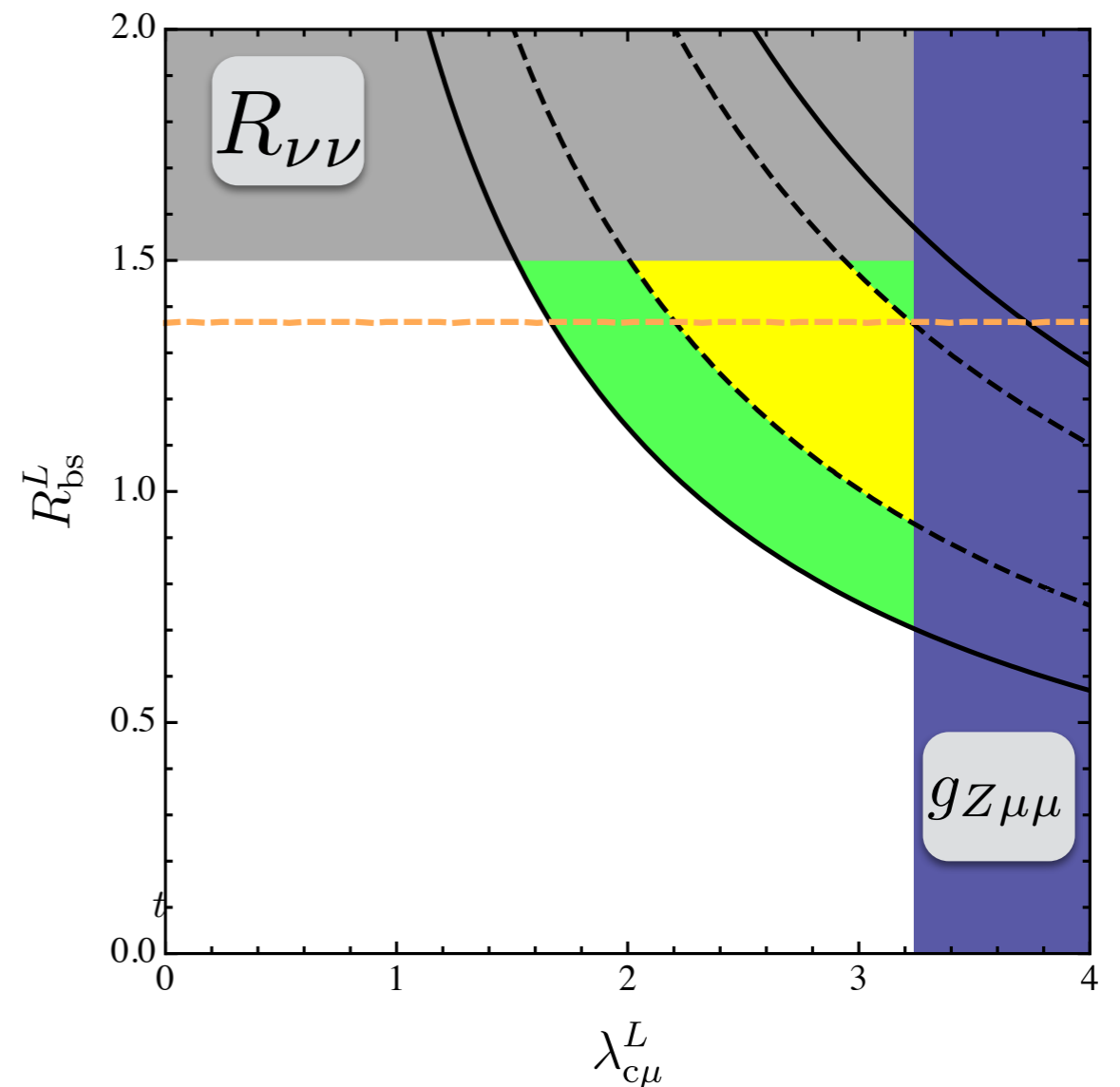
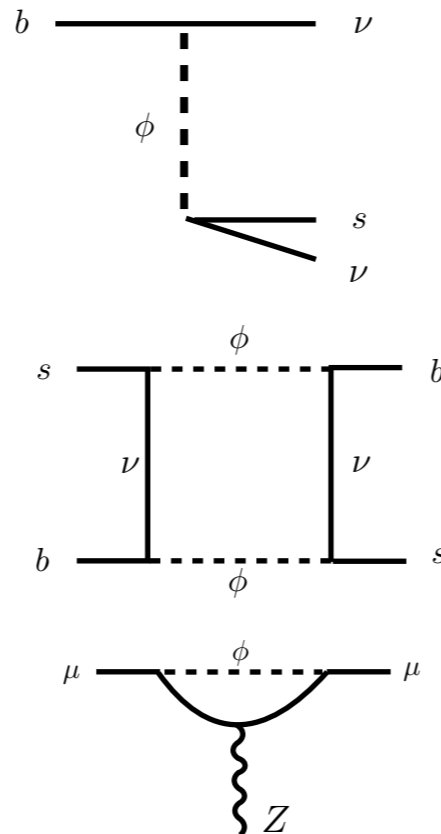
$$\sum_i |\lambda_{u_i\mu}^L|^2 \underbrace{\text{Re} \frac{(\lambda^L \lambda^{L\dagger})_{bs}}{V_{tb} V_{ts}^*}}_{R_{bs}^L} - 1.74 |\lambda_{t\mu}^L|^2 \approx 12.5 \frac{M_\phi^2}{\text{TeV}^2}$$

Constraints:

$$\bar{B} \rightarrow K^{(*)} \nu \bar{\nu}$$

$$\bar{B}_s - B_s$$

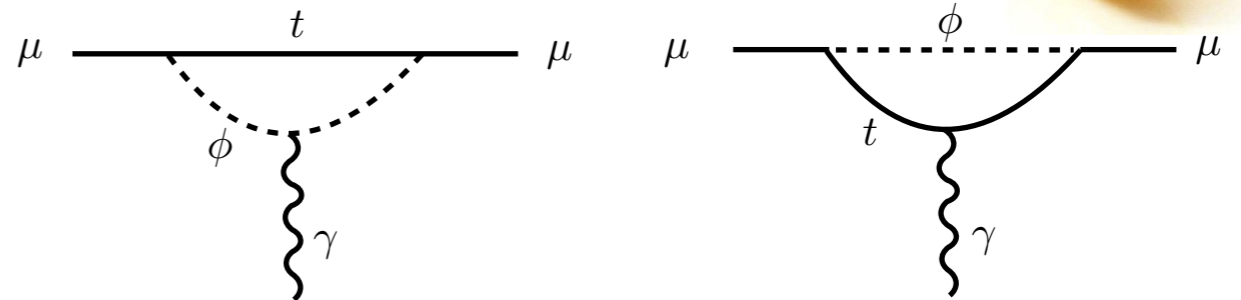
$$gZ\mu\mu$$



One LQ to rule them all



- One-loop Contribution to $g-2$



$$a_{\mu}^{(\phi)} = \sum_{q=t,c} \frac{m_{\mu} m_q}{4\pi^2 M_{\phi}^2} \left(\ln \frac{M_{\phi}^2}{m_q^2} - \frac{7}{4} \right) \text{Re}(\lambda_{q\mu}^R \lambda_{q\mu}^{L*}) - \frac{m_{\mu}^2}{32\pi^2 M_{\phi}^2} \left[(\lambda^{L\dagger} \lambda^L)_{\mu\mu} + (\lambda^{R\dagger} \lambda^R)_{\mu\mu} \right]$$

$$a_{\mu}^{\text{exp}} = 287 \pm 80 \times 10^{-11}$$

$$-37 \times 10^{-11}$$

$$\left(1 + 0.17 \ln \frac{M_{\phi}}{\text{TeV}} \right) \text{Re}(\lambda_{c\mu}^R \lambda_{c\mu}^{L*}) + 20.7 \left(1 + 1.06 \ln \frac{M_{\phi}}{\text{TeV}} \right) \text{Re}(\lambda_{t\mu}^R \lambda_{t\mu}^{L*}) \approx 0.08 \frac{M_{\phi}^2}{\text{TeV}^2}$$

For $|\lambda_{c\mu}^L| \sim 2.4$, we need $|\lambda_{c\mu}^R| \sim 0.03$.

One LQ to rule them all



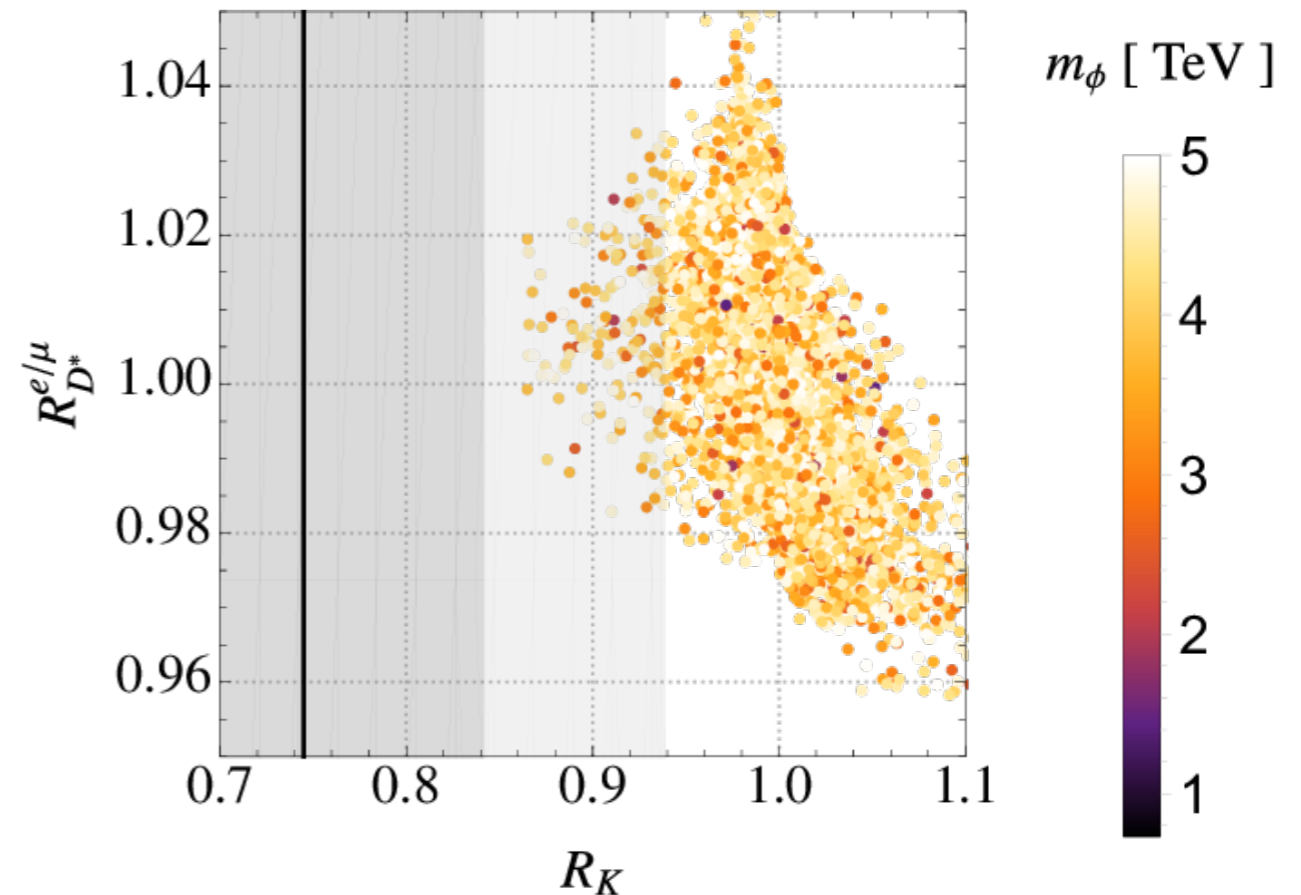
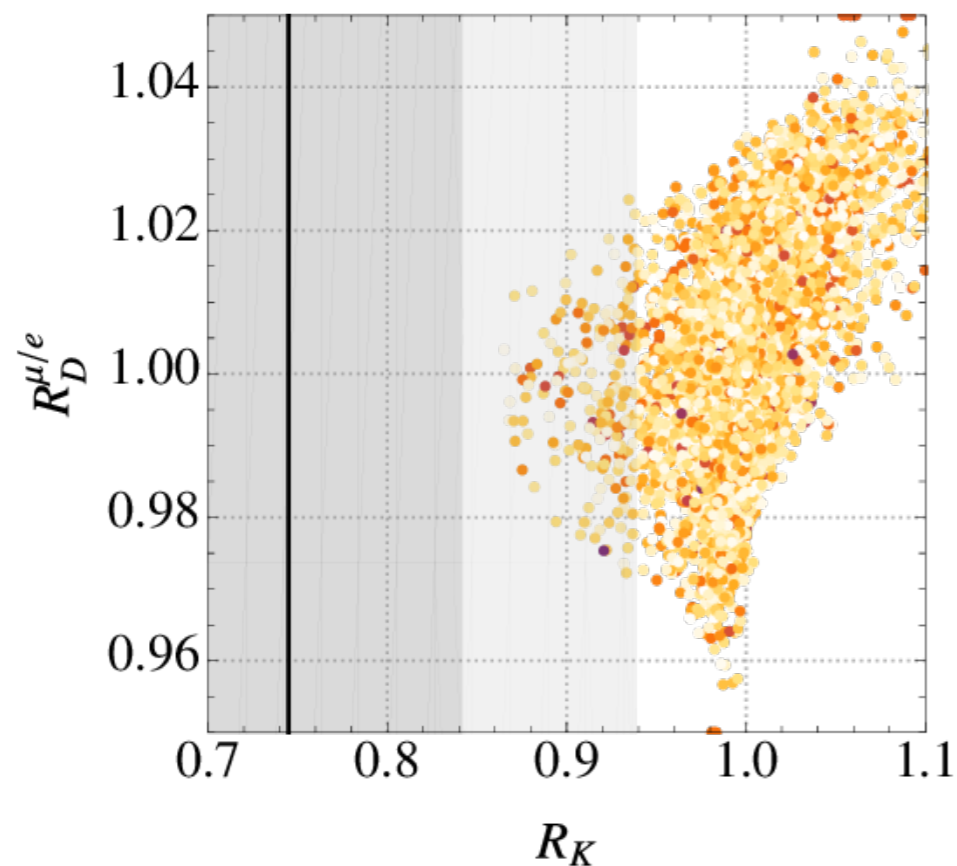
Loop-induced non-universality in mu and e comes at a prize

Becirevic et al. 1608.08501 Cai et. al. 1704.05849

$$R_{D^{(*)}}^{\mu/e} = \frac{\Gamma(\bar{B} \rightarrow D^{(*)} \mu \bar{\nu})}{\Gamma(\bar{B} \rightarrow D^{(*)} e \bar{\nu})},$$

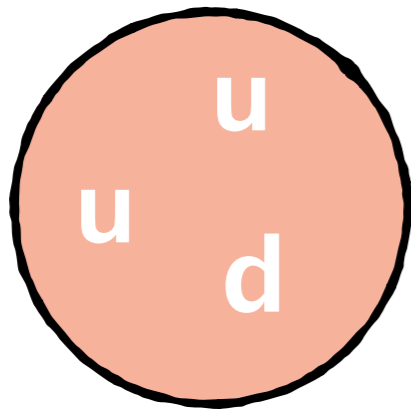
$$R_D^{\mu/e} = 0.995 \pm 0.022 \pm 0.039$$

$$R_{D^*}^{e/\mu} = 1.04 \pm 0.05 \pm 0.01$$

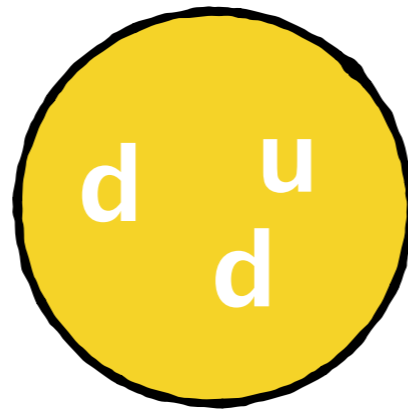


The Standard Model in the 30s

The known particles were the



Proton



Neutron



Electron

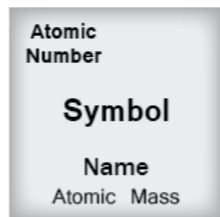


Neutrino

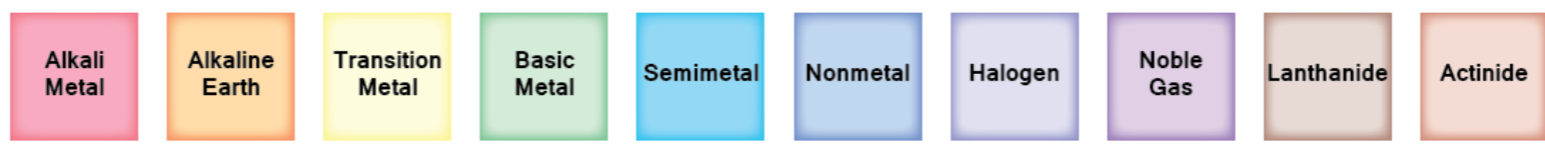
This was a very successful model, as it greatly simplified the previous best candidate for a fundamental theory of elementary particles, the periodic table of elements.

Periodic Table of the Elements

1 IA 1A																	13 IIIA 3A	14 IVA 4A	15 VA 5A	16 VIA 6A	17 VIIA 7A	18 VIIIA 8A	
1 H Hydrogen 1.008																	5 B Boron 10.811	6 C Carbon 12.011	7 N Nitrogen 14.007	8 O Oxygen 15.999	9 F Fluorine 18.998	10 Ne Neon 20.180	
3 Li Lithium 6.941	4 Be Beryllium 9.012																	13 Al Aluminum 26.982	14 Si Silicon 28.086	15 P Phosphorus 30.974	16 S Sulfur 32.066	17 Cl Chlorine 35.453	18 Ar Argon 39.948
11 Na Sodium 22.990	12 Mg Magnesium 24.305	3 IIIB 3B	4 IVB 4B	5 VB 5B	6 VIB 6B	7 VIIB 7B	8 VIII 8	9 VIII 8	10 VIII 8	11 IB 1B	12 IIB 2B	31 Ga Gallium 69.723	32 Ge Germanium 72.631	33 As Arsenic 74.922	34 Se Selenium 78.971	35 Br Bromine 79.904	36 Kr Krypton 84.798						
19 K Potassium 39.098	20 Ca Calcium 40.078	21 Sc Scandium 44.956	22 Ti Titanium 47.867	23 V Vanadium 50.942	24 Cr Chromium 51.996	25 Mn Manganese 54.938	26 Fe Iron 55.845	27 Co Cobalt 58.933	28 Ni Nickel 58.693	29 Cu Copper 63.546	30 Zn Zinc 65.38	49 In Indium 114.818	50 Sn Tin 118.711	51 Sb Antimony 121.760	52 Te Tellurium 127.6	53 I Iodine 126.904	54 Xe Xenon 131.294						
37 Rb Rubidium 84.468	38 Sr Strontium 87.62	39 Y Yttrium 88.906	40 Zr Zirconium 91.224	41 Nb Niobium 92.906	42 Mo Molybdenum 95.95	43 Tc Technetium 98.907	44 Ru Ruthenium 101.07	45 Rh Rhodium 102.906	46 Pd Palladium 106.42	47 Ag Silver 107.868	48 Cd Cadmium 112.411	81 Tl Thallium 204.383	82 Pb Lead 207.2	83 Bi Bismuth 208.980	84 Po Polonium [208.982]	85 At Astatine 209.987	86 Rn Radon 222.018						
55 Cs Cesium 132.905	56 Ba Barium 137.328	57-71	72 Hf Hafnium 178.49	73 Ta Tantalum 180.948	74 W Tungsten 183.84	75 Re Rhenium 186.207	76 Os Osmium 190.23	77 Ir Iridium 192.217	78 Pt Platinum 195.085	79 Au Gold 196.967	80 Hg Mercury 200.592	113 Uut Ununtrium unknown	114 Fl Flerovium [289]	115 Uup Ununpentium unknown	116 Lv Livermorium [298]	117 Uus Ununseptium unknown	118 Uuo Ununoctium unknown						
87 Fr Francium 223.020	88 Ra Radium 226.025	89-103	104 Rf Rutherfordium [261]	105 Db Dubnium [262]	106 Sg Seaborgium [266]	107 Bh Bohrium [264]	108 Hs Hassium [269]	109 Mt Meitnerium [268]	110 Ds Darmstadtium [269]	111 Rg Roentgenium [272]	112 Cn Copernicium [277]	113 Uut Ununtrium unknown	114 Fl Flerovium [289]	115 Uup Ununpentium unknown	116 Lv Livermorium [298]	117 Uus Ununseptium unknown	118 Uuo Ununoctium unknown						



Lanthanide Series	57 La Lanthanum 138.905	58 Ce Cerium 140.116	59 Pr Praseodymium 140.908	60 Nd Neodymium 144.243	61 Pm Promethium 144.913	62 Sm Samarium 150.36	63 Eu Europium 151.964	64 Gd Gadolinium 157.25	65 Tb Terbium 158.925	66 Dy Dysprosium 162.500	67 Ho Holmium 164.930	68 Er Erbium 167.259	69 Tm Thulium 168.934	70 Yb Ytterbium 173.055	71 Lu Lutetium 174.967
Actinide Series	89 Ac Actinium 227.028	90 Th Thorium 232.038	91 Pa Protactinium 231.036	92 U Uranium 238.029	93 Np Neptunium 237.048	94 Pu Plutonium 244.064	95 Am Americium 243.061	96 Cm Curium 247.070	97 Bk Berkelium 247.070	98 Cf Californium 251.080	99 Es Einsteinium [254]	100 Fm Fermium 257.095	101 Md Mendelevium 258.1	102 No Nobelium 259.101	103 Lr Lawrencium [262]



The Standard Model in the 30s

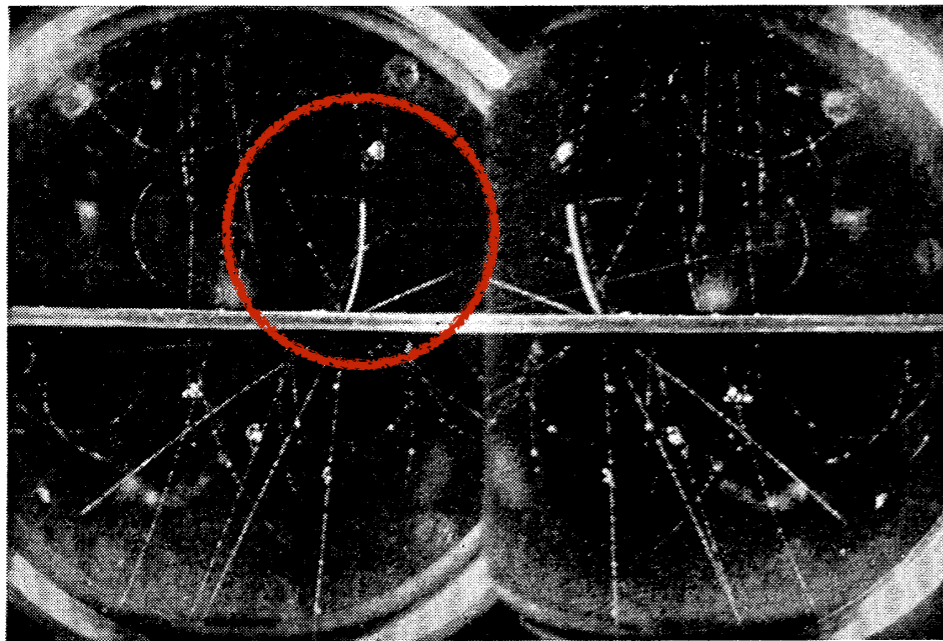


FIG. 12. Pike's Peak, 7900 gauss. A disintegration produced by a nonionizing ray occurs at a point in the 0.35 cm lead plate, from which six particles are ejected. One of the particles (strongly ionizing) ejected nearly vertically upward has the range of a 1.5 MEV proton. Its energy (given by its range) corresponds to an $H\rho = 1.7 \times 10^5$, or a radius of 20 cm, which is three times the observed value. If the observed curvature were produced entirely by magnetic deflection it would be necessary to conclude that this track represents a massive particle with an e/m much greater than that of a proton or any other known nucleus. As there are no experimental data available on the multiple scattering of low energy protons in argon it is difficult to estimate to what extent scattering may have modified the curvature in this case. The particle is therefore tentatively interpreted as a proton. The other particle ejected upward

Neddermeyer and Anderson discover a new fermion with

$$m = 106 \text{ MeV}$$



Neddermeyer



Anderson

Who ordered that?

-Rabi