

# Latest developments from xFitter



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on behalf of xFitter developers team  
2019-09-17

- ▶ Analyses being prepared
  - ▶ PDF Profiling Using the Forward-Backward Asymmetry in Neutral Current Drell-Yan Production
  - ▶ Probing the strange content of the proton with charm production in charged current at LHeC
  - ▶ Parton Distribution Functions of the Charged Pion Within The `xFitter` Framework
- ▶ Development of `xFitter` code

## PDF Profiling Using the Forward-Backward Asymmetry in Neutral Current Drell-Yan Production ([arxiv:1907.07727](https://arxiv.org/abs/1907.07727))

How will new  $A_{\text{FB}}^*$  data on neutral-current Drell-Yan process from the LHC improve determinations of PDFs?

$$A_{\text{FB}}^* = \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B}, \quad \sigma_F = \sigma[\cos \theta > 0], \quad \sigma_B = \sigma[\cos \theta < 0],$$

where  $\theta$  is the angle between the incoming quark and the outgoing lepton in the Collins-Soper frame.

Perform profiling for different PDF sets: CT14nnlo[1], NNPDF3.1nnlo (Hessian set)[2], ABMP16nnlo[3], HERAPDF2.0nnlo (EIG)[4], and MMHT2014nnlo[5]

# Expected sensitivity of $A_{\text{FB}}^*$

$$\frac{d^3\sigma}{dM_{\ell\ell}dy_{\ell\ell}d\cos\theta^*} = \frac{\pi\alpha^2}{3M_{\ell\ell}s} \sum_q P_q [f_q(x_1, Q^2)f_{\bar{q}}(x_2, Q^2) + f_{\bar{q}}(x_1, Q^2)f_q(x_2, Q^2)]$$

$$\begin{aligned} P_q &= e_\ell^2 e_q^2 (1 + \cos^2 \theta^*) \\ &+ \frac{2M_{\ell\ell}^2(M_{\ell\ell}^2 - M_Z^2)}{\sin^2 \theta_W \cos^2 \theta_W [(M_{\ell\ell}^2 - M_Z^2)^2 + \Gamma_Z^2 M_Z^2]} (e_\ell e_q) [\nu_\ell \nu_q (1 + \cos^2 \theta^*) + \cancel{2a_\ell a_q \cos \theta^*}] \\ &+ \frac{M_{\ell\ell}^4}{\sin^4 \theta_W \cos^4 \theta_W [(M_{\ell\ell}^2 - M_Z^2)^2 + \Gamma_Z^2 M_Z^2]} [(a_\ell^2 + \nu_\ell^2)(a_q^2 + \nu_q^2)(1 + \cos^2 \theta^*) \\ &+ \cancel{8a_\ell \nu_\ell a_q \nu_q \cos \theta^*}], \end{aligned}$$

Terms other than those linear in  $\cos \theta^*$  cancel in  $A_{\text{FB}}^*$ , and the dominant contribution is the  $\gamma Z$  interference term.

Therefore, we expect  $A_{\text{FB}}^*$  to be sensitive to

$$e_\ell a_\ell [e_u a_u u_V(x, Q^2) + e_d a_d d_V(x, Q^2)] \propto \frac{2}{3} u_V(x, Q^2) + \frac{1}{3} d_V(x, Q^2)$$

This is complementary to lepton charge asymmetry Drell-Yan data, which is most sensitive to  $u_V - d_V$

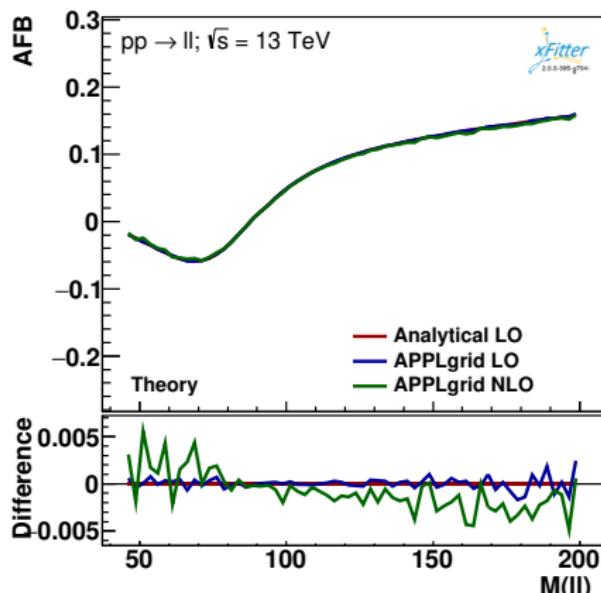
# Generation of pseudodata

Pseudodata was generated in bins of dilepton mass  $M_{\ell\ell}$  from 45 GeV to 200 GeV with step 2.5 GeV (62 bins), and with different dilepton rapidity  $|y_{\ell\ell}|$  cuts, from  $|y_{\ell\ell}| = 0$  to  $|y_{\ell\ell}| = 2.5$  with step 0.5. The statistical uncertainty of the pseudodata was based on 3 values for integrated luminosity:

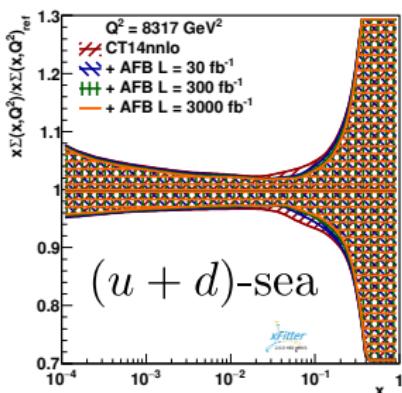
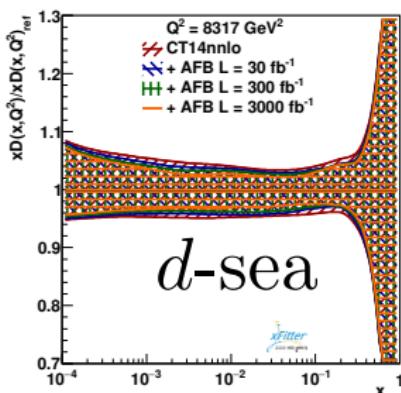
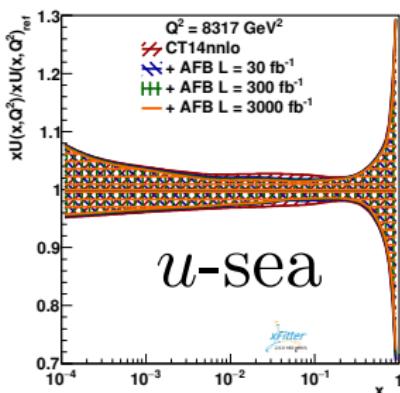
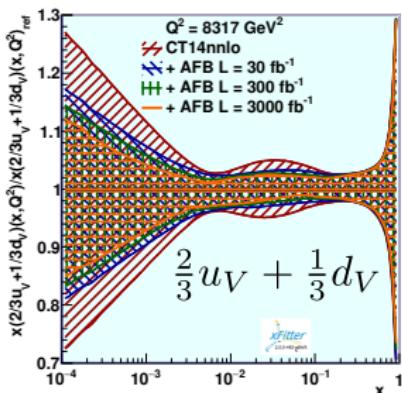
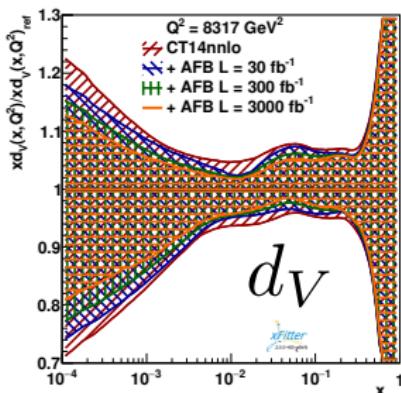
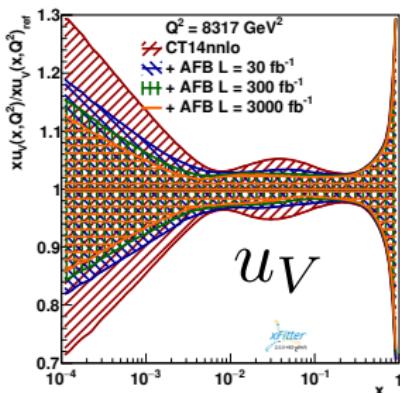
- ▶  $L = 30 \text{ fb}^{-1}$ ,
- ▶  $L = 300 \text{ fb}^{-1}$  (end of Run 3),
- ▶  $L = 3000 \text{ fb}^{-1}$  (end of HL-LHC).

This estimate of statistical uncertainty included a factor of  $\sim 0.2$  for detector acceptance and efficiency.

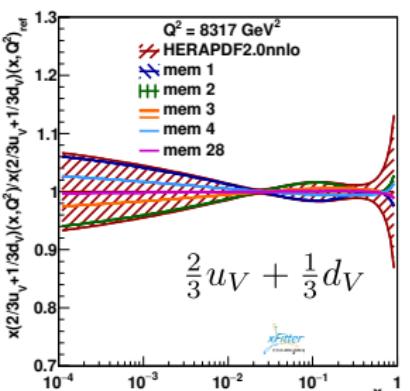
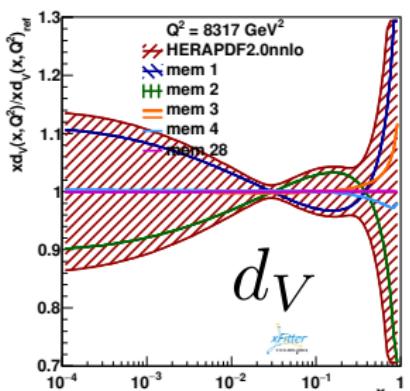
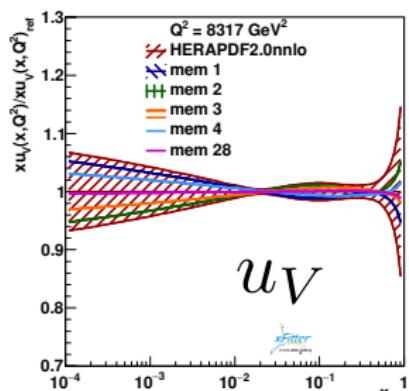
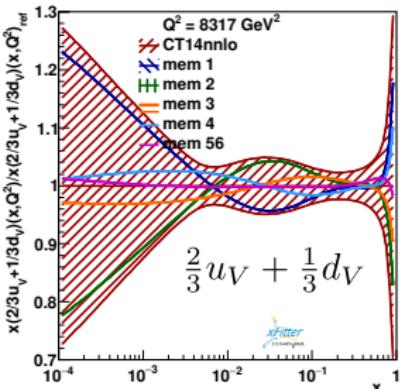
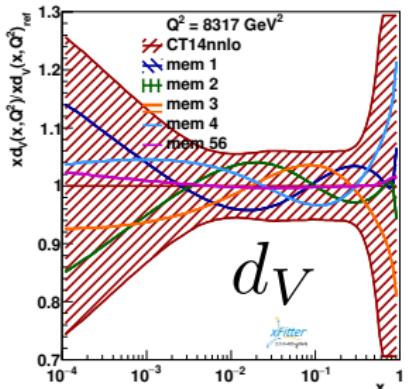
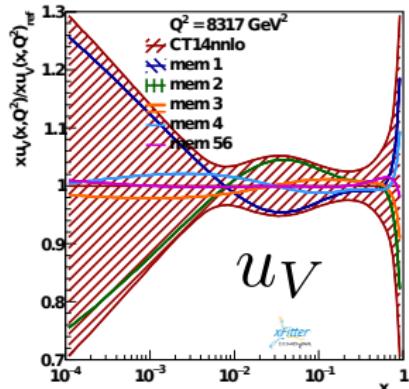
Predictions at LO and NLO were obtained using MadGraph5\_aMC@NLO[6], APPLgrid[7], and aMCfast[8] packages, and with an independent analytical code at LO.



# Impact on PDFs



# Rotated eigenvectors



## Probing the strange content of the proton with charm production in charged current at LHeC ([arxiv:1907.01014](https://arxiv.org/abs/1907.01014))

1. How can future data on charm production in charged-current DIS at the LHeC constrain strange-quark PDF?
2. What is the difference in predictions for different heavy flavor schemes?

Heavy-flavor schemes:

**FFNS A** 3 flavors in both PDFs and  $\alpha_S$  evolution. Heavy flavors (charm) appear in matrix elements only.

PDF sets: ABMP16[9], HERAPDF2.0 FF3A[4]

**FFNS B** 3 flavors in PDFs, but variable number of active flavors in  $\alpha_S$  evolution. At NLO same matrix elements as in FFNS A.

PDF sets: HERAPDF2.0 FF3B[4]

**FONLL-B** (VFNS) Variable number of active flavors both in PDFs and in  $\alpha_S$  evolution, neglecting masses. Fixed-order-next-to-leading massive matrix elements.

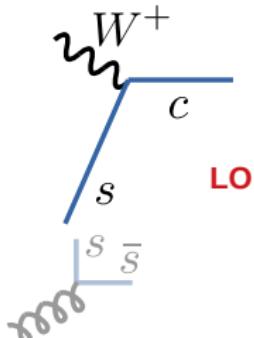
PDF sets: NNPDF3.1[2]

Predictions for each scheme are obtained with associated PDF sets and theory parameters. All calculations and PDF sets are at NLO.

# Feynman diagrams in VFNS and in FFNS

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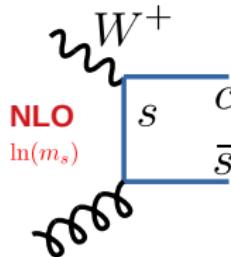
**t-channel**



$$f_s \otimes \sigma_{sW^+ \rightarrow c}$$

**VFNS  
only**

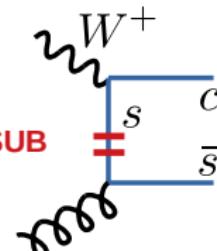
gluon initiated



$$f_g \otimes \sigma_{gW^+ \rightarrow c\bar{s}}$$

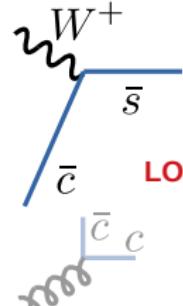
gluon initiated

gluon initiated

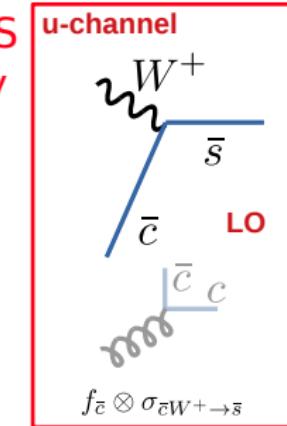


$$\tilde{f} \sim \ln(m_s)$$

**u-channel**



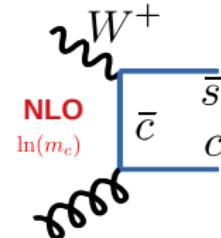
$$f_{\bar{c}} \otimes \sigma_{\bar{c}W^+ \rightarrow \bar{s}}$$



$$f_g \otimes \sigma_{gW^+ \rightarrow \bar{s}c}$$

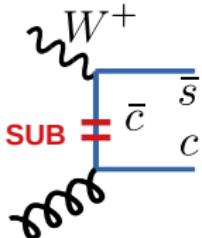
$$f_g \otimes \tilde{f}_{g \rightarrow s} \otimes \sigma_{sW^+ \rightarrow c}$$

**VFNS  
only**



$$f_g \otimes \sigma_{gW^+ \rightarrow \bar{s}c}$$

gluon initiated

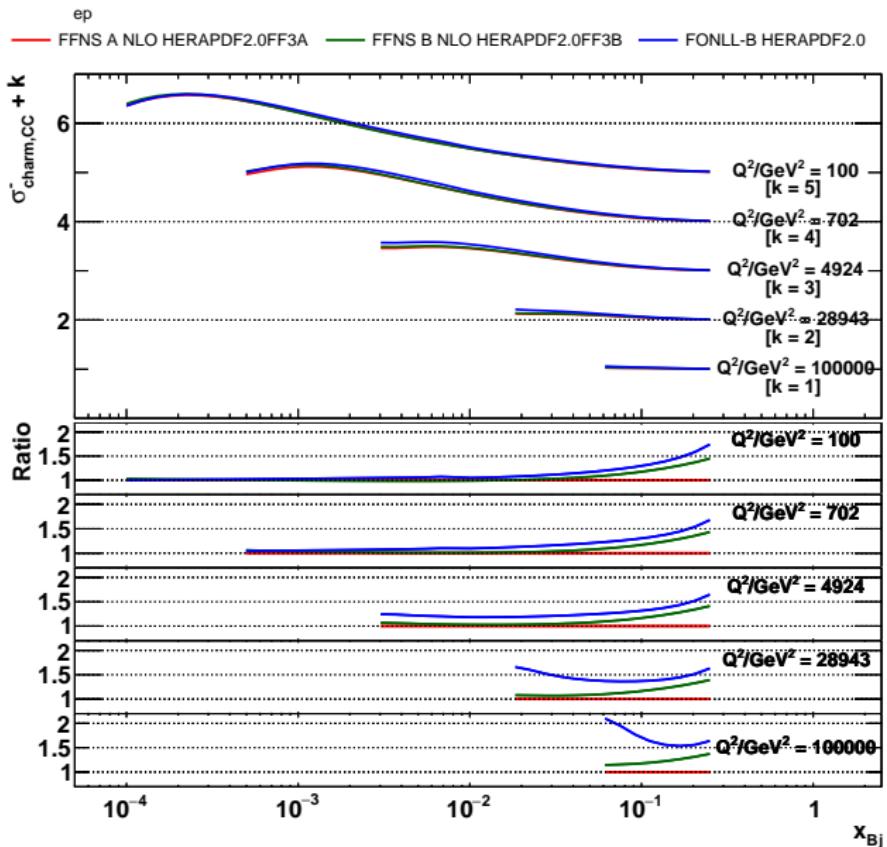


$$\tilde{f} \sim \ln(m_c)$$

$$f_g \otimes \tilde{f}_{g \rightarrow \bar{c}} \otimes \sigma_{\bar{c}W^+ \rightarrow \bar{s}}$$

# Comparison of predictions of different schemes

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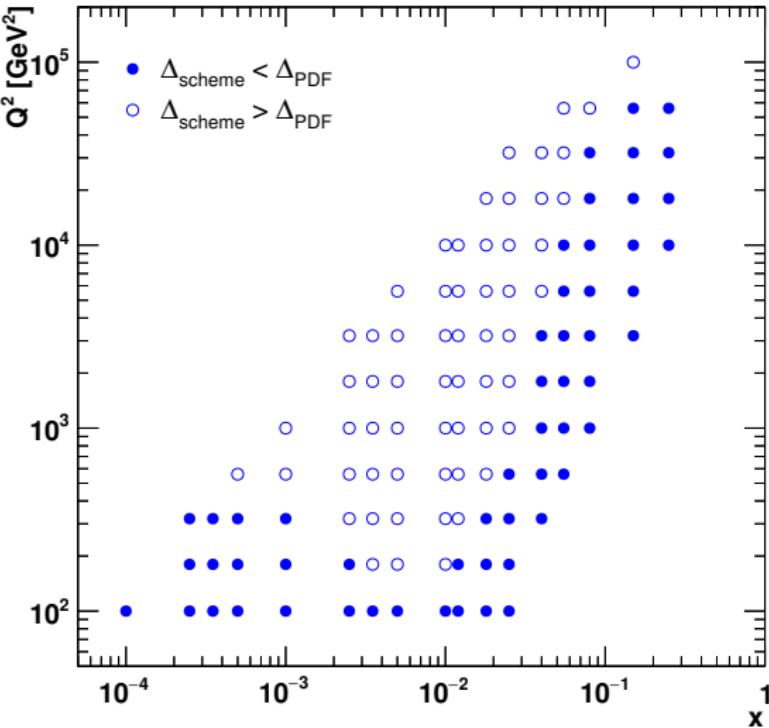
Predictions are different at large  $Q^2$  and high- $x$

# Generation of pseudodata

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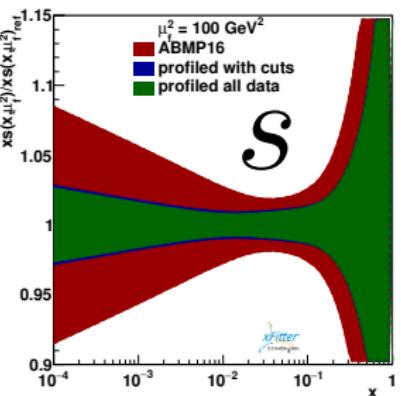
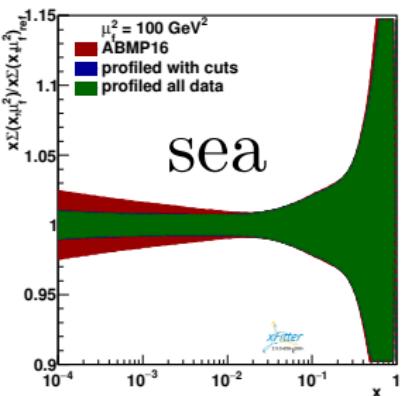
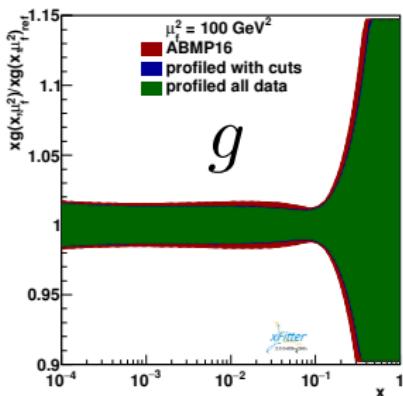
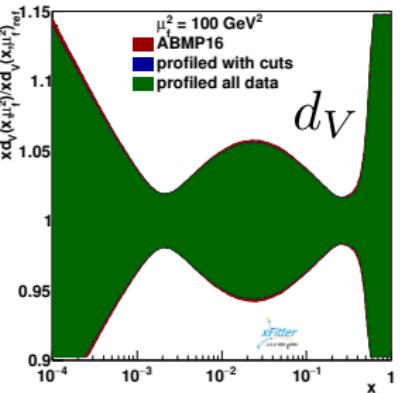
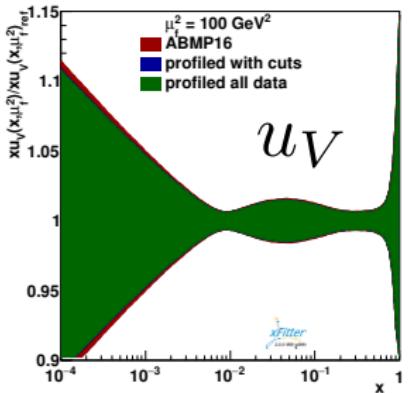
Pseudodata was generated with  
 $L = 100 \text{ fb}^{-1}$  and electron  
polarisation  $P = -0.8$

Restrict profiling to points with  
 $\Delta_{\text{scheme}} < \Delta_{\text{PDF}}$



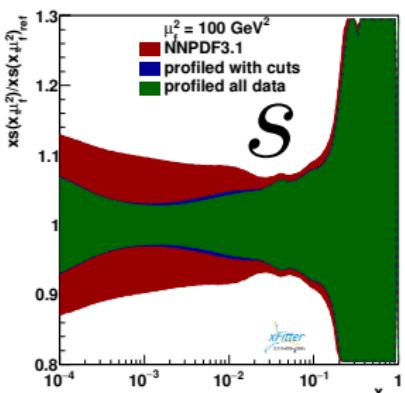
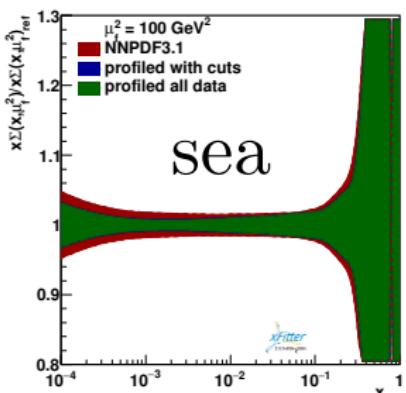
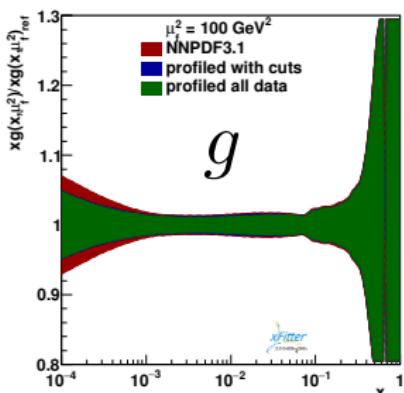
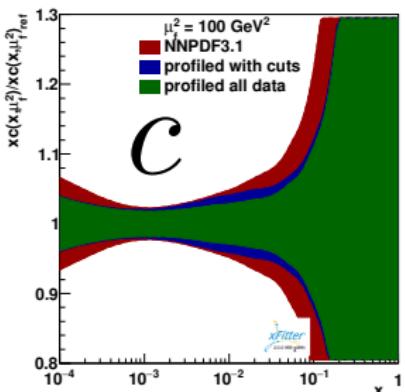
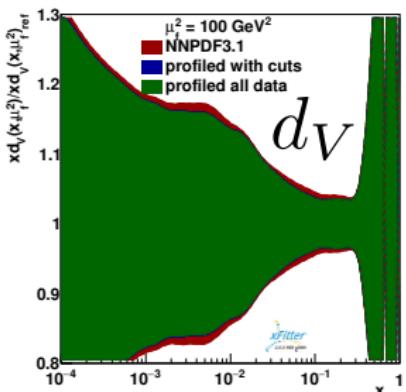
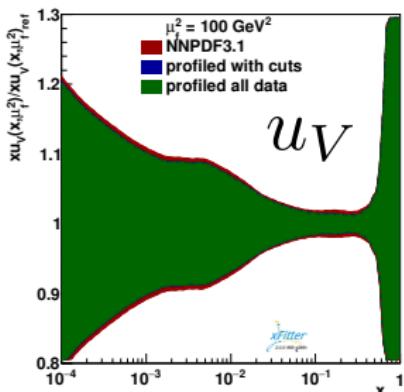
# Profiling ABMP16

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# Profiling NNPDF3.1

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**Parton Distribution Functions of the Charged Pion Within The xFitter Framework** (will be uploaded to arxiv in a few weeks)

A Next-to-leading order extraction of PDFs of charged pion from Drell-Yan and prompt photon production data.

E615[10] and NA10[11] experiments studied Drell-Yan dimuon production with a negative pion beam on a tungsten target:

$$\pi^- \frac{^{184}}{_{74}}\text{W} \rightarrow \mu^+ \mu^- X$$

The WA70[12] experiment studied prompt photon production with beams of negative and positive pions and a proton target:

$$\pi^\pm p \rightarrow \gamma X$$

In comparison to the prompt photon data, the Drell-Yan data is more precise, but is only sensitive to valence-quark PDFs. The prompt photon data has some sensitivity to sea and gluon, but also has larger uncertainties.

Predictions are obtained using APPLgrid[7], grids were generated using MCFM[13]. QCNDNUM[14] library is used for DGLAP evolution. Nuclear PDF set nCTEQ15[15] was used for target PDFs.

To parameterize PDFs of  $\pi^-$ , assume at the initial scale  $Q_0^2 = 1.9 \text{ GeV}^2$  charge symmetry:  $d = \bar{u}$ , and  $SU(3)$ -symmetric sea:  $u = \bar{d} = s = \bar{s}$ .

$$\begin{aligned} v &:= (d - \bar{d}) - (u - \bar{u}), & xv(x) &= A_v x^{B_v} (1-x)^{C_v} (1 + D_v x^{\frac{5}{2}}), \\ S &:= 2u + 2\bar{d} + s + \bar{s} = 6u, & xs(x) &= A_S x^{B_S} (1-x)^{C_S}, \\ g &:= g, & xg(x) &= A_g x^{B_g} (1-x)^{C_g}. \end{aligned}$$

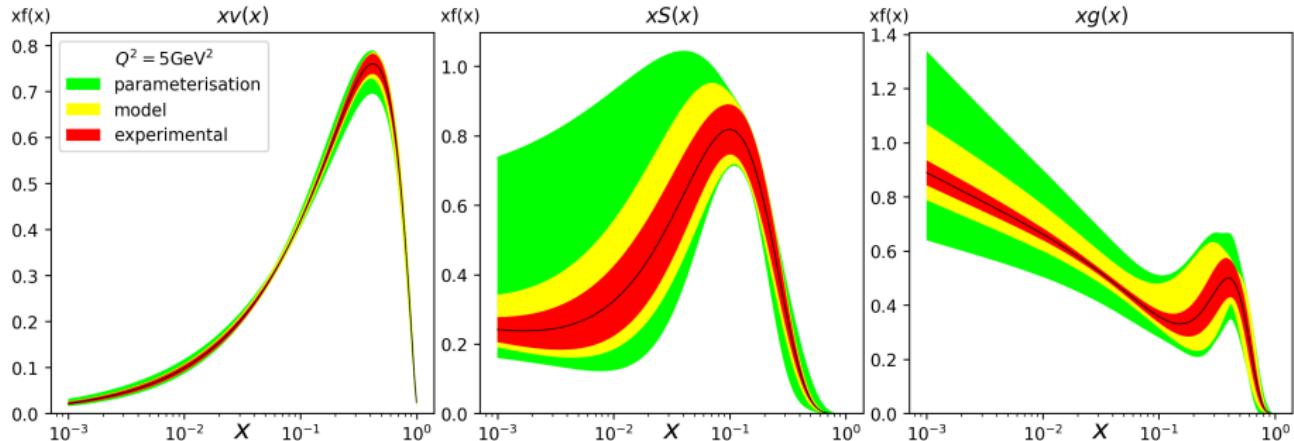
The  $A_v$  and  $A_g$  parameters are determined by the sum rules:

$$\int_0^1 v(x) dx = 2, \quad \int_0^1 x(v(x) + S(x) + g(x)) dx = 1.$$

Initial fits failed to determine all sea and gluon parameters simultaneously, so we fixed  $C_s = 8$ ,  $C_g = 5$ .

# Extracted pion PDFs

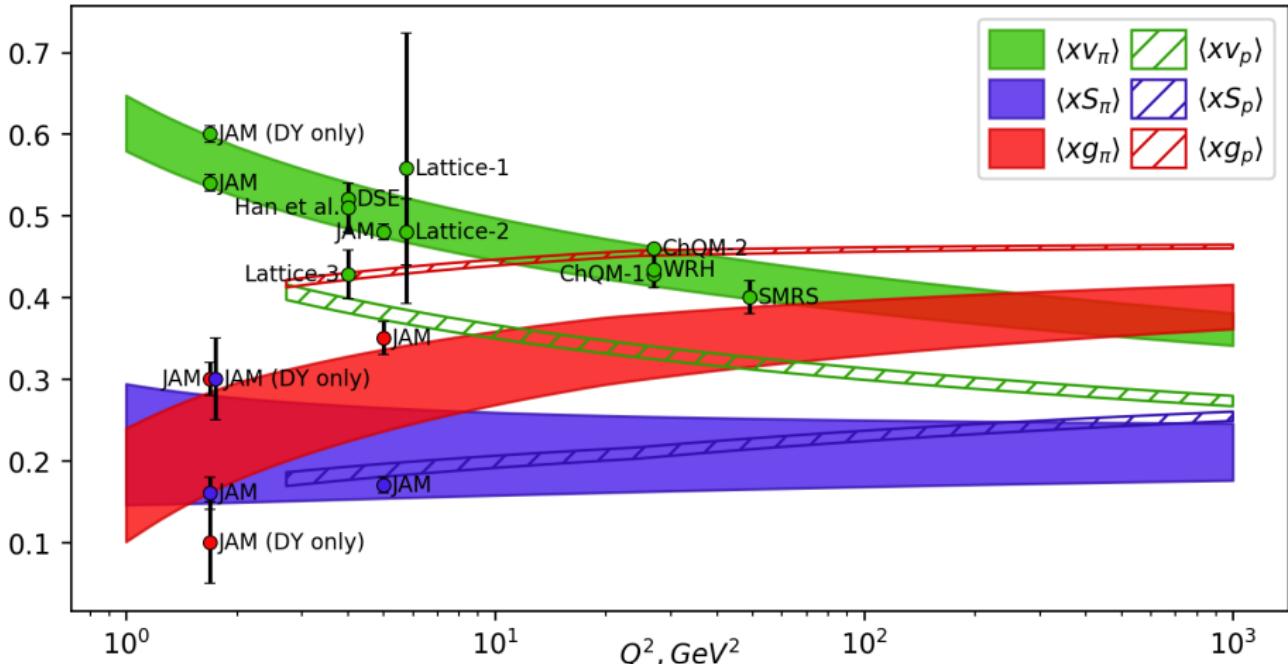
15



$$\frac{\chi^2}{N_{\text{DoF}}} = \frac{474}{373} = 1.27$$

# Momentum fractions as a function of $Q^2$

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We evaluate fractions of pion's momentum carried by valence quarks, sea quarks, and gluon, as a function of factorization scale  $Q^2$ , and compare them to predictions of theoretical models, results of lattice QCD calculations, and results of fits by other groups (See legend in backup section)

New bugfix release xFitter 2.0.1 “OldFashioned”, available on  
<https://xfitter.org>

Overview of improvements in xFitter 2.2 (unreleased, experimental)

- ▶ New flexible and modular fit architecture
  - ▶ Support for multiple PDFs in the same fit
  - ▶ Easy way to provide parameterisations as a formula in steering file
- ▶ Improved LHAPDF support, for both export and import
- ▶ Moving from Fortran NAMELIST-based steering to YAML
- ▶ Partial support of Ceres minimizer, as an alternative to MINUIT
- ▶ Changing build system from autotools to CMake

Available on gitlab:

<https://gitlab.cern.ch/fitters/xfitter/>

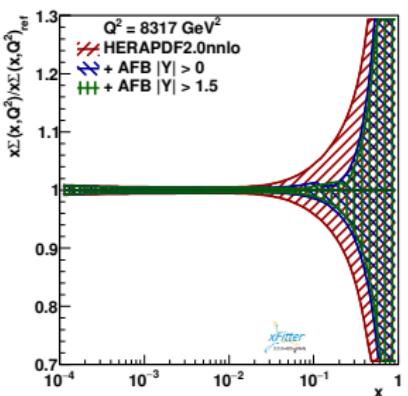
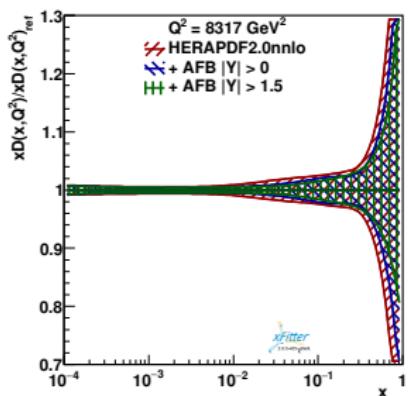
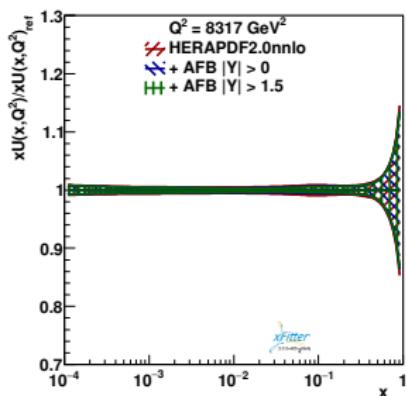
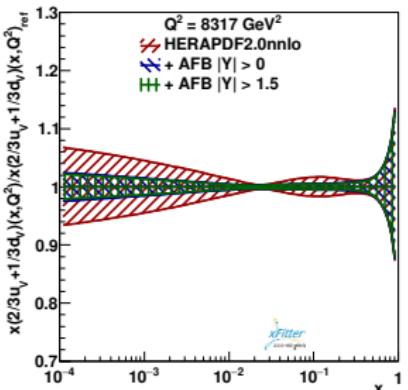
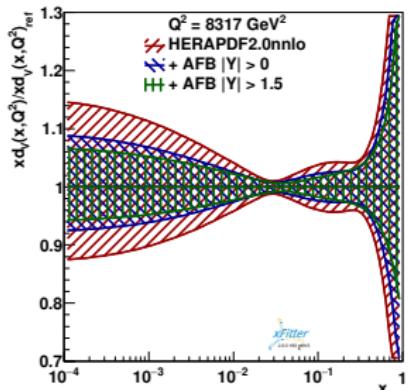
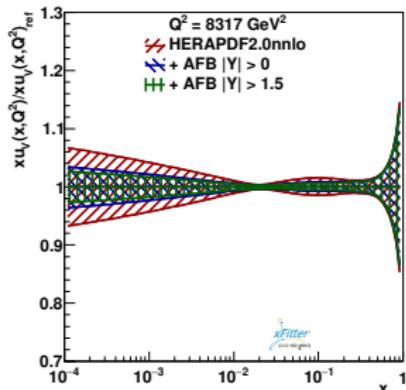
**Thank you for your attention!**

# Backup

Label	$\langle xv \rangle$	$\langle xS \rangle$	$\langle xg \rangle$	$Q^2$ (GeV $^2$ )
JAM[16]	$0.54 \pm 0.01$	$0.16 \pm 0.02$	$0.30 \pm 0.02$	1.69
JAM (DY)	$0.60 \pm 0.01$	$0.30 \pm 0.05$	$0.10 \pm 0.05$	1.69
this work	$0.58 \pm 0.04$	$0.21 \pm 0.07$	$0.21 \pm 0.07$	1.69
Lattice-3[17]	$0.428 \pm 0.030$			4
SMRS[18]	$0.40 \pm 0.02$			4
Han et al.[19]	$0.428 \pm 0.03$			4
DSE[20]	0.52			4
this work	$0.52 \pm 0.04$	$0.21 \pm 0.06$	$0.27 \pm 0.06$	4
JAM	$0.48 \pm 0.01$	$0.17 \pm 0.01$	$0.35 \pm 0.02$	5
this work	$0.51 \pm 0.04$	$0.21 \pm 0.06$	$0.28 \pm 0.06$	5
Lattice-1[21]	$0.558 \pm 0.166$			5.76
Lattice-2[22]	$0.48 \pm 0.04$			5.76
this work	$0.50 \pm 0.04$	$0.21 \pm 0.06$	$0.28 \pm 0.06$	5.76
WRH[23]	$0.434 \pm 0.022$			27
ChQM-1[24]	0.428			27
ChQM-2[25]	0.46			27
this work	$0.45 \pm 0.03$	$0.21 \pm 0.05$	$0.33 \pm 0.06$	27
SMRS[18]	$0.49 \pm 0.02$			49
this work	$0.43 \pm 0.03$	$0.21 \pm 0.05$	$0.35 \pm 0.04$	49

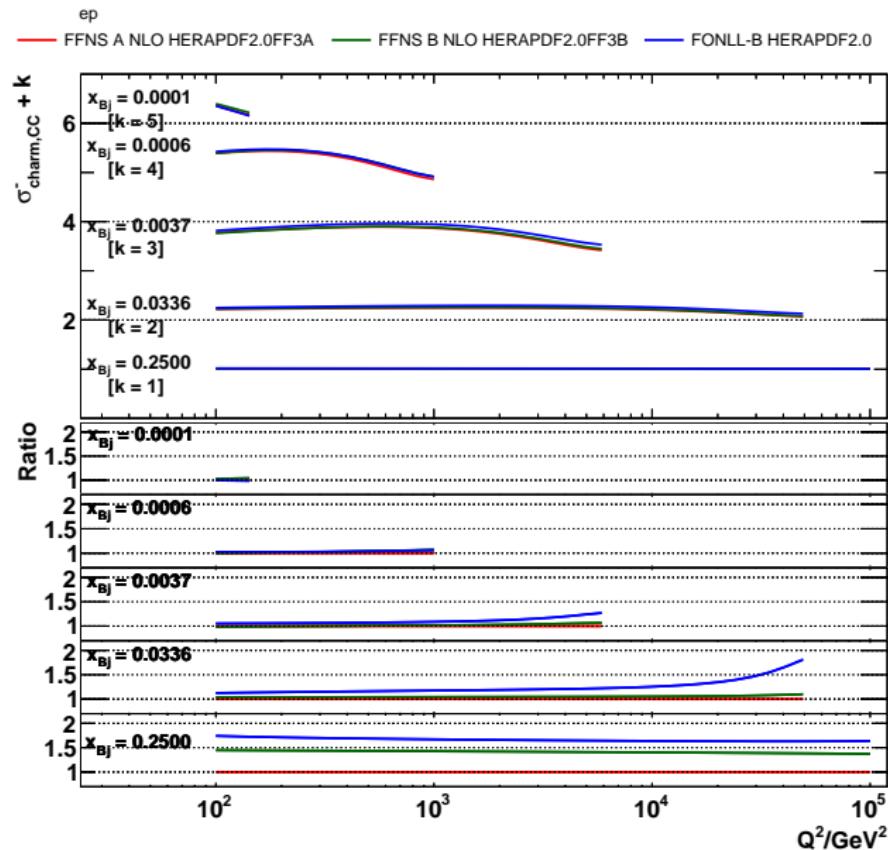
# AFB profiling with different rapidity cuts

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# Comparison of predictions of different schemes

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- [1] Sayipjamal Dulat, Tie-Jiun Hou, Jun Gao, Marco Guzzi, Joey Huston, Pavel Nadolsky, Jon Pumplin, Carl Schmidt, Daniel Stump, and C. P. Yuan.  
New parton distribution functions from a global analysis of quantum chromodynamics.  
*Phys. Rev.*, D93(3):033006, 2016.
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Parton distributions from high-precision collider data.  
*Eur. Phys. J.*, C77(10):663, 2017.
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Parton distribution functions,  $\alpha_s$ , and heavy-quark masses for LHC Run II.  
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Combination of measurements of inclusive deep inelastic  $e^\pm p$  scattering cross sections and QCD analysis of HERA data.  
*Eur. Phys. J.*, C75(12):580, 2015.

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Parton distributions in the LHC era: MMHT 2014 PDFs.  
*Eur. Phys. J.*, C75(5):204, 2015.
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*Eur. Phys. J.*, C66:503–524, 2010.
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aMCfast: automation of fast NLO computations for PDF fits.  
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Determination of Strange Sea Quark Distributions from Fixed-target and Collider Data.  
*Phys. Rev.*, D91(9):094002, 2015.
- [10] J. S. Conway et al.  
Experimental Study of Muon Pairs Produced by 252-GeV Pions on Tungsten.  
*Phys. Rev.*, D39:92–122, 1989.
- [11] B. Betev et al.  
Differential Cross-section of High Mass Muon Pairs Produced by a 194-GeV/ $c\pi^-$  Beam on a Tungsten Target.  
*Z. Phys.*, C28:9, 1985.  
Note that the original NA10 data have since been revised; updated data are published in [26].

- [12] M. Bonesini et al.  
High Transverse Momentum Prompt Photon Production by  $\pi^-$  and  $\pi^+$  on Protons at 280-GeV/c.  
*Z. Phys.*, C37:535, 1988.
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An Update on vector boson pair production at hadron colliders.  
*Phys. Rev.*, D60:113006, 1999.
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QCDNUM: Fast QCD Evolution and Convolution.  
*Comput. Phys. Commun.*, 182:490–532, 2011.
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nCTEQ15 - Global analysis of nuclear parton distributions with uncertainties in the CTEQ framework.  
*Phys. Rev.*, D93(8):085037, 2016.

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