

Colliders, Higgs and the strong interaction

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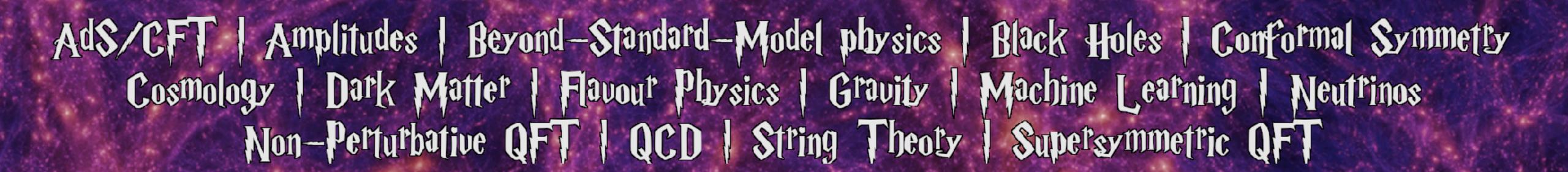
*on leave from CERN and CNRS





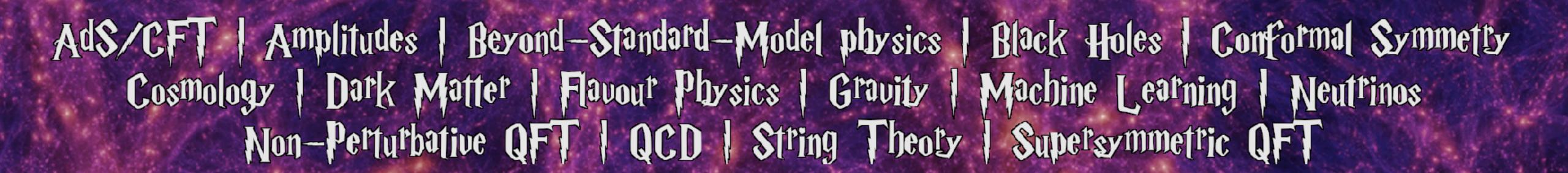






invitation for this talk:

"engage and inspire young researchers in [your] field, whilst also straddling the boundary of both Mathematics and Physics"



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Mission Impossible? (at least for me!)

a thread through this talk

what are our metrics for progress and/or success?

for progress on the big picture of particle physics and the more specific problems that we work on daily



I personally expect supersymmetry to be discovered at the LHC

-a Nobel prize-winning theorist [2008]

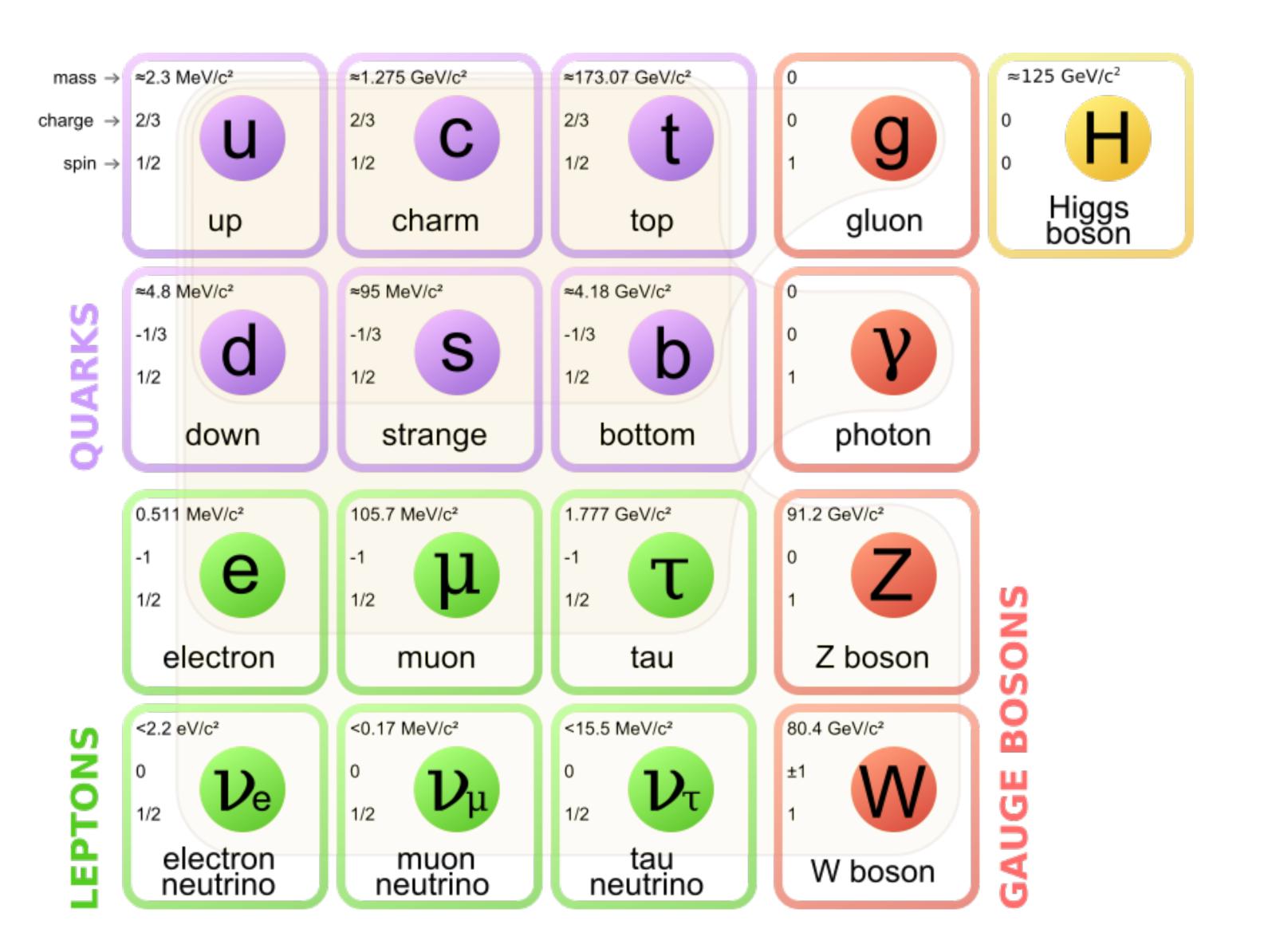
particle physics

"big unanswered questions" about fundamental particles & their interactions (dark matter, matter-antimatter asymmetry, nature of dark energy, hierarchy of scales...)

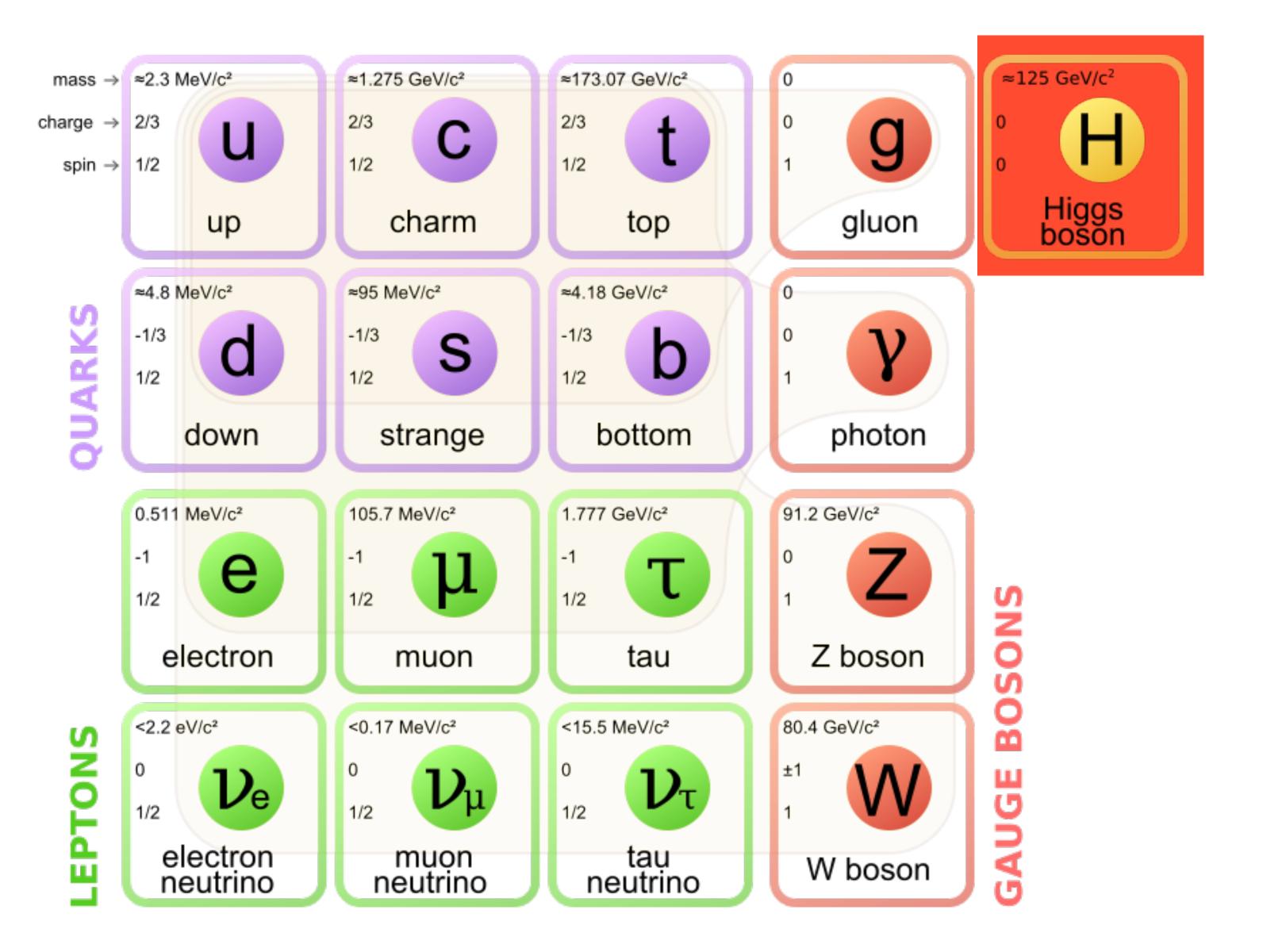
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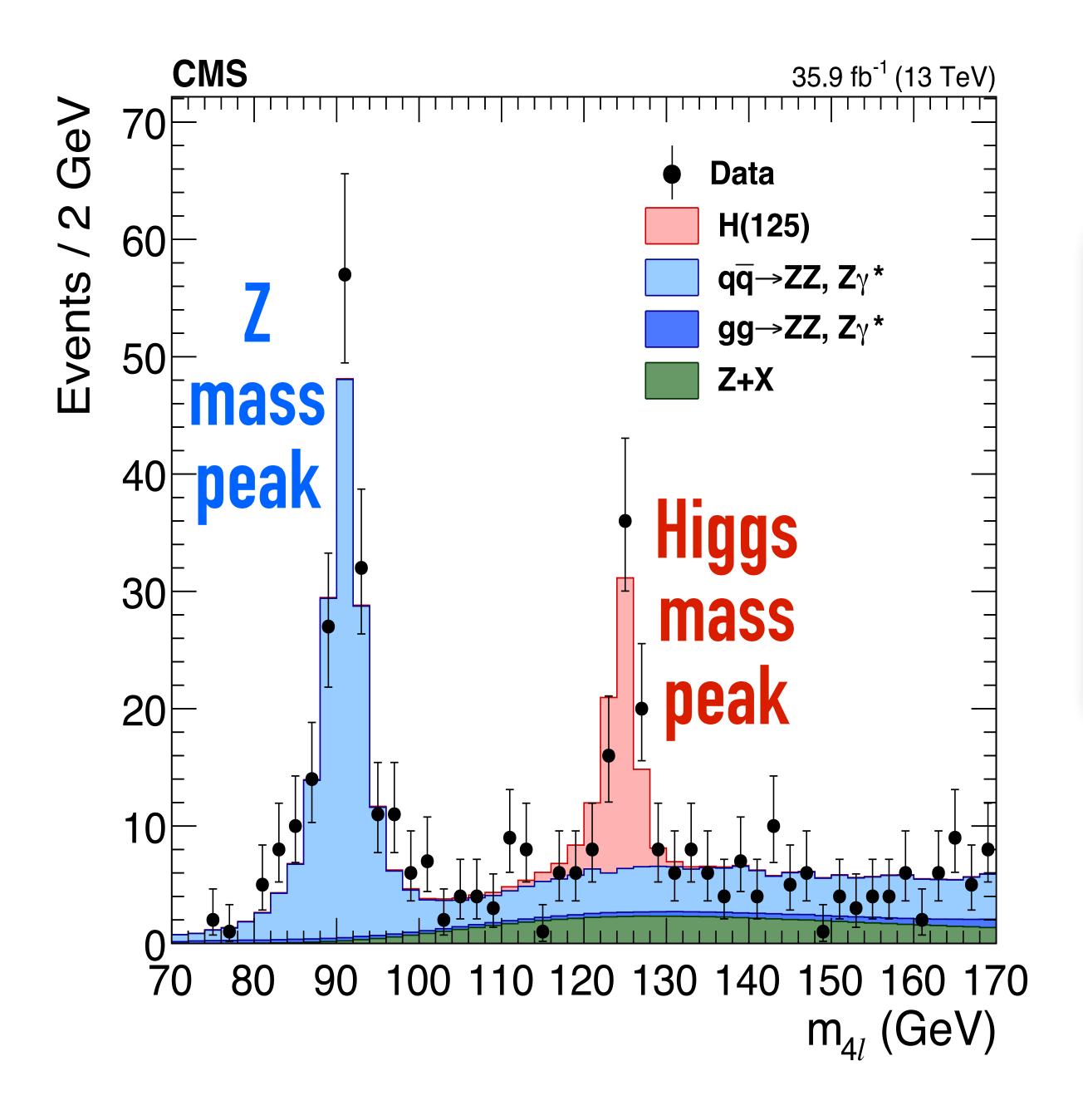
"big answerable questions"
and how we go about answering them
(nature of Higgs interactions, validity of SM up to high scales, lepton flavour universality, pattern of neutrino mixing, ...)

The Higgs boson



The Higgs boson



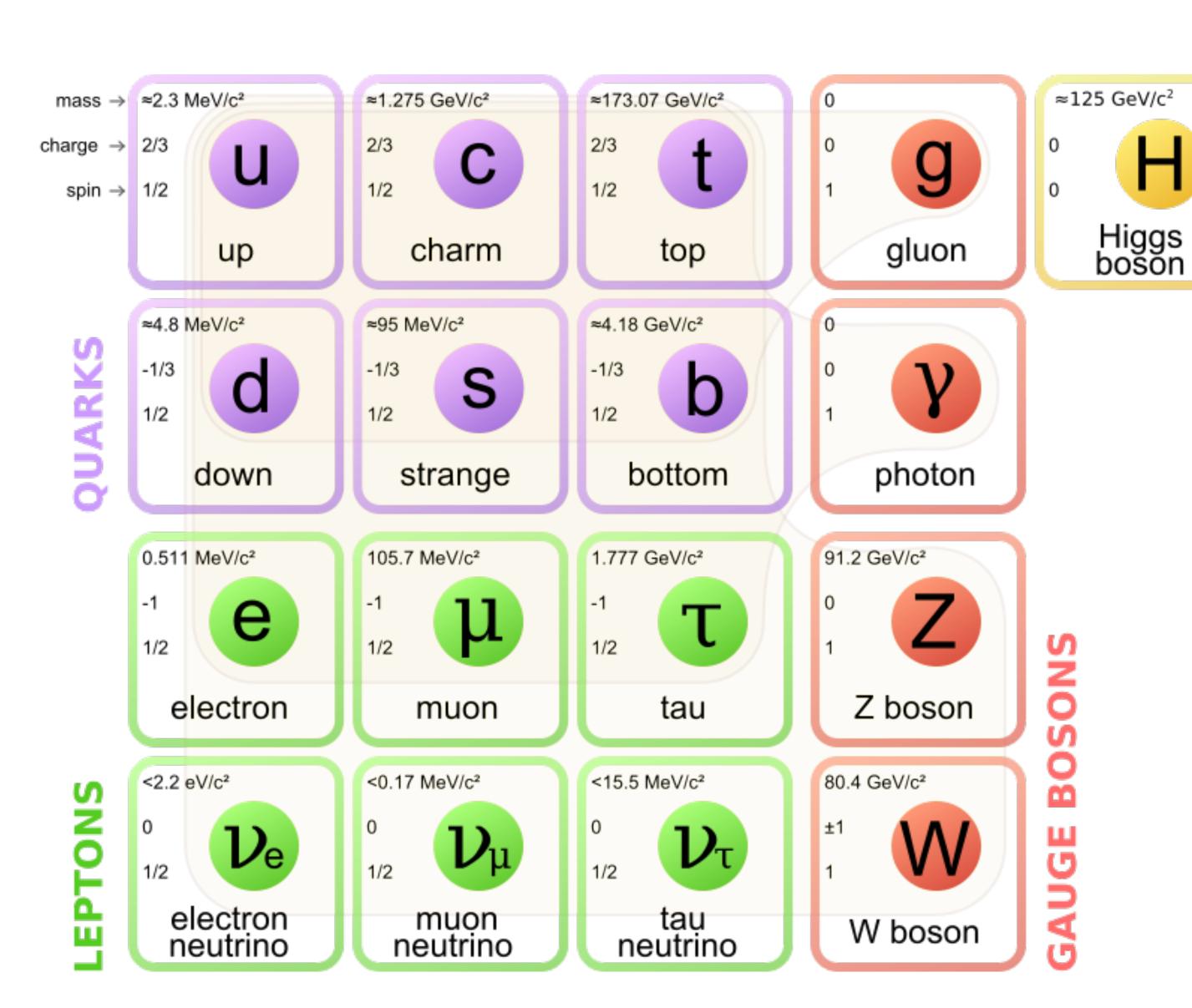


ATLAS and CMS collaborations at CERN's Large Hadron Collider (LHC):

2012 discovery of a Higgs-like boson

plot shows more recent data

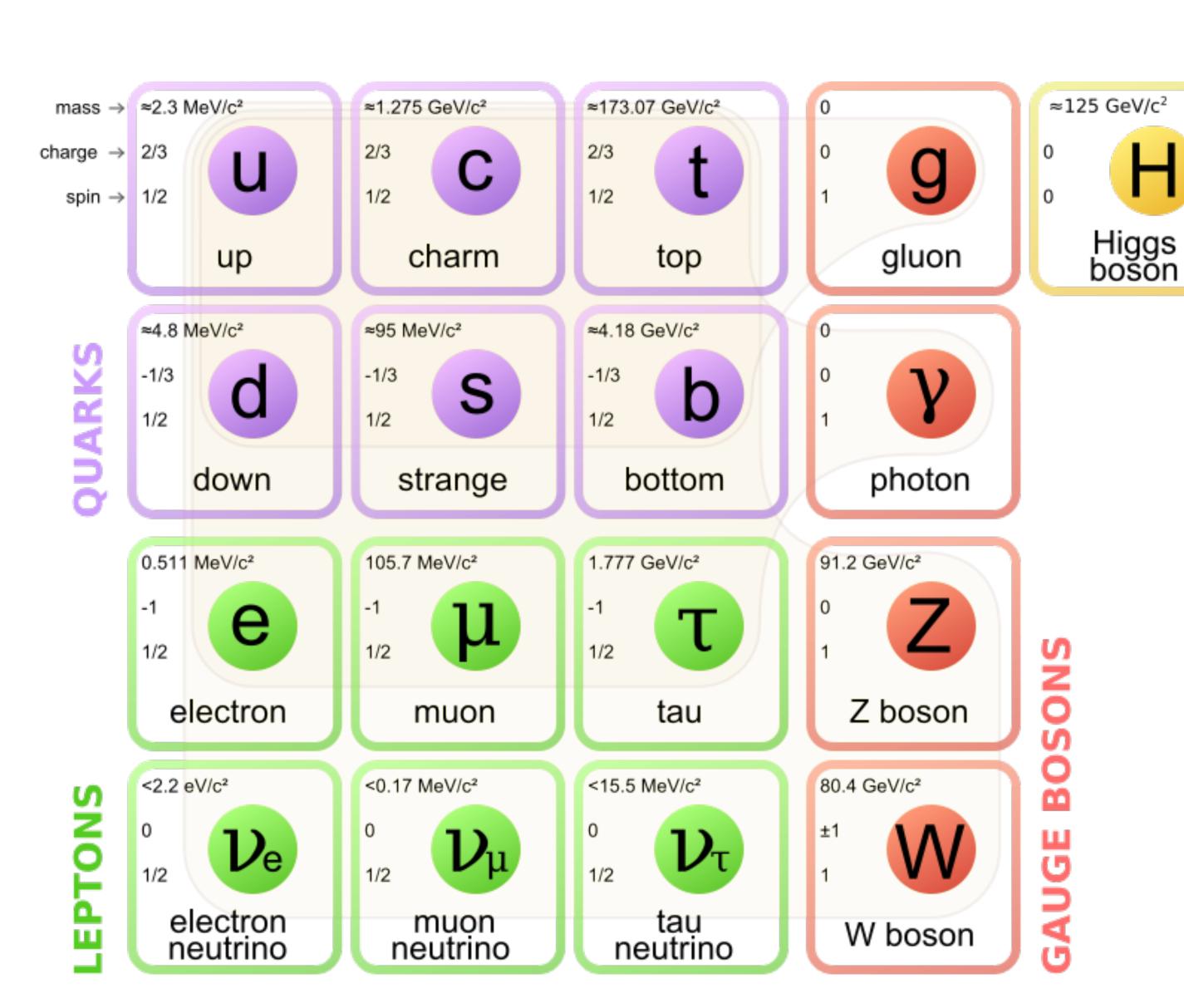
The Higgs boson (2012)



Success!

"The Standard Model is complete"

The Higgs boson (2012)



Success!

"The Standard Model is complete"

Crisis!

No supersymmetry, no extra dimensions, there's nothing left for us to do . . .

The New York Eimes

By DENNIS OVERBYE JUNE 19, 2017

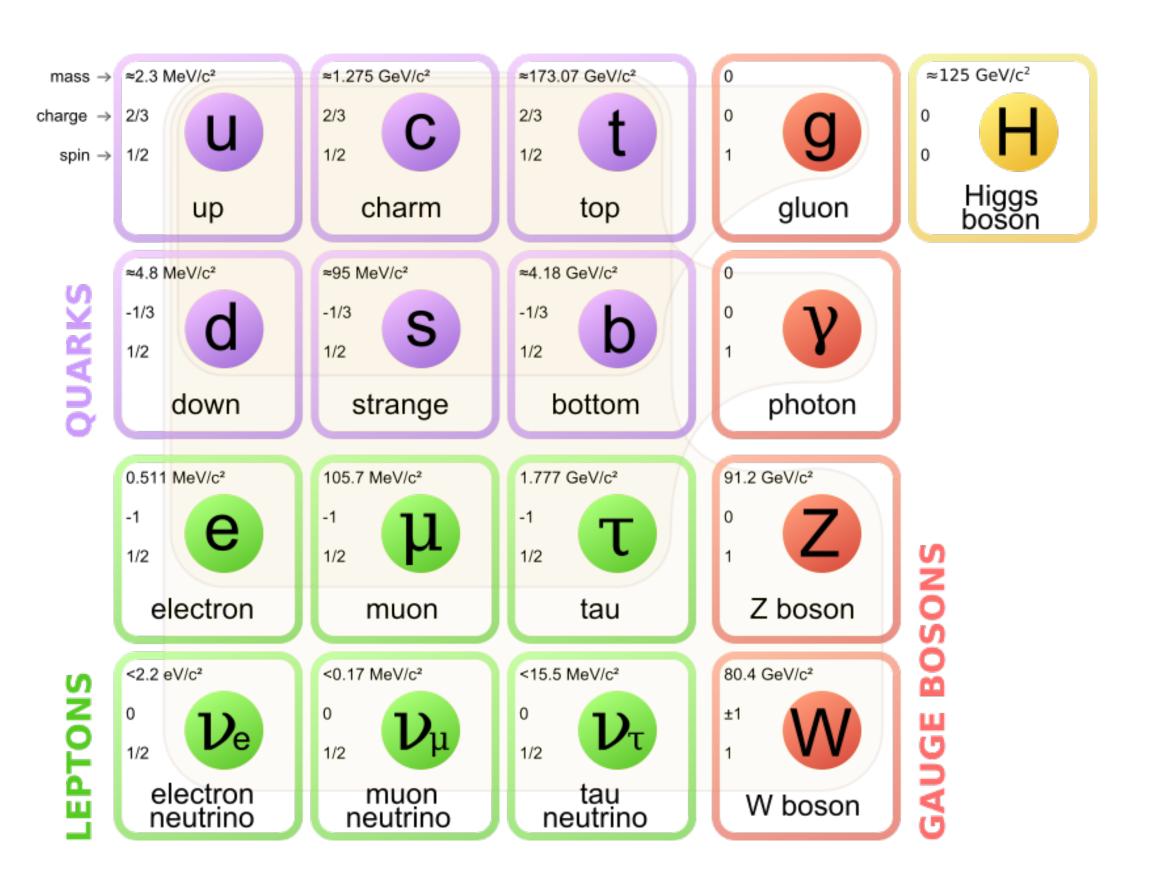
[...]

What if there is nothing new to discover? That prospect is now a cloud hanging over the physics community.

[...]

https://www.nytimes.com/2017/06/19/science/cern-large-hadron-collider-higgs-physics.html

what is the Standard Model?



particles

what is the Standard Model?



particles

interactions

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu}
+ i F N Y$$

$$+ Y: Y: Y: Y: Y: P + h.c.$$

$$+ |Q|^2 - V(\phi)$$

STANDARD MODEL — KNOWABLE UNKNOWNS

These T-shirts come with a little explanation

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu}
+ i F N Y$$

$$+ Y: Y: Y: Y: Y: P + h.c.$$

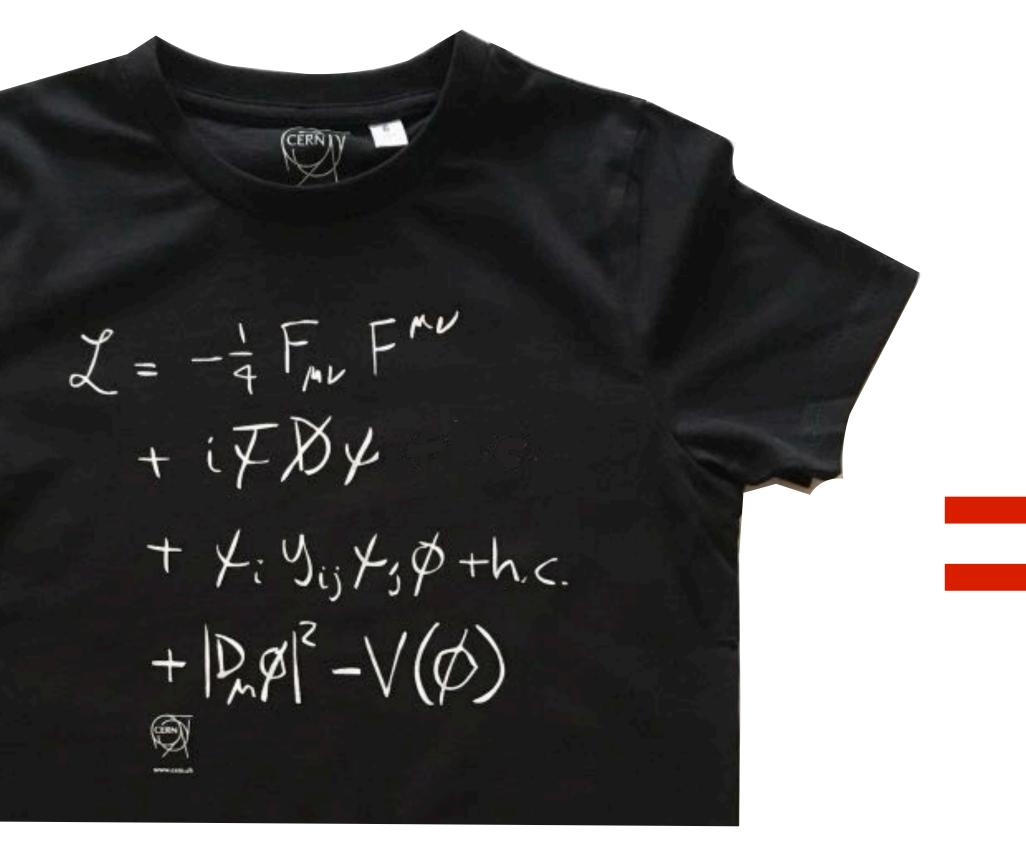
$$+ |D_{\mu}|^{2} - V(\phi)$$

STANDARD MODEL — KNOWABLE UNKNOWNS

These T-shirts come with a little explanation

"understanding" = knowledge?

"understanding" = assumption?



Standard Model Lagrangian (including neutrino mass terms)
From An Introduction to the Standard Model of Particle Physics, 2nd Edition,
W. N. Cottingham and D. A. Greenwood, Cambridge University Press, Cambridge, 2007,
Extracted by J.A. Shifflett, updated from Particle Data Group tables at pdg.lbl.gov, 2 Feb 2015.

$$\mathcal{L} = -\frac{1}{4}B_{\mu\nu}B^{\mu\nu} - \frac{1}{8}tr(\mathbf{W}_{\mu\nu}\mathbf{W}^{\mu\nu}) - \frac{1}{2}tr(\mathbf{G}_{\mu\nu}\mathbf{G}^{\mu\nu}) \qquad (U(1), SU(2) \text{ and } SU(3) \text{ gauge terms})$$

$$+(\bar{\nu}_L, \bar{e}_L)\,\tilde{\sigma}^{\mu}iD_{\mu}\begin{pmatrix} \nu_L \\ e_L \end{pmatrix} + \bar{e}_R\sigma^{\mu}iD_{\mu}e_R + \bar{\nu}_R\sigma^{\mu}iD_{\mu}\nu_R + \text{(h.c.)} \qquad (\text{lepton dynamical term})$$

$$-\frac{\sqrt{2}}{v}\left[(\bar{\nu}_L, \bar{e}_L)\,\phi M^e e_R + \bar{e}_R\bar{M}^e\bar{\phi}\begin{pmatrix} \nu_L \\ e_L \end{pmatrix}\right] \qquad (\text{electron, muon, tauon mass term})$$

$$-\frac{\sqrt{2}}{v}\left[(-\bar{e}_L, \bar{\nu}_L)\,\phi^*M^{\nu}\nu_R + \bar{\nu}_R\bar{M}^{\nu}\phi^T\begin{pmatrix} -e_L \\ \nu_L \end{pmatrix}\right] \qquad (\text{neutrino mass term})$$

$$+(\bar{u}_L, \bar{d}_L)\,\tilde{\sigma}^{\mu}iD_{\mu}\begin{pmatrix} u_L \\ d_L \end{pmatrix} + \bar{u}_R\sigma^{\mu}iD_{\mu}u_R + \bar{d}_R\sigma^{\mu}iD_{\mu}d_R + \text{(h.c.)} \qquad (\text{quark dynamical term})$$

$$-\frac{\sqrt{2}}{v}\left[(\bar{u}_L, \bar{d}_L)\,\phi M^d d_R + \bar{d}_R\bar{M}^d\bar{\phi}\begin{pmatrix} u_L \\ d_L \end{pmatrix}\right] \qquad (\text{down, strange, bottom mass term})$$

$$-\frac{\sqrt{2}}{v}\left[(-\bar{d}_L, \bar{u}_L)\,\phi^*M^u u_R + \bar{u}_R\bar{M}^u\phi^T\begin{pmatrix} -d_L \\ u_L \end{pmatrix}\right] \qquad (\text{up, charmed, top mass term})$$

$$+\overline{(D_{\mu}\phi)}D^{\mu}\phi - m_h^2[\bar{\phi}\phi - v^2/2]^2/2v^2. \qquad (\text{Higgs dynamical and mass term}) \qquad (1)$$

where (h.c.) means Hermitian conjugate of preceeding terms, $\bar{\psi} = (\text{h.c.})\psi = \psi^{\dagger} = \psi^{*T}$, and the derivative operators are

$$D_{\mu}\begin{pmatrix} \nu_{L} \\ e_{L} \end{pmatrix} = \left[\partial_{\mu} - \frac{ig_{1}}{2} B_{\mu} + \frac{ig_{2}}{2} \mathbf{W}_{\mu} \right] \begin{pmatrix} \nu_{L} \\ e_{L} \end{pmatrix}, \quad D_{\mu}\begin{pmatrix} u_{L} \\ d_{L} \end{pmatrix} = \left[\partial_{\mu} + \frac{ig_{1}}{6} B_{\mu} + \frac{ig_{2}}{2} \mathbf{W}_{\mu} + ig\mathbf{G}_{\mu} \right] \begin{pmatrix} u_{L} \\ d_{L} \end{pmatrix}, \tag{2}$$

$$D_{\mu}\nu_{R} = \partial_{\mu}\nu_{R}, \quad D_{\mu}e_{R} = \left[\partial_{\mu} - ig_{1}B_{\mu}\right]e_{R}, \quad D_{\mu}u_{R} = \left[\partial_{\mu} + \frac{i2g_{1}}{3}B_{\mu} + ig\mathbf{G}_{\mu}\right]u_{R}, \quad D_{\mu}d_{R} = \left[\partial_{\mu} - \frac{ig_{1}}{3}B_{\mu} + ig\mathbf{G}_{\mu}\right]d_{R}, \quad (3)$$

$$D_{\mu}\phi = \left[\partial_{\mu} + \frac{ig_1}{2}B_{\mu} + \frac{ig_2}{2}\mathbf{W}_{\mu}\right]\phi. \tag{4}$$

 ϕ is a 2-component complex Higgs field. Since \mathcal{L} is SU(2) gauge invariant, a gauge can be chosen so ϕ has the form

$$\phi^T = (0, v + h)/\sqrt{2}, \qquad \langle \phi \rangle_0^T = (\text{expectation value of } \phi) = (0, v)/\sqrt{2}, \qquad (5)$$

where v is a real constant such that $\mathcal{L}_{\phi} = \overline{(\partial_{\mu}\phi)}\partial^{\mu}\phi - m_{h}^{2}[\bar{\phi}\phi - v^{2}/2]^{2}/2v^{2}$ is minimized, and h is a residual Higgs field. B_{μ} , \mathbf{W}_{μ} and \mathbf{G}_{μ} are the gauge boson vector potentials, and \mathbf{W}_{μ} and \mathbf{G}_{μ} are composed of 2×2 and 3×3 traceless Hermitian matrices. Their associated field tensors are

 $B_{\mu\nu} = \partial_{\mu}B_{\nu} - \partial_{\nu}B_{\mu}, \quad \mathbf{W}_{\mu\nu} = \partial_{\mu}\mathbf{W}_{\nu} - \partial_{\nu}\mathbf{W}_{\mu} + ig_2(\mathbf{W}_{\mu}\mathbf{W}_{\nu} - \mathbf{W}_{\nu}\mathbf{W}_{\mu})/2, \quad \mathbf{G}_{\mu\nu} = \partial_{\mu}\mathbf{G}_{\nu} - \partial_{\nu}\mathbf{G}_{\mu} + ig(\mathbf{G}_{\mu}\mathbf{G}_{\nu} - \mathbf{G}_{\nu}\mathbf{G}_{\mu}). \quad (6)$ The non-matrix $A_{\mu}, Z_{\mu}, W_{\mu}^{\pm}$ bosons are mixtures of \mathbf{W}_{μ} and B_{μ} components, according to the weak mixing angle θ_{w} ,

$$A_{\mu} = W_{11\mu} sin\theta_w + B_{\mu} cos\theta_w, \qquad Z_{\mu} = W_{11\mu} cos\theta_w - B_{\mu} sin\theta_w, \qquad W_{\mu}^+ = W_{\mu}^{-*} = W_{12\mu} / \sqrt{2}, \qquad ($$

$$B_{\mu} = A_{\mu} cos\theta_{w} - Z_{\mu} sin\theta_{w}, \quad W_{11\mu} = -W_{22\mu} = A_{\mu} sin\theta_{w} + Z_{\mu} cos\theta_{w}, \quad W_{12\mu} = W_{21\mu}^{*} = \sqrt{2} W_{\mu}^{+}, \quad sin^{2}\theta_{w} = .2315(4). \quad (8)$$

The fermions include the leptons e_R, e_L, ν_R, ν_L and quarks u_R, u_L, d_R, d_L . They all have implicit 3-component generation indices, $e_i = (e, \mu, \tau), \ \nu_i = (\nu_e, \nu_\mu, \nu_\tau), \ u_i = (u, c, t), \ d_i = (d, s, b),$ which contract into the fermion mass matrices $M_{ip}^e, M_{ip}^u, M_{ip}^u, M_{ip}^d$, and implicit 2-component indices which contract into the Pauli matrices,

$$\sigma^{\mu} = \left[\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}, \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}, \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix}, \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \right], \quad \tilde{\sigma}^{\mu} = \left[\sigma^{0}, -\sigma^{1}, -\sigma^{2}, -\sigma^{3} \right], \quad tr(\sigma^{i}) = 0, \quad \sigma^{\mu\dagger} = \sigma^{\mu}, \quad tr(\sigma^{\mu}\sigma^{\nu}) = 2\delta^{\mu\nu}. \quad (9)$$

The quarks also have implicit 3-component color indices which contract into \mathbf{G}_{μ} . So \mathcal{L} really has implicit sums over 3-component generation indices, 2-component Pauli indices, 3-component color indices in the quark terms, and 2-component SU(2) indices in $(\bar{\nu}_L, \bar{e}_L), (\bar{u}_L, \bar{d}_L), (-\bar{e}_L, \bar{\nu}_L), (-\bar{d}_L, \bar{u}_L), \bar{\phi}, \mathbf{W}_{\mu}, \binom{\nu_L}{e_L}, \binom{u_L}{d_L}, \binom{-e_L}{\nu_L}, \binom{-d_L}{u_L}, \phi$.

The electroweak and strong coupling constants, Higgs vacuum expectation value (VEV), and Higgs mass are,

 $g_1 = e/\cos\theta_w, \quad g_2 = e/\sin\theta_w, \quad g > 6.5e = g(m_\tau^2), \quad v = 246GeV(PDG) \approx \sqrt{2} \cdot 180 \, GeV(CG), \quad m_h = 125.02(30) GeV \quad (10)$ where $e = \sqrt{4\pi\alpha\hbar c} = \sqrt{4\pi/137}$ in natural units. Using (4,5) and rewriting some things gives the mass of A_μ, Z_μ, W_μ^\pm ,

$$-\frac{1}{4}B_{\mu\nu}B^{\mu\nu} - \frac{1}{8}tr(\mathbf{W}_{\mu\nu}\mathbf{W}^{\mu\nu}) = -\frac{1}{4}A_{\mu\nu}A^{\mu\nu} - \frac{1}{4}Z_{\mu\nu}Z^{\mu\nu} - \frac{1}{2}\mathcal{W}_{\mu\nu}^{-}\mathcal{W}^{+\mu\nu} + \begin{pmatrix} \text{higher} \\ \text{order terms} \end{pmatrix}, \tag{1}$$

$$A_{\mu\nu} = \partial_{\mu}A_{\nu} - \partial_{\nu}A_{\mu}, \quad Z_{\mu\nu} = \partial_{\mu}Z_{\nu} - \partial_{\nu}Z_{\mu}, \quad \mathcal{W}^{\pm}_{\mu\nu} = D_{\mu}W^{\pm}_{\nu} - D_{\nu}W^{\pm}_{\mu}, \quad D_{\mu}W^{\pm}_{\nu} = [\partial_{\mu} \pm ieA_{\mu}]W^{\pm}_{\nu}, \quad (12)$$

$$D_{\mu} < \phi >_{0} = \frac{iv}{\sqrt{2}} \left(\frac{g_{2}W_{12\mu}/2}{g_{1}B_{\mu}/2 + g_{2}W_{22\mu}/2} \right) = \frac{ig_{2}v}{2} \left(\frac{W_{12\mu}/\sqrt{2}}{(B_{\mu}sin\theta_{w}/cos\theta_{w} + W_{22\mu})/\sqrt{2}} \right) = \frac{ig_{2}v}{2} \left(\frac{W_{\mu}^{+}}{-Z_{\mu}/\sqrt{2}\cos\theta_{w}} \right), \quad (13)$$

Ordinary 4-component Dirac fermions are composed of the left and right handed 2-component fields,

$$e = \begin{pmatrix} e_{L1} \\ e_{R1} \end{pmatrix}, \ \nu_e = \begin{pmatrix} \nu_{L1} \\ \nu_{R1} \end{pmatrix}, \ u = \begin{pmatrix} u_{L1} \\ u_{R1} \end{pmatrix}, \ d = \begin{pmatrix} d_{L1} \\ d_{R1} \end{pmatrix}, \ \text{(electron, electron neutrino, up and down quark)}$$
 (15)

$$\mu = \begin{pmatrix} e_{L2} \\ e_{R2} \end{pmatrix}, \ \nu_{\mu} = \begin{pmatrix} \nu_{L2} \\ \nu_{R2} \end{pmatrix}, \ c = \begin{pmatrix} u_{L2} \\ u_{R2} \end{pmatrix}, \ s = \begin{pmatrix} d_{L2} \\ d_{R2} \end{pmatrix}, \ \text{(muon, muon neutrino, charmed and strange quark)}$$
 (16)

$$\tau = \begin{pmatrix} e_{L3} \\ e_{R3} \end{pmatrix}, \ \nu_{\tau} = \begin{pmatrix} \nu_{L3} \\ \nu_{R3} \end{pmatrix}, \ t = \begin{pmatrix} u_{L3} \\ u_{R3} \end{pmatrix}, \ b = \begin{pmatrix} d_{L3} \\ d_{R3} \end{pmatrix}, \ \text{(tauon, tauon neutrino, top and bottom quark)}$$
 (17)

$$\gamma^{\mu} = \begin{pmatrix} 0 & 0' \\ \tilde{\sigma}^{\mu} & 0 \end{pmatrix} \qquad \text{where } \gamma^{\mu}\gamma^{\nu} + \gamma^{\nu}\gamma^{\mu} = 2Ig^{\mu\nu}. \quad \text{(Dirac gamma matrices in chiral representation)}$$
 (18)

The corresponding antiparticles are related to the particles according to $\psi^c = -i\gamma^2\psi^*$ or $\psi^c_L = -i\sigma^2\psi^*_R$, $\psi^c_R = i\sigma^2\psi^*_L$. The fermion charges are the coefficients of A_μ when (8,10) are substituted into either the left or right handed derivative operators (2-4). The fermion masses are the singular values of the 3×3 fermion mass matrices M^ν , M^e , M^u , M^d ,

$$M^{e} = \mathbf{U}_{L}^{e\dagger} \begin{pmatrix} m_{e} & 0 & 0 \\ 0 & m_{\mu} & 0 \\ 0 & 0 & m_{\tau} \end{pmatrix} \mathbf{U}_{R}^{e}, \quad M^{\nu} = \mathbf{U}_{L}^{\nu\dagger} \begin{pmatrix} m_{\nu_{e}} & 0 & 0 \\ 0 & m_{\nu_{\mu}} & 0 \\ 0 & 0 & m_{\nu_{\tau}} \end{pmatrix} \mathbf{U}_{R}^{\nu}, \quad M^{u} = \mathbf{U}_{L}^{u\dagger} \begin{pmatrix} m_{u} & 0 & 0 \\ 0 & m_{c} & 0 \\ 0 & 0 & m_{t} \end{pmatrix} \mathbf{U}_{R}^{u}, \quad M^{d} = \mathbf{U}_{L}^{d\dagger} \begin{pmatrix} m_{d} & 0 & 0 \\ 0 & m_{s} & 0 \\ 0 & 0 & m_{b} \end{pmatrix} \mathbf{U}_{R}^{d}, \quad (19)$$

$$m_e = .510998910(13)MeV, \quad m_{\nu_e} \sim .001 - 2eV, \qquad m_u = 1.7 - 3.1MeV, \qquad m_d = 4.1 - 5.7MeV,$$
 (20)

$$m_{\mu} = 105.658367(4) MeV, \quad m_{\nu_{\mu}} \sim .001 - 2 eV, \qquad \qquad m_{c} = 1.18 - 1.34 GeV, \qquad m_{s} = 80 - 130 MeV, \qquad (21)$$

$$m_{\tau} = 1776.84(17)MeV, \qquad m_{\nu_{\tau}} \sim .001 - 2eV, \qquad m_{t} = 171.4 - 174.4GeV, \quad m_{b} = 4.13 - 4.37GeV, \quad (22)$$

where the Us are 3×3 unitary matrices ($\mathbf{U}^{-1}=\mathbf{U}^{\dagger}$). Consequently the "true fermions" with definite masses are actually linear combinations of those in \mathcal{L} , or conversely the fermions in \mathcal{L} are linear combinations of the true fermions,

$$\begin{aligned} e'_L &= \mathbf{U}^e_L e_L, & e'_R &= \mathbf{U}^e_R e_R, & \nu'_L &= \mathbf{U}^\nu_L \nu_L, & \nu'_R &= \mathbf{U}^\nu_R \nu_R, & u'_L &= \mathbf{U}^u_L u_L, & u'_R &= \mathbf{U}^u_R u_R, & d'_L &= \mathbf{U}^d_L d_L, & d'_R &= \mathbf{U}^d_R d_R, & (23) \\ e_L &= \mathbf{U}^{e\dagger}_L e'_L, & e_R &= \mathbf{U}^{e\dagger}_R e'_R, & \nu_L &= \mathbf{U}^{\nu\dagger}_L \nu'_L, & \nu_R &= \mathbf{U}^{\nu\dagger}_R \nu'_R, & u_L &= \mathbf{U}^{u\dagger}_L u'_L, & u_R &= \mathbf{U}^{u\dagger}_R u'_R, & d_L &= \mathbf{U}^{d\dagger}_L d'_L, & d_R &= \mathbf{U}^{d\dagger}_R d'_R. & (24) \end{aligned}$$

When \mathcal{L} is written in terms of the true fermions, the Us fall out except in $\bar{u}_L' \mathbf{U}_L^u \tilde{\sigma}^\mu W_\mu^\pm \mathbf{U}_L^{d\dagger} d_L'$ and $\bar{\nu}_L' \mathbf{U}_L^\nu \tilde{\sigma}^\mu W_\mu^\pm \mathbf{U}_L^{e\dagger} e_L'$. Because of this, and some absorption of constants into the fermion fields, all the parameters in the Us are contained in only four components of the Cabibbo-Kobayashi-Maskawa matrix $\mathbf{V}^q = \mathbf{U}_L^u \mathbf{U}_L^{d\dagger}$ and four components of the Pontecorvo-Maki-Nakagawa-Sakata matrix $\mathbf{V}^l = \mathbf{U}_L^\nu \mathbf{U}_L^{e\dagger}$. The unitary matrices \mathbf{V}^q and \mathbf{V}^l are often parameterized as

$$\mathbf{V} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} e^{-i\delta/2} & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & e^{i\delta/2} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13} \\ 0 & 1 & 0 \\ -s_{13} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} e^{i\delta/2} & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & e^{-i\delta/2} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}, \quad c_{j} = \sqrt{1 - s_{j}^{2}}, \quad (25)$$

$$\delta^{q} = 69(4) \deg, \quad s_{12}^{q} = 0.2253(7), \quad s_{23}^{q} = 0.041(1), \quad s_{13}^{q} = 0.0035(2), \quad (26)$$

 $\delta^l = ?,$ $s^l_{12} = 0.560(16),$ $s^l_{23} = 0.7(1),$ $s^l_{13} = 0.153(28).$

 \mathcal{L} is invariant under a $U(1) \otimes SU(2)$ gauge transformation with $U^{-1} = U^{\dagger}$, detU = 1, θ real,

$$\mathbf{W}_{\mu} \to U \mathbf{W}_{\mu} U^{\dagger} - (2i/g_2) U \partial_{\mu} U^{\dagger}, \quad \mathbf{W}_{\mu\nu} \to U \mathbf{W}_{\mu\nu} U^{\dagger}, \quad B_{\mu} \to B_{\mu} + (2/g_1) \partial_{\mu} \theta, \quad B_{\mu\nu} \to B_{\mu\nu}, \quad \phi \to e^{-i\theta} U \phi, \tag{28}$$

$$\begin{pmatrix} \nu_L \\ e_L \end{pmatrix} \to e^{i\theta} U \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}, \quad \begin{pmatrix} u_L \\ d_L \end{pmatrix} \to e^{-i\theta/3} U \begin{pmatrix} u_L \\ d_L \end{pmatrix}, \quad \begin{matrix} \nu_R \to \nu_R, & u_R \to e^{-4i\theta/3} u_R, \\ e_R \to e^{2i\theta} e_R, & d_R \to e^{2i\theta/3} d_R, \end{matrix}$$
(2)

and under an SU(3) gauge transformation with $V^{-1} = V^{\dagger}, \ det V = 1,$

$$\mathbf{G}_{\mu} \to V \mathbf{G}_{\mu} V^{\dagger} - (i/g) V \partial_{\mu} V^{\dagger}, \quad \mathbf{G}_{\mu\nu} \to V \mathbf{G}_{\mu\nu} V^{\dagger}, \quad u_L \to V u_L, \quad d_L \to V d_L, \quad u_R \to V u_R, \quad d_R \to V d_R. \tag{30}$$

http://einstein-schrodinger.com/Standard_Model.pdf

(27)

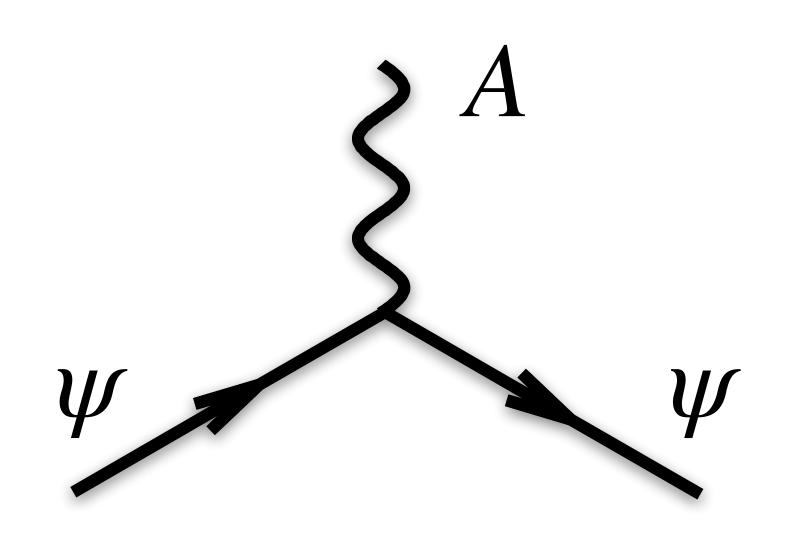
$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + F^{\mu$$

What does it mean?

Quantum formulation of Maxwell's equations, (and their analogues for the weak and strong forces).

What does it mean?

 $\psi = fermion (e.g. electron) field$ $D \sim eA(=photon field) + \cdots$



tells you there's an electron-photon interaction vertex

$$\mathcal{L} = -\frac{1}{4} F_{NN} F^{NN} + F^{N$$

What does it mean?

many experiments have probed these so-called "gauge" interactions (in classical form, they date back to 1860s)

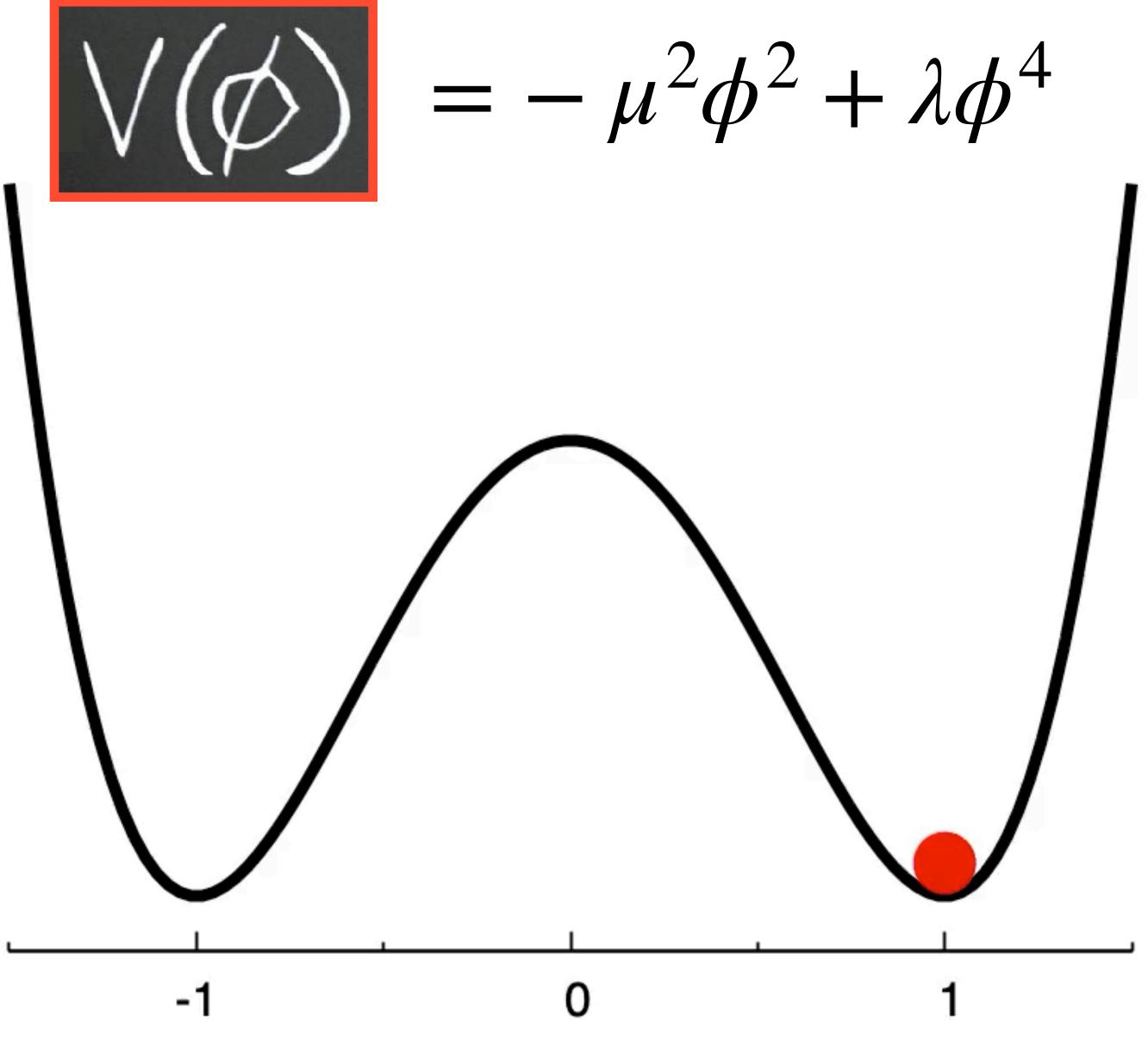
Describe electromagnetism, full electroweak theory & the strong force.

They work to high precision (best tests go up to 1 part in 108)

$$\mathcal{L} = -\frac{1}{4} F_{NN} F^{NN}
+ i F N Y$$
+ Y: Y: Y: Y: Y P + h.c.
$$+ | D_{N} P |^{2} - V(\Phi)$$

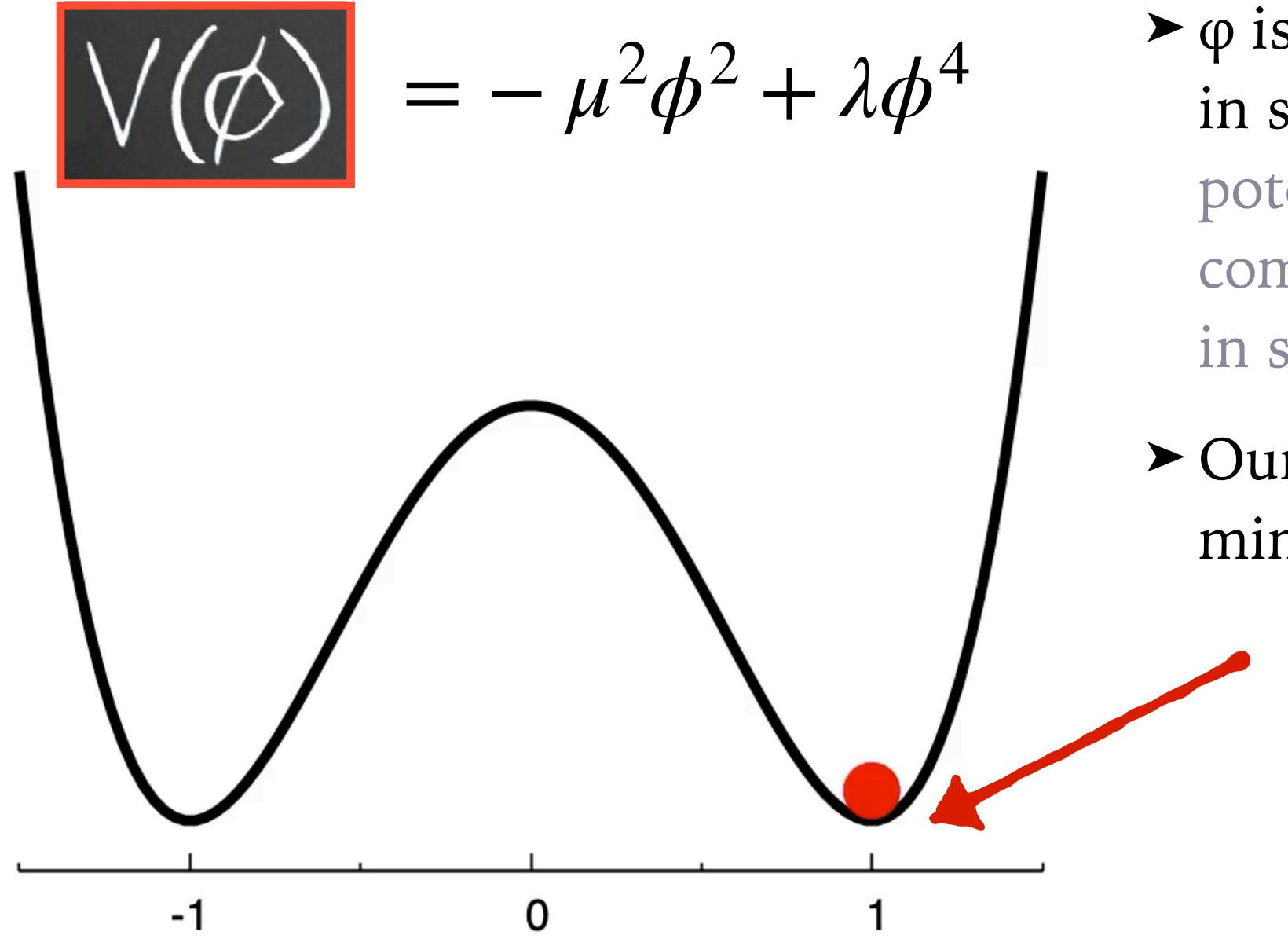
Higgs sector

until 7 years ago none of these terms had ever been directly observed.



Higgs field ϕ [units of vacuum expectation value, ϕ_0]

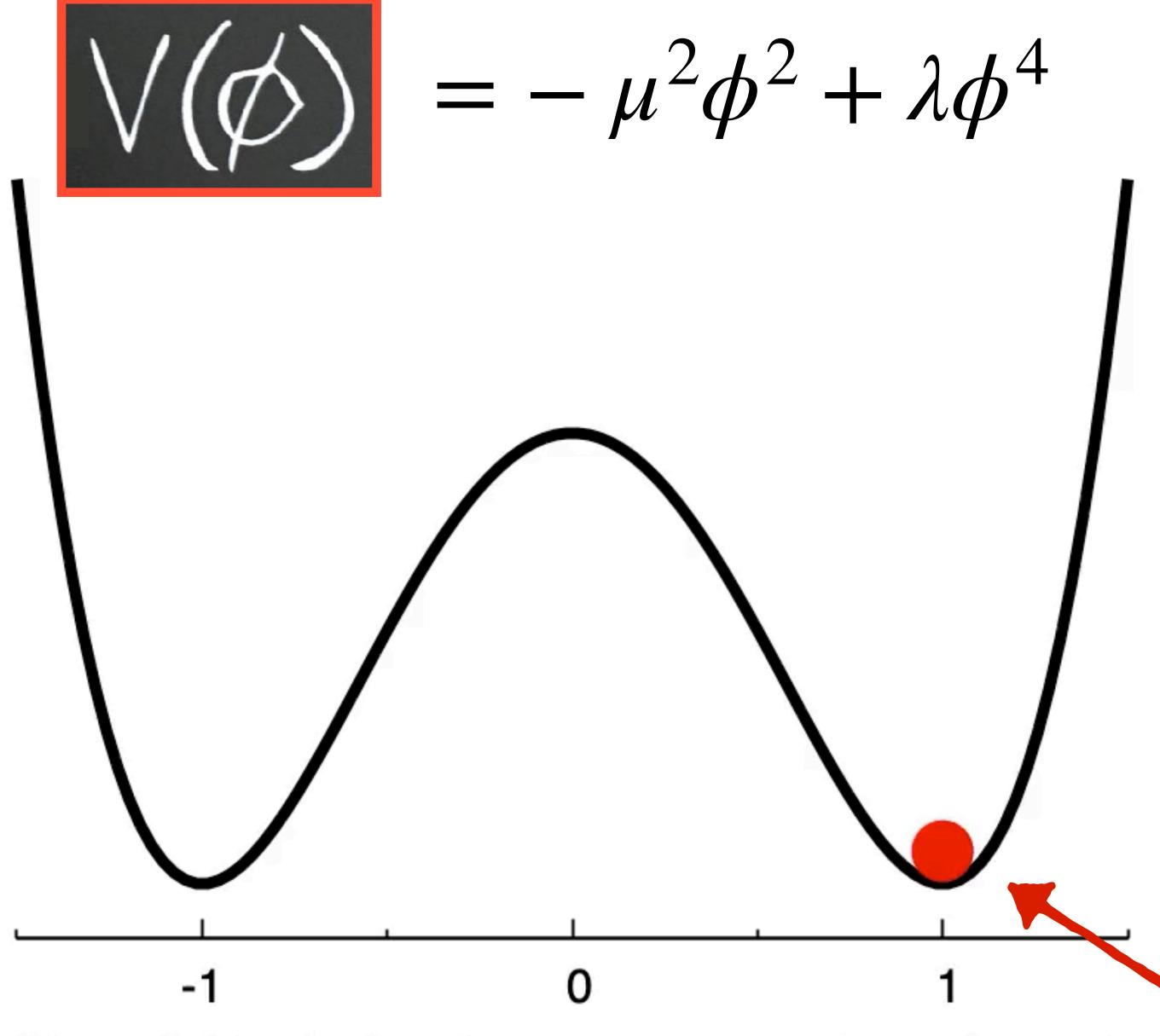
φ is a field at every point in space (plot shows potential vs. 1 of 4 components, at 1 point in space)



Higgs field ϕ [units of vacuum expectation value, ϕ_0]

- φ is a field at every point in space (plot shows potential vs. 1 of 4 components, at 1 point in space)
- > Our universe sits at minimum of $V(\phi)$, at

$$\phi = \phi_0 = \frac{\mu}{\sqrt{2\lambda}}$$



Higgs field ϕ [units of vacuum expectation value, ϕ_0]

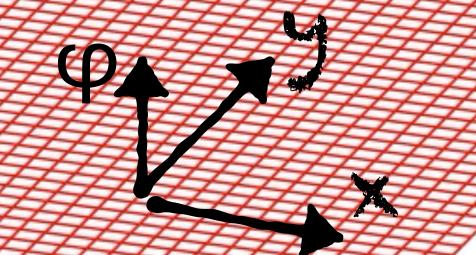
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- > Our universe sits at minimum of $V(\phi)$, at

$$\phi = \phi_0 = \frac{\mu}{\sqrt{2\lambda}}$$

Excitation of the φ field around φ_0 is a Higgs

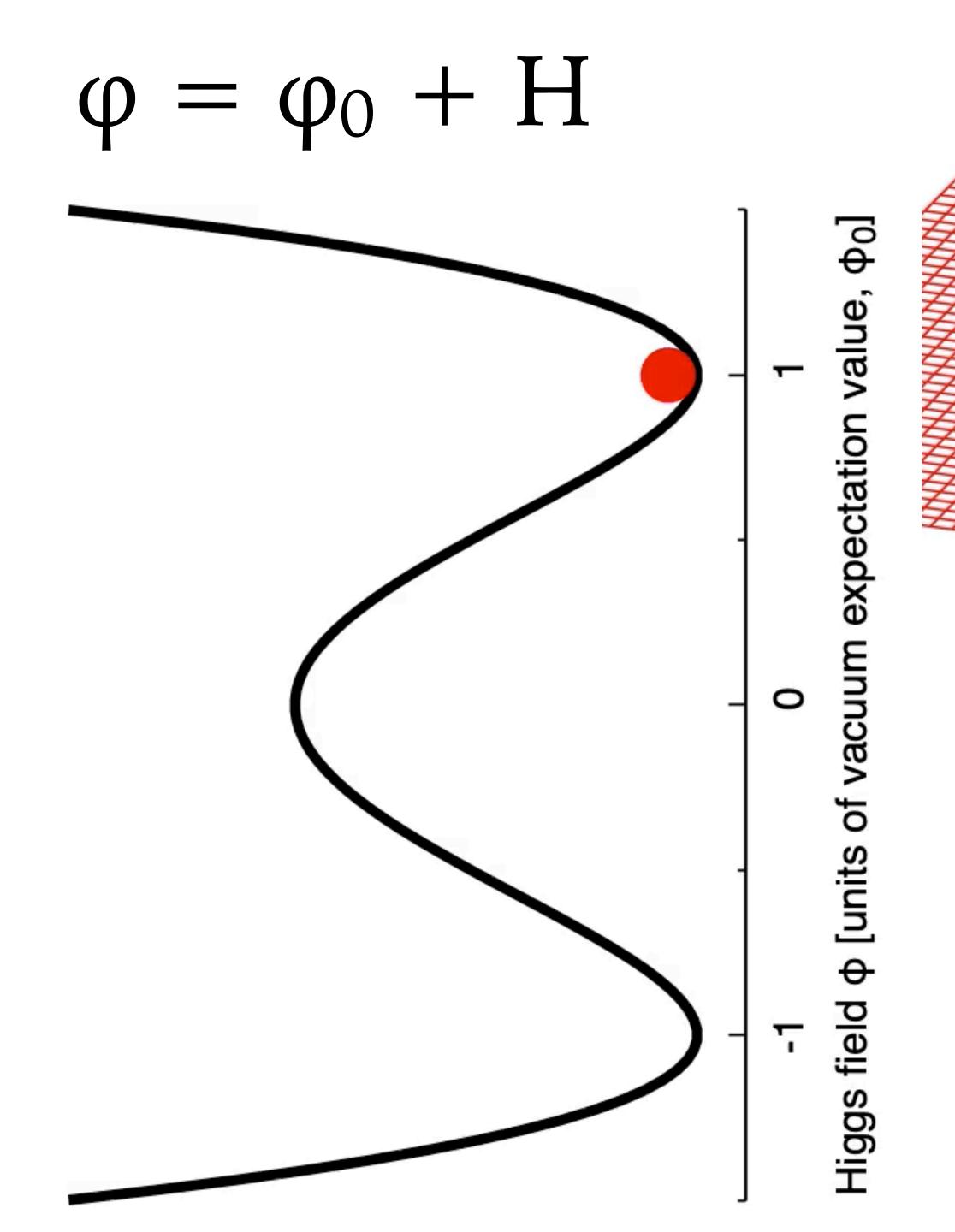
boson ($\varphi = \varphi_0 + H$)

Higgs boson

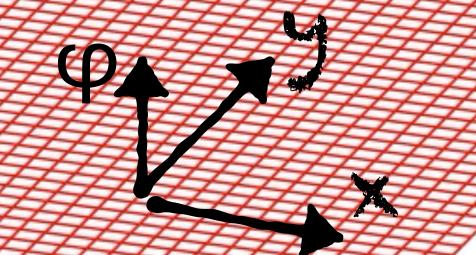


Higgs field can be different at each point in space

A Higgs boson at a given point in space is a localised fluctuation of the field

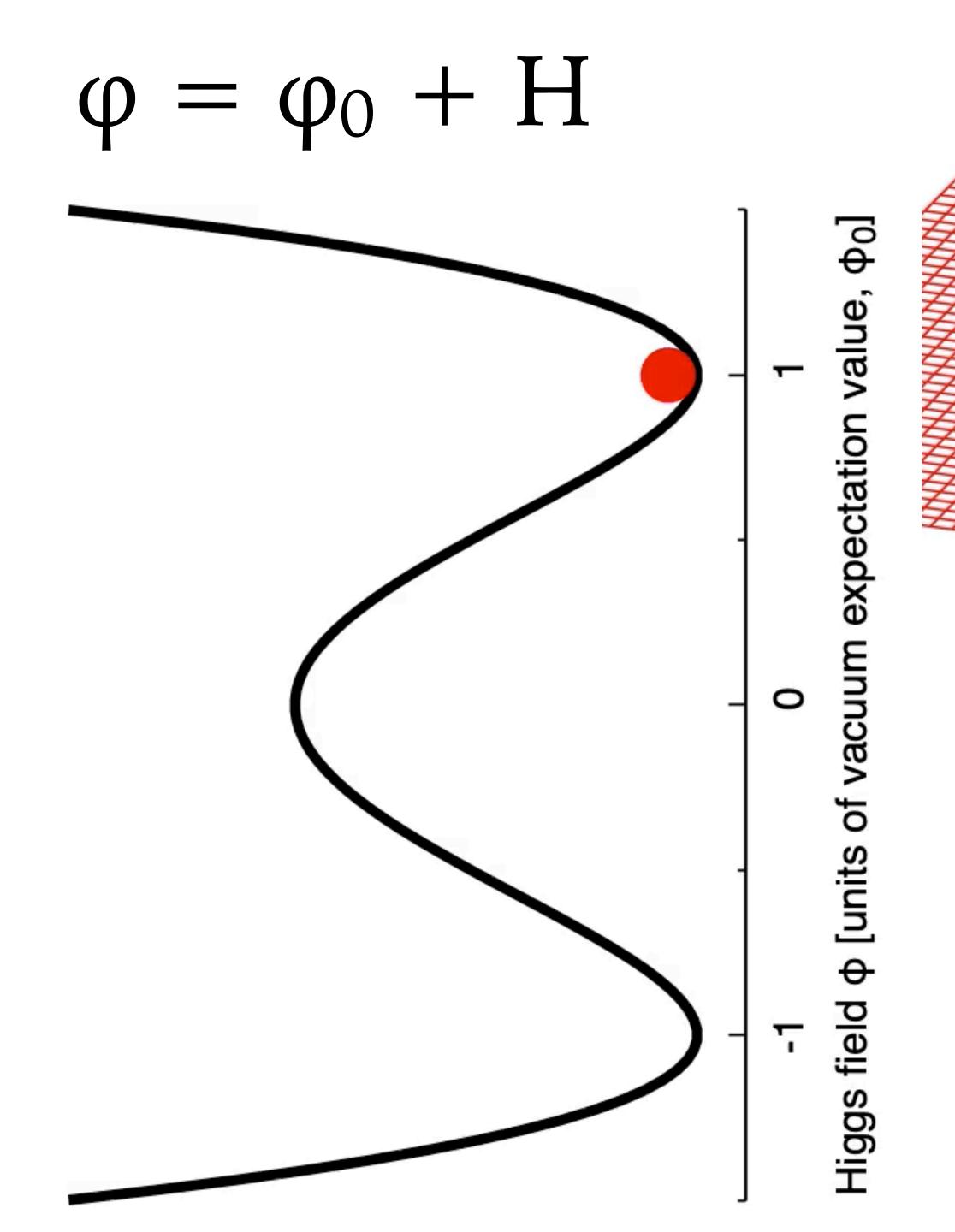


Higgs boson



Higgs field can be different at each point in space

A Higgs boson at a given point in space is a localised fluctuation of the field



 $\varphi = \varphi_0 + H$

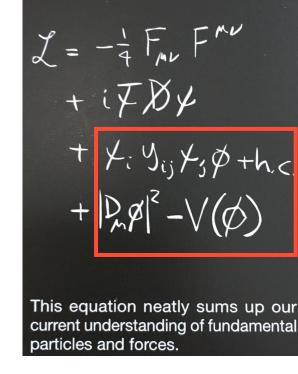
established (2012 Higgs boson discovery)

$$\phi = \phi_0 + H$$

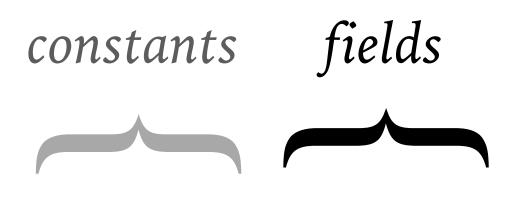
established (2012 Higgs boson discovery)

nypothesis

what terms are there in the Higgs sector? 2. Gauge-Higgs term

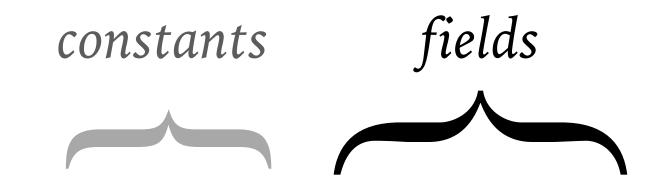








Z-boson mass term

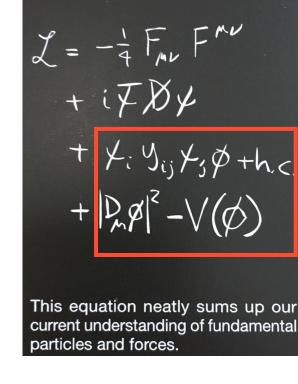


$$+ \ 2g^2\phi_0\,H\,Z_\mu Z^\mu$$

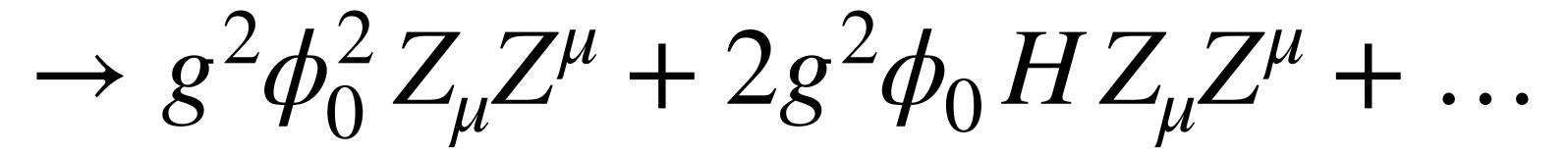
HZZ interaction term

$$[\phi^2 = (\phi_0 + H)^2 = \phi_0^2 + 2\phi_0 H + \dots]$$

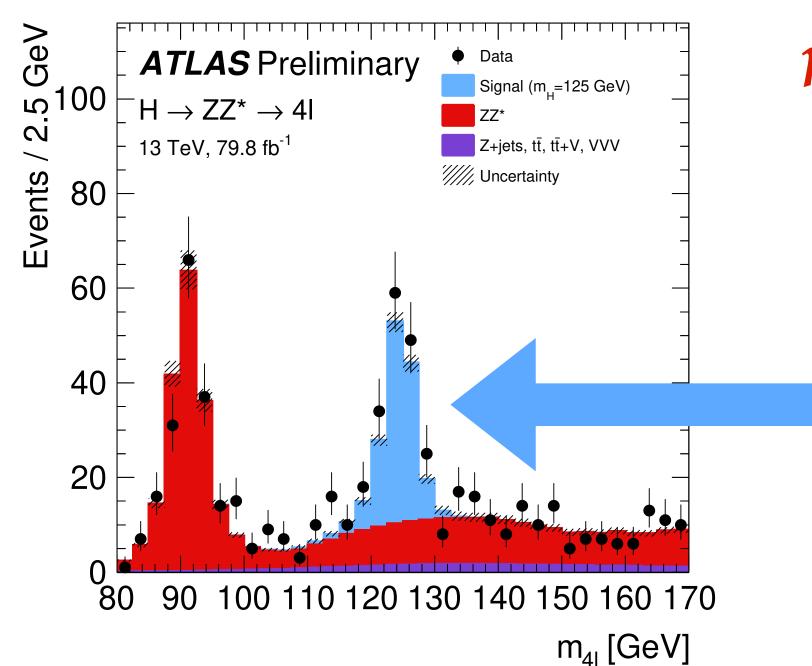
what terms are there in the Higgs sector? 2. Gauge-Higgs term

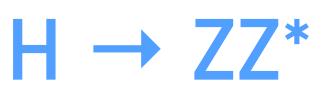






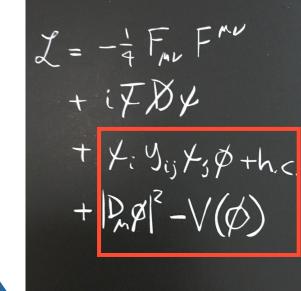
Z-boson mass term ZZH interaction term



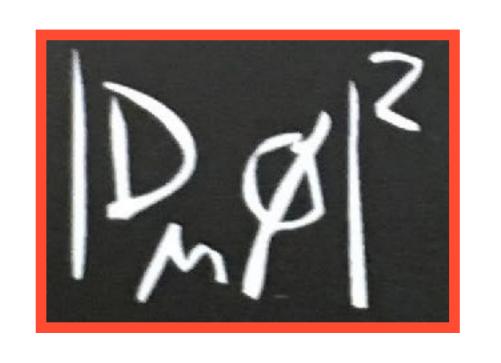


Higgs mechanism
predicts specific relation
between Z-boson mass
and HZZ interaction

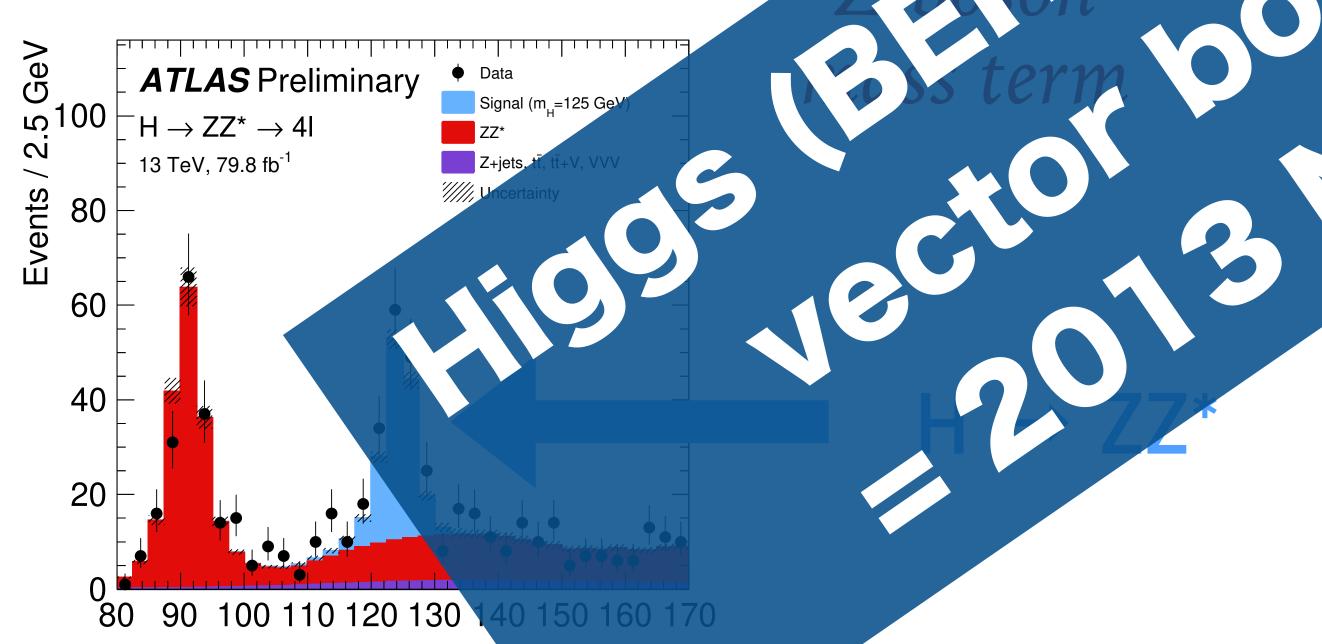
what terms are there in the Higgs sector? CO 2. Gauge-Higgs term



This equation neatly sums up of current understanding of fundamentarticles and forces.



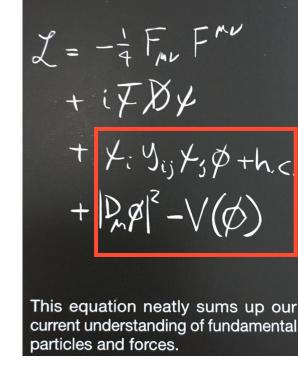


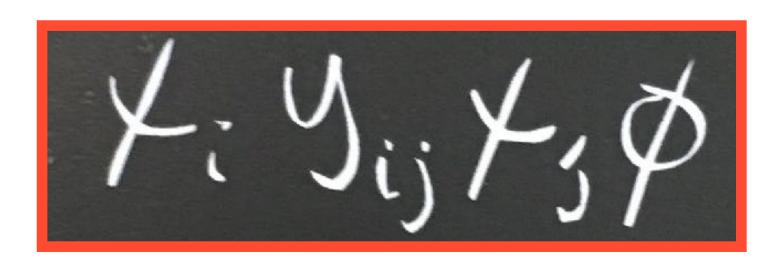


m₄₁ [GeV]

Higgs mechanism
predicts specific relation
between Z-boson mass
and HZZ interaction

what terms are there in the Higgs sector? 3. Fermion-Higgs (Yukawa) term





\rightarrow	y_{ij}	ϕ_0	ψ_i	ψ_j	+	y_{ij}	H	ψ_i	ψ_j
---------------	----------	----------	----------	----------	---	----------	---	----------	----------

i	Уi	i	Уi
u	$2 \cdot 10^{-5}$	d	$3 \cdot 10^{-5}$
С	$8 \cdot 10^{-3}$	S	$6 \cdot 10^{-4}$
b	$3 \cdot 10^{-2}$	t	1
$ u_{e}$		е	$3 \cdot 10^{-6}$
$ u_{\mu}$	$\sim 10^{-13}$	μ	$6 \cdot 10^{-4}$
$ \nu_{ au} $		τ	$1 \cdot 10^{-4}$

fermion

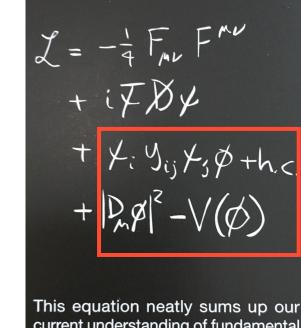
mass term $m_i = y_{ii}\phi_0$

Higgs-fermion-fermion interaction term; coupling ~ yii

$$\phi = \phi_0 + H$$

what terms are there in the Higgs sector?

3. Fermion-Higgs (Yukawa) term



4: Gij Ksp

o y_{ij} θ ψ_i ψ_i ψ_j H ψ_i ψ_j

i	Уi	i	Уi	
u	$2 \cdot 10^{-5}$	d	3 · 10	
С	$8 \cdot 10^{-3}$	S	$6 \cdot 10^{-4}$	
b	$3 \cdot 10^{-2}$	t	1	
$ u_e $		е	$3 \cdot 10^{-6}$	
$\mid \nu_{\mu} \mid$	$\sim 10^{-13}$	μ	$6 \cdot 10^{-4}$	
$ \nu_{ au} $		τ	$1 \cdot 10^{-4}$	

Higgs-fermion-fermion interaction term; coupling ~ yii

$$\phi = \phi_0 + H$$

Yukawa interaction hypothesis

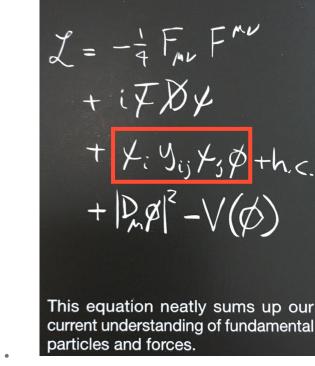
Yukawa couplings ~ fermion mass

first fundamental interaction that we probe at the quantum level where interaction strength (y_{ij}) not quantised

(i.e. no underlying unit of conserved charge across particles)

Why do Yukawa couplings matter?

(1) Because, within SM conjecture, they're what give masses to all quarks

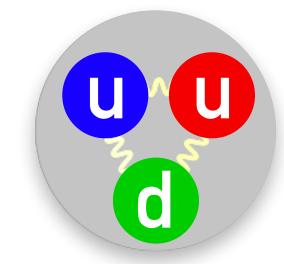


Up quarks (mass ~ 2.2 MeV) are lighter than down quarks (mass ~ 4.7 MeV)

proton (up+up+down):
$$2.2 + 2.2 + 4.7 + ... = 938.3 \text{ MeV}$$

neutron (up+down+down): $2.2 + 4.7 + 4.7 + ... = 939.6 \text{ MeV}$

proton mass = 938.3 MeV

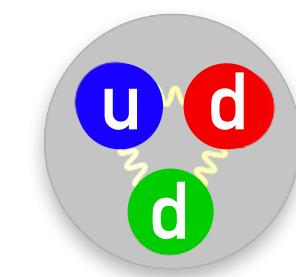


So protons are **lighter** than neutrons,

→ protons are stable.

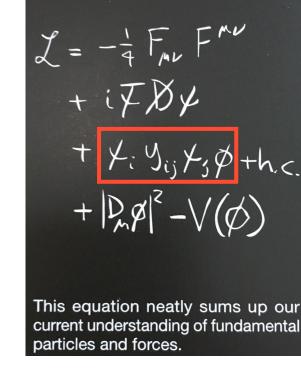
Which gives us the hydrogen atom, & chemistry and biology as we know it

neutron mass = 939.6 MeV



Why do Yukawa couplings matter?

(2) Because, within SM conjecture, they're what give masses to all leptons

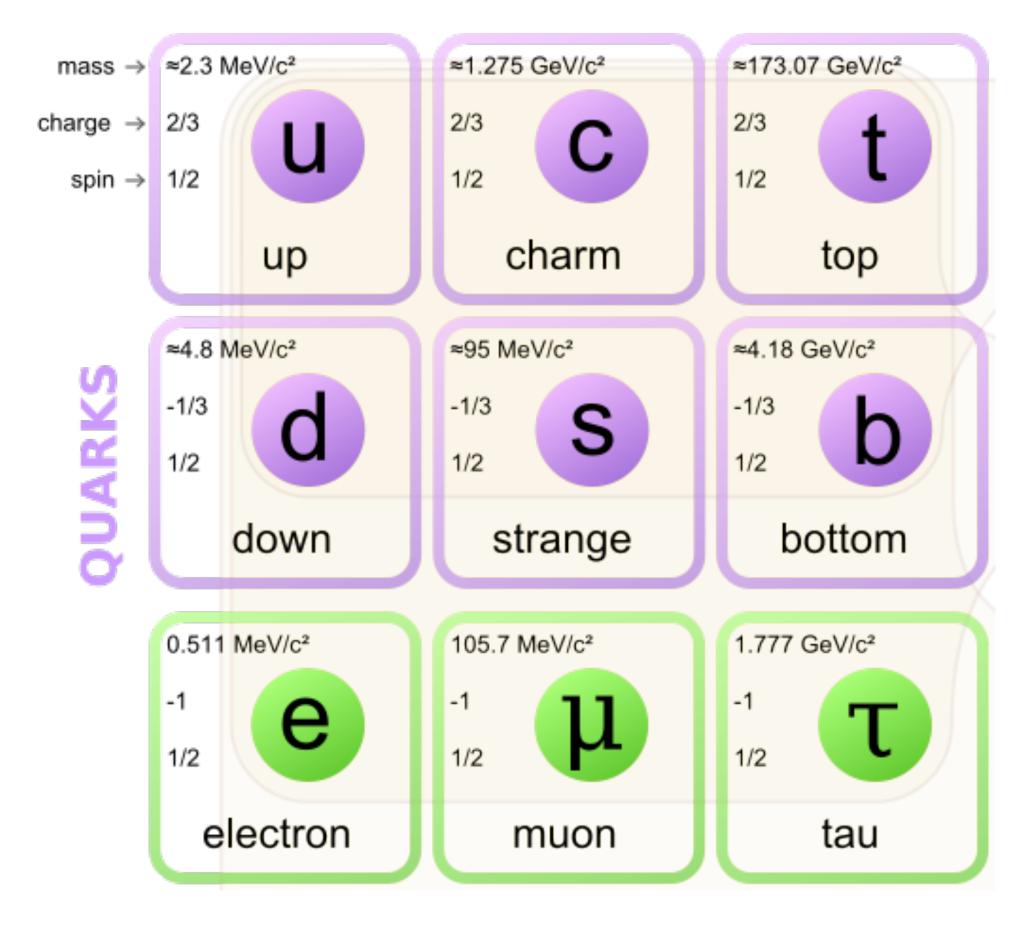


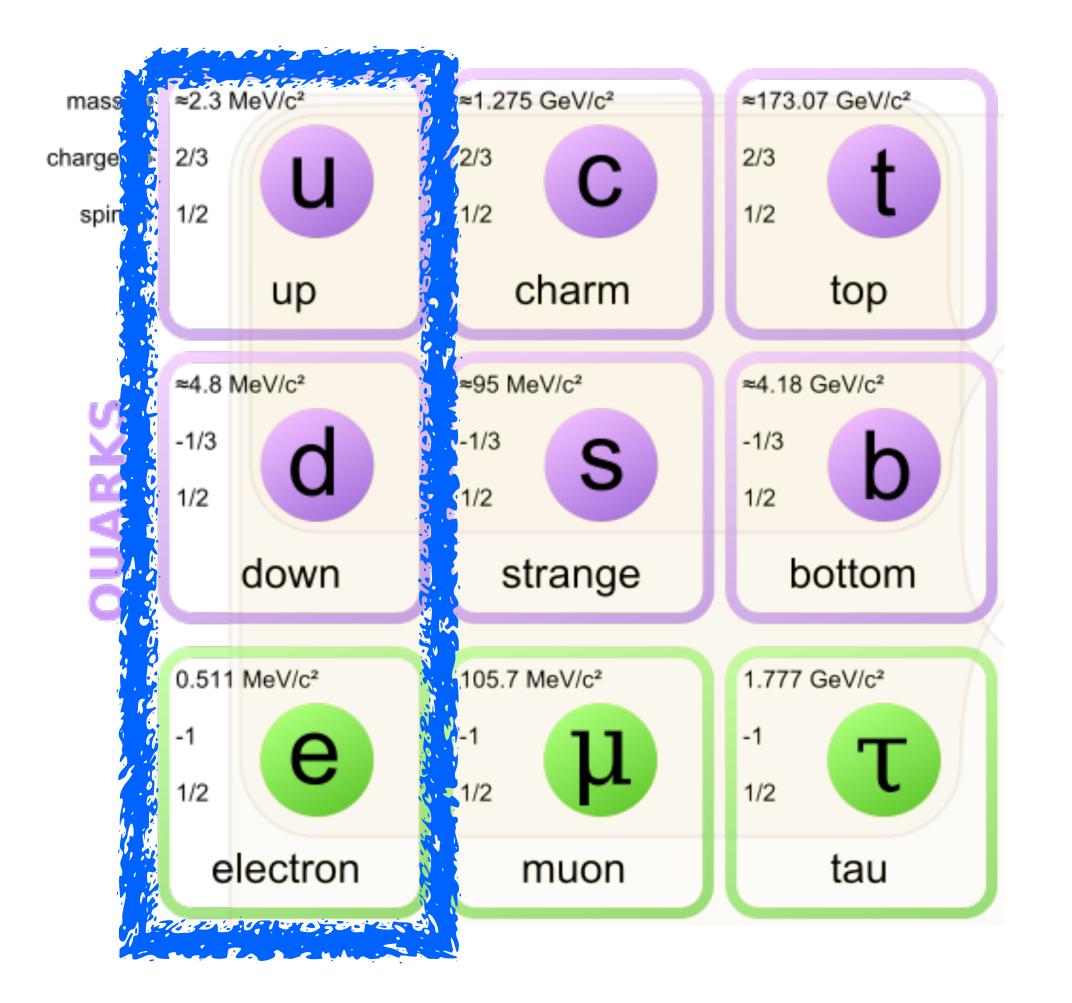
Bohr radius

$$a_0 = \frac{4\pi\epsilon_0 \hbar^2}{m_e e^2} = \frac{\hbar}{m_e c\alpha} \propto \frac{1}{y_e}$$

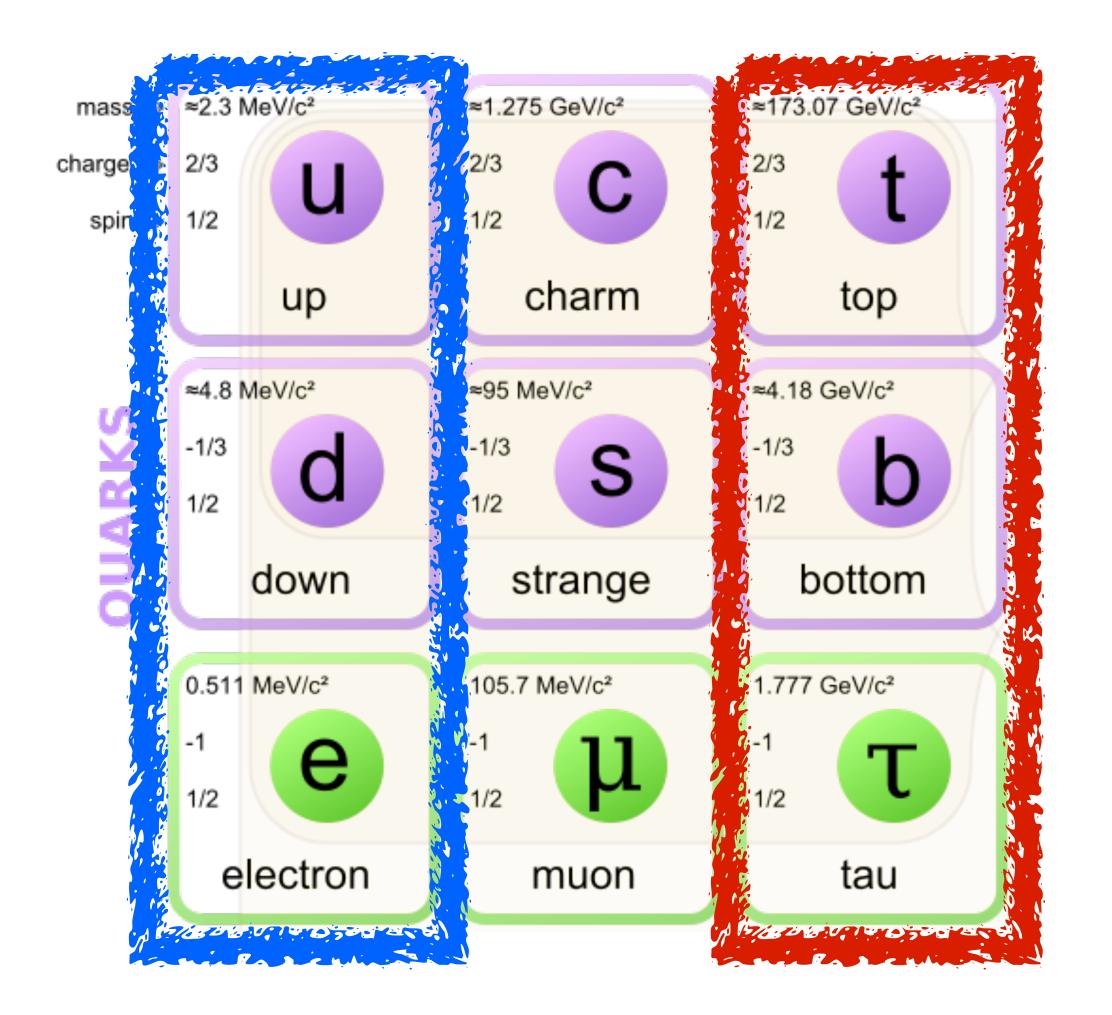
electron mass determines size of all atoms

it sets energy levels of all chemical reactions



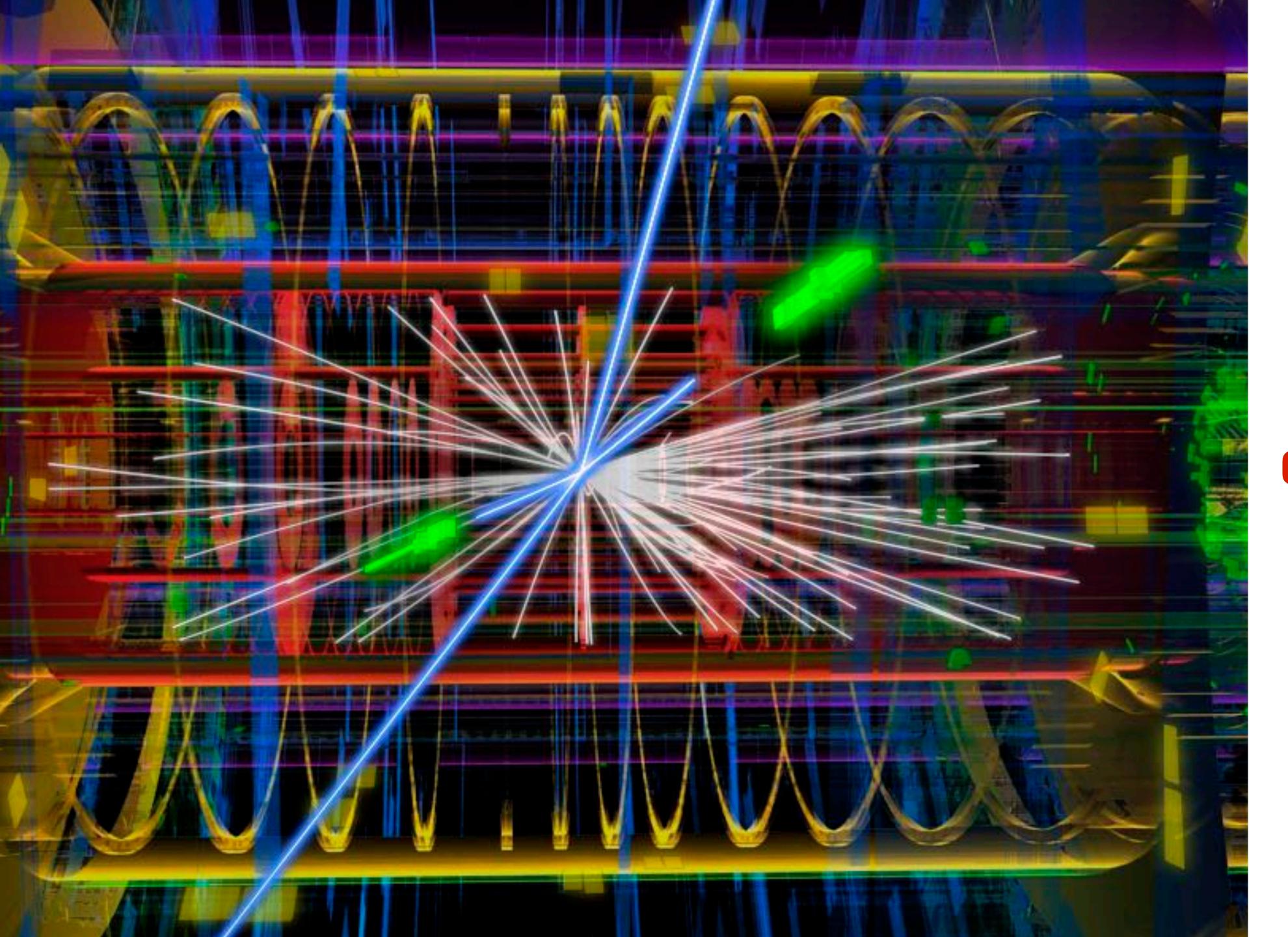


1st generation (us) has low
mass because of weak
interactions with Higgs field
(and so with Higgs bosons):
too weak to test today



1st generation (us) has low
mass because of weak
interactions with Higgs field
(and so with Higgs bosons):
too weak to test today

3rd generation (us) has high mass because of strong interactions with Higgs field (and so with Higgs bosons): can potentially be tested



ATLAS & CMS

@LHC

~up to 2 billion collisions/second

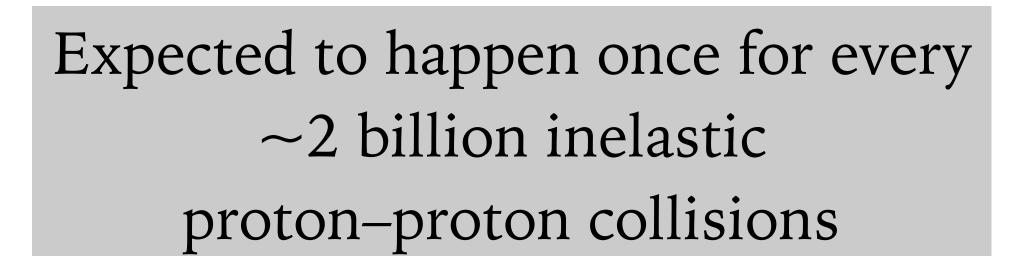
(+ lower rates at LHCb and ALICE)

what underlying processes tell us about Yukawa interactions?

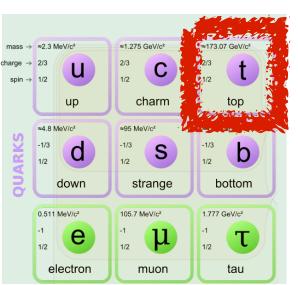
gluon in from proton 1 virtual top-quark pair: not actually seen in detector gluon in from proton 2

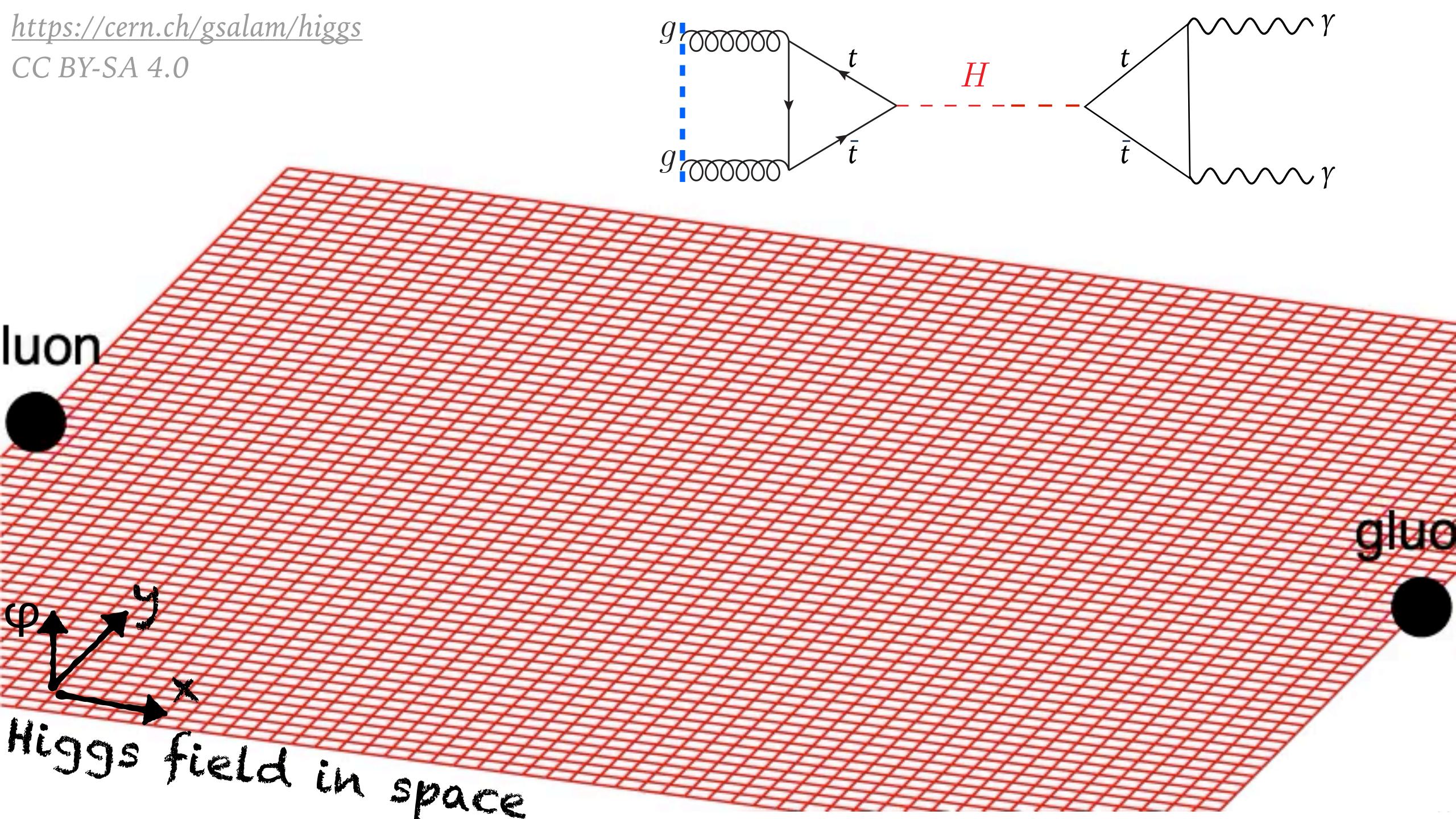
Higgs production: the dominant channel

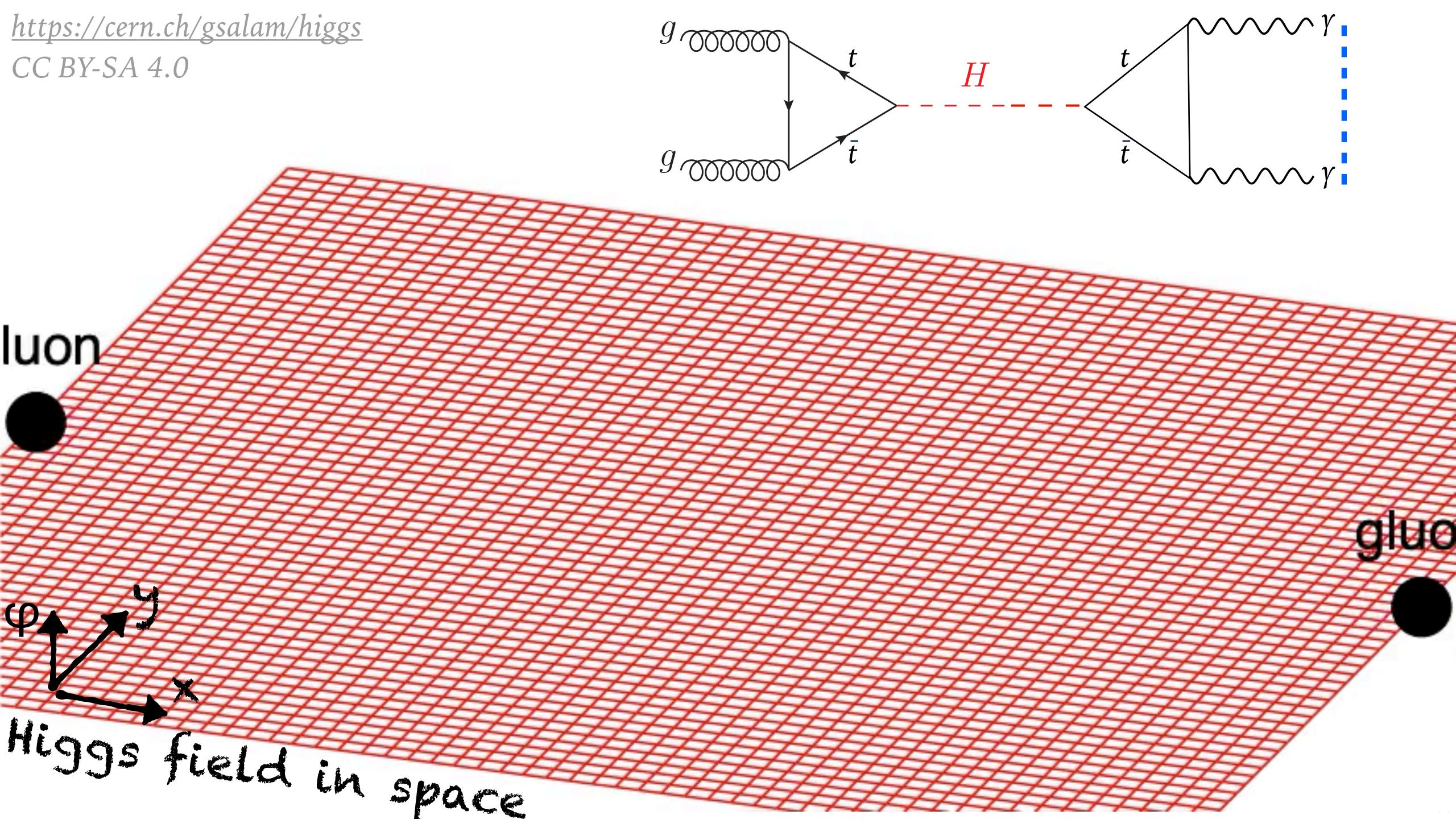
Higgs out

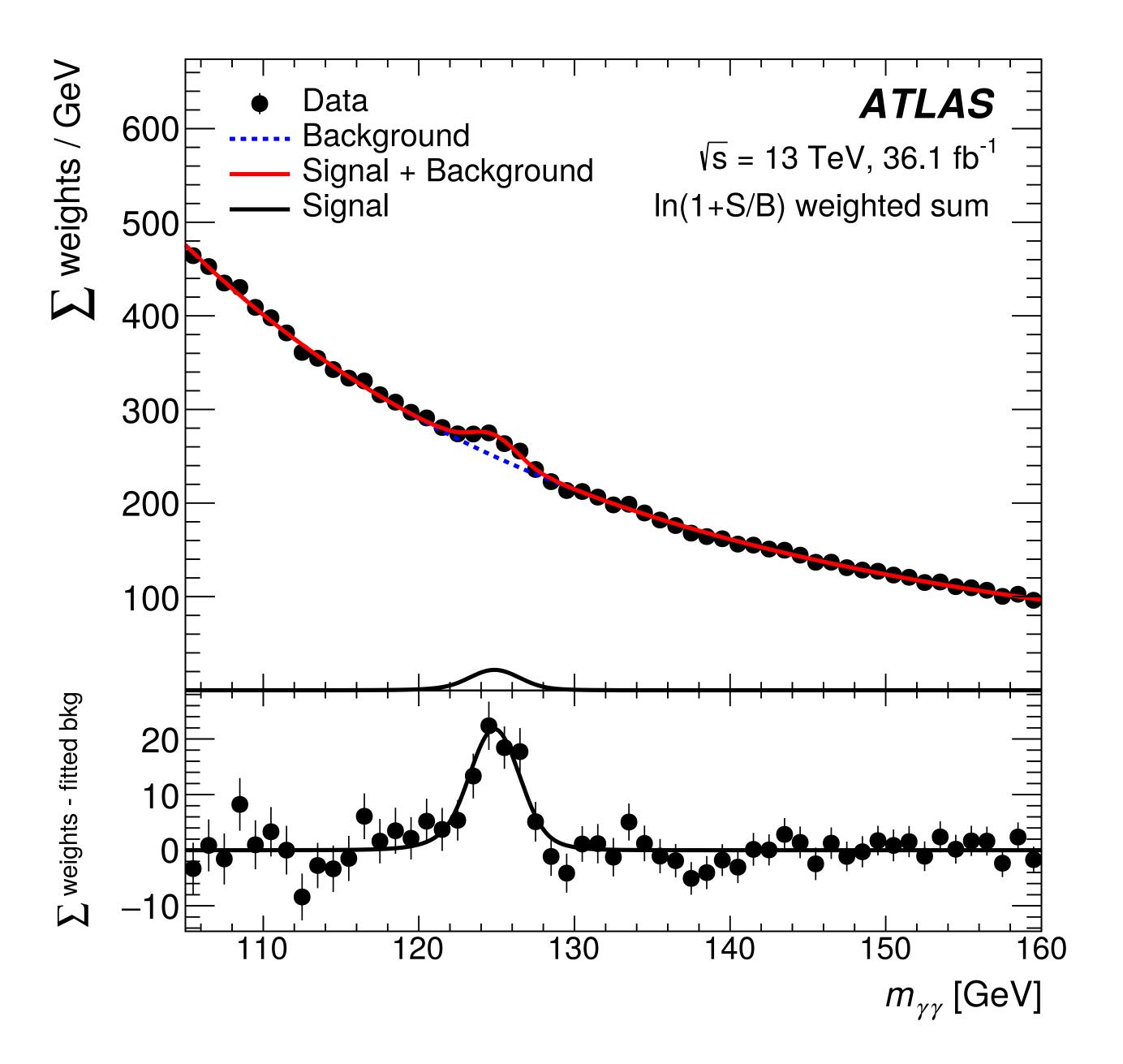


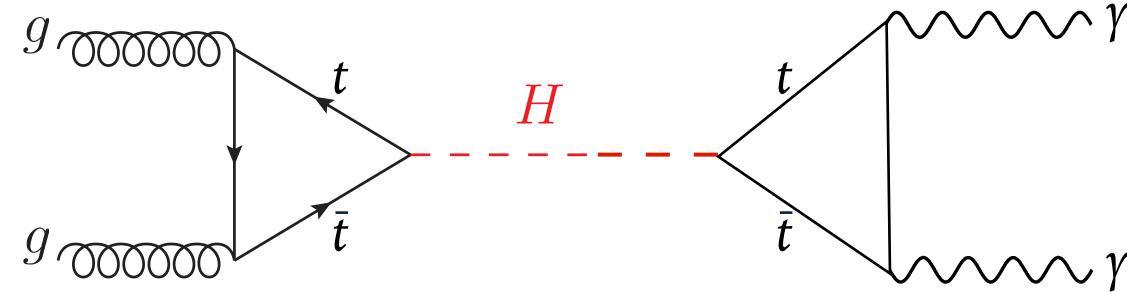
LHC data consistent with that already at discovery in 2012

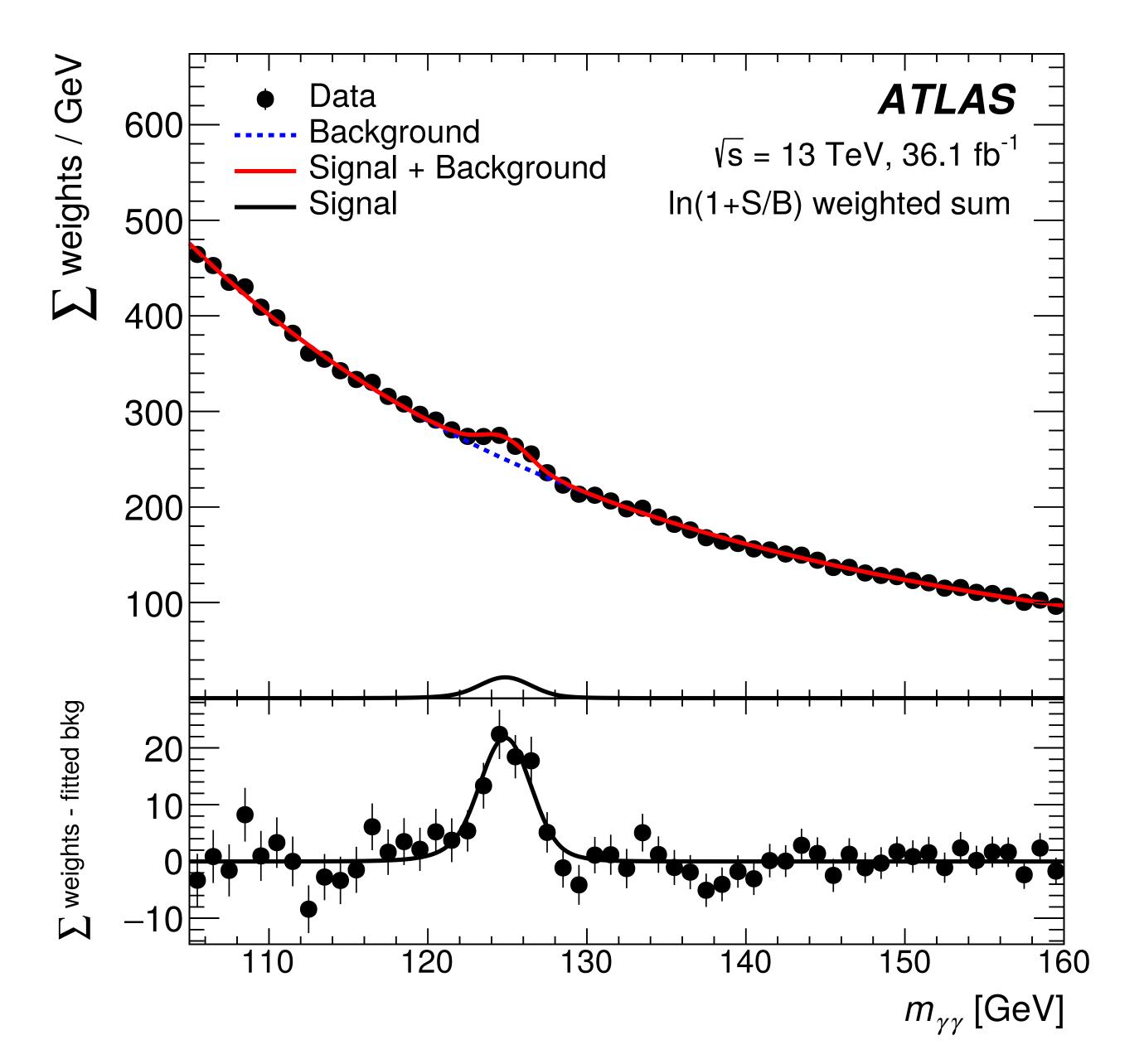


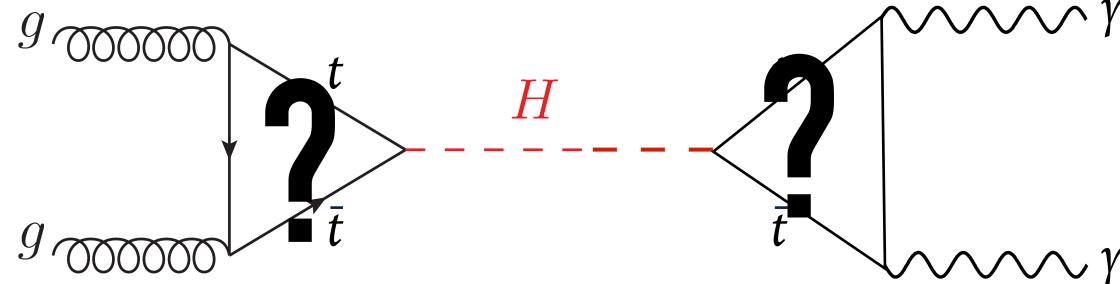












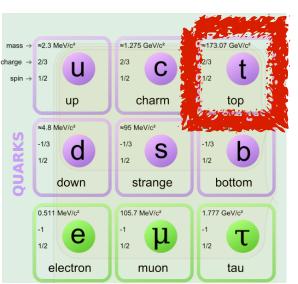
but how can you be sure the Higgs boson is really being radiated off a top-quark, i.e. that you're actually seeing a Yukawa coupling?

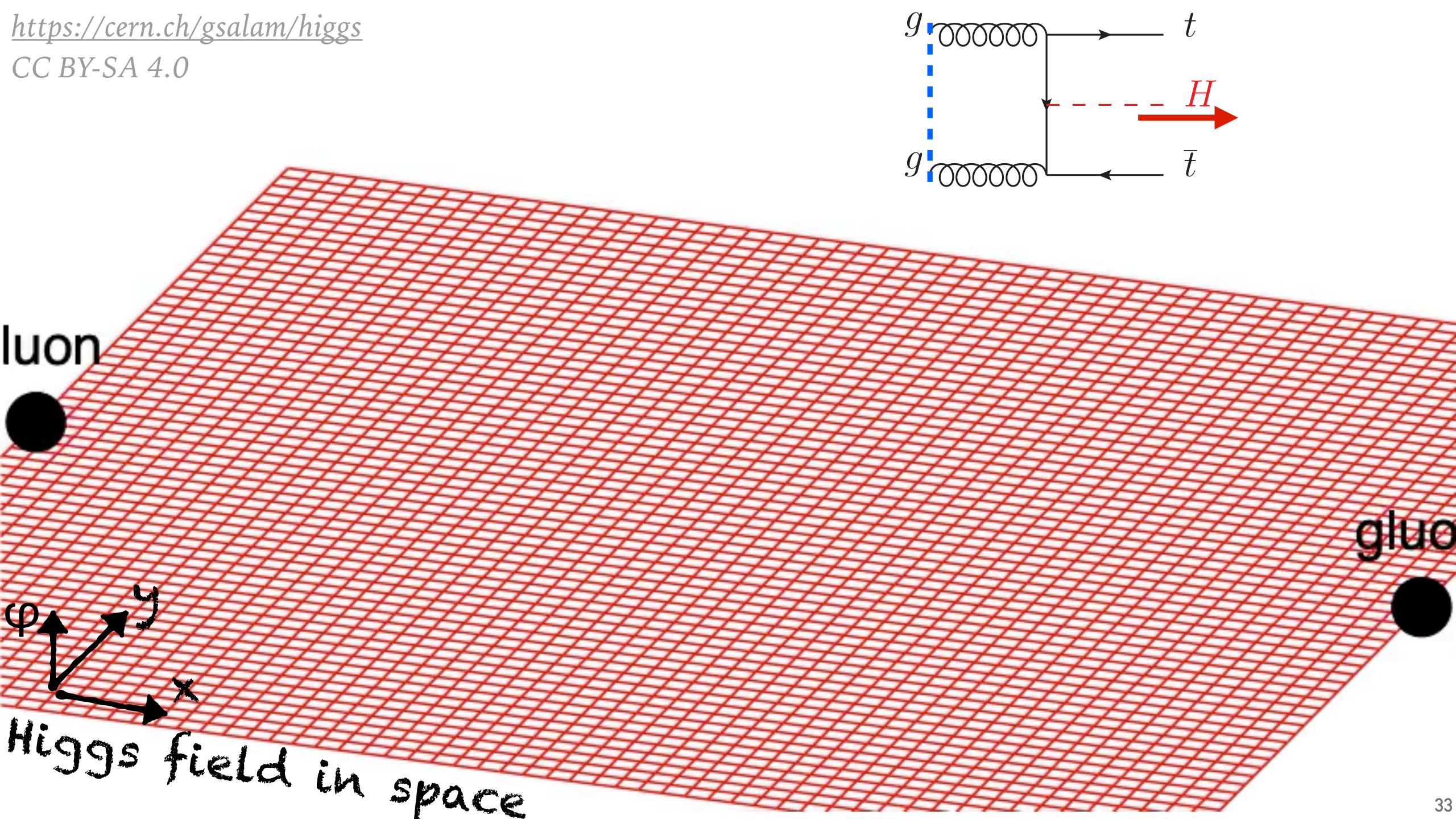
gluon in from proton 1 Higgs out real top-quarks seen in detector gluon in from proton 2

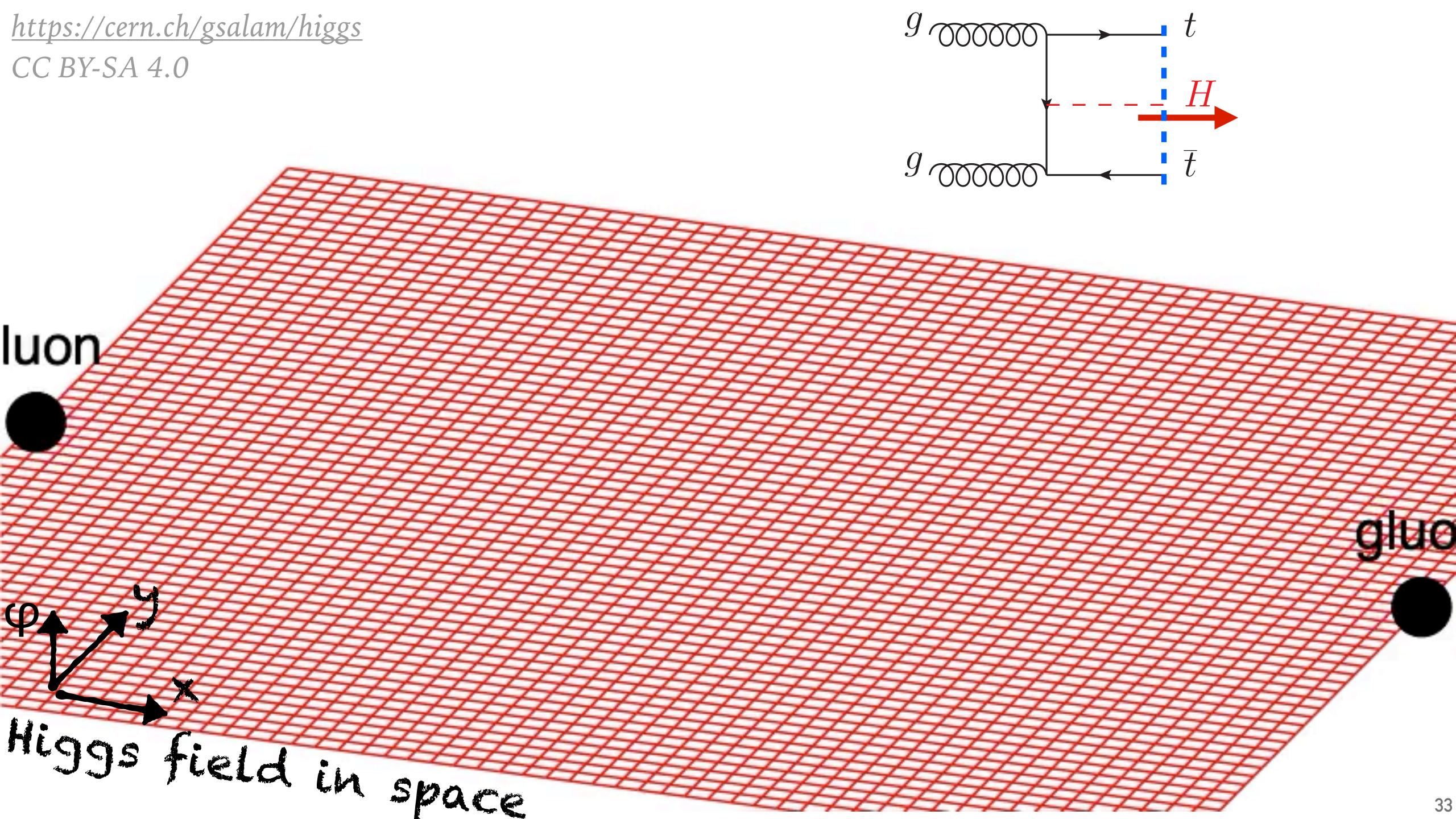
Higgs production: the ttH channel

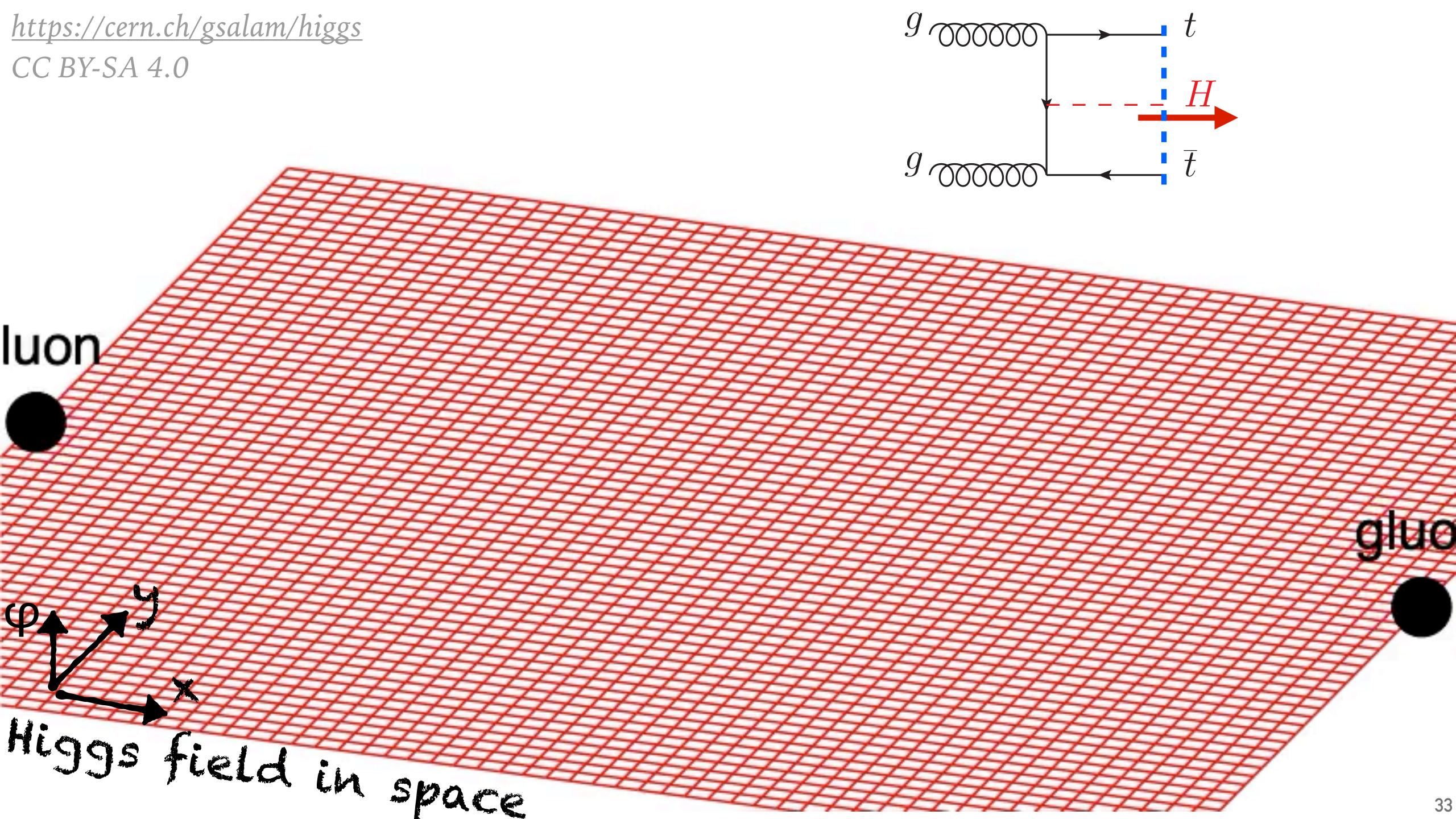
If SM top-Yukawa hypothesis is correct, expect 1 Higgs for every 1600 top-quark pairs.

(rather than 1 Higgs for every 2 billion pp collisions)

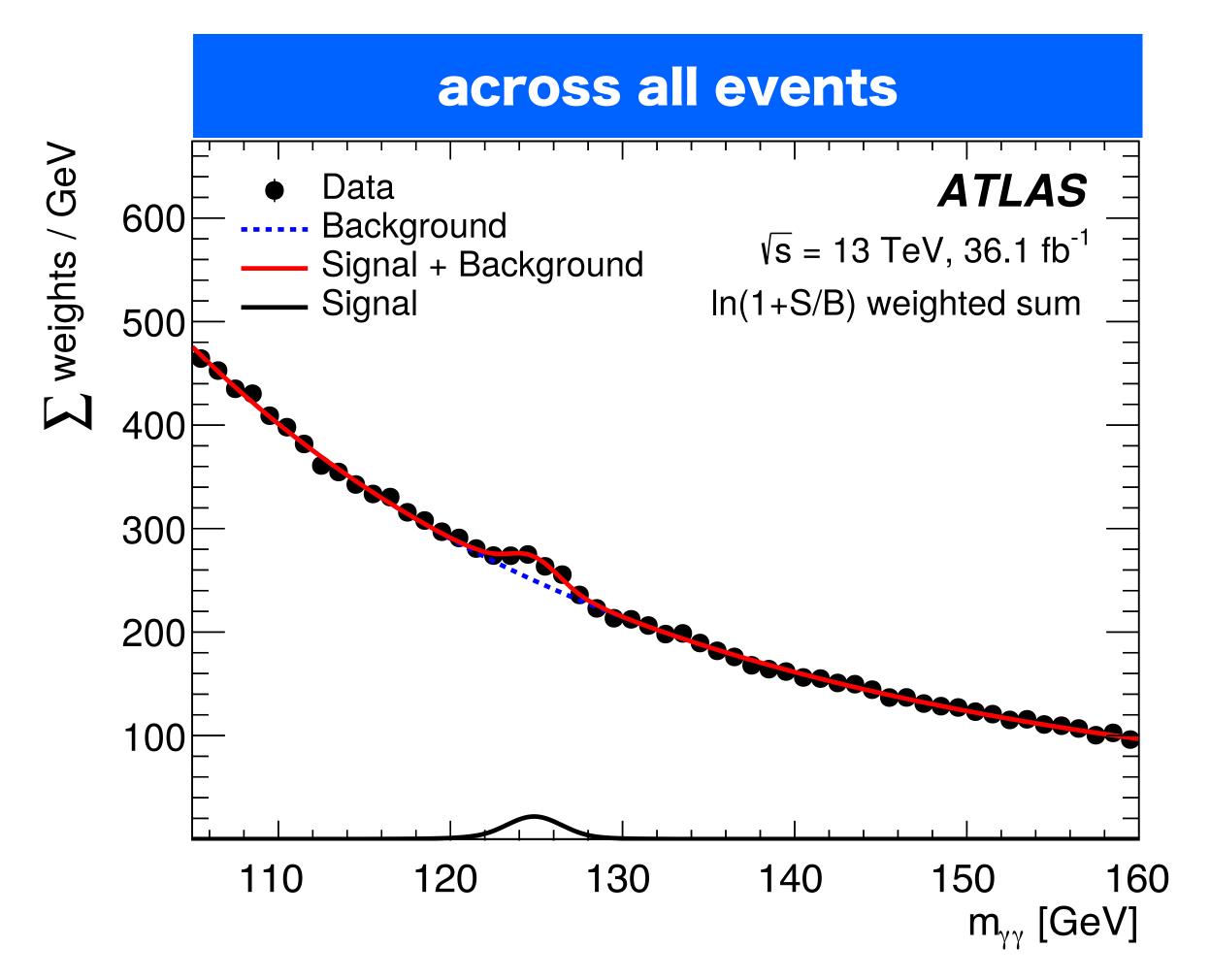


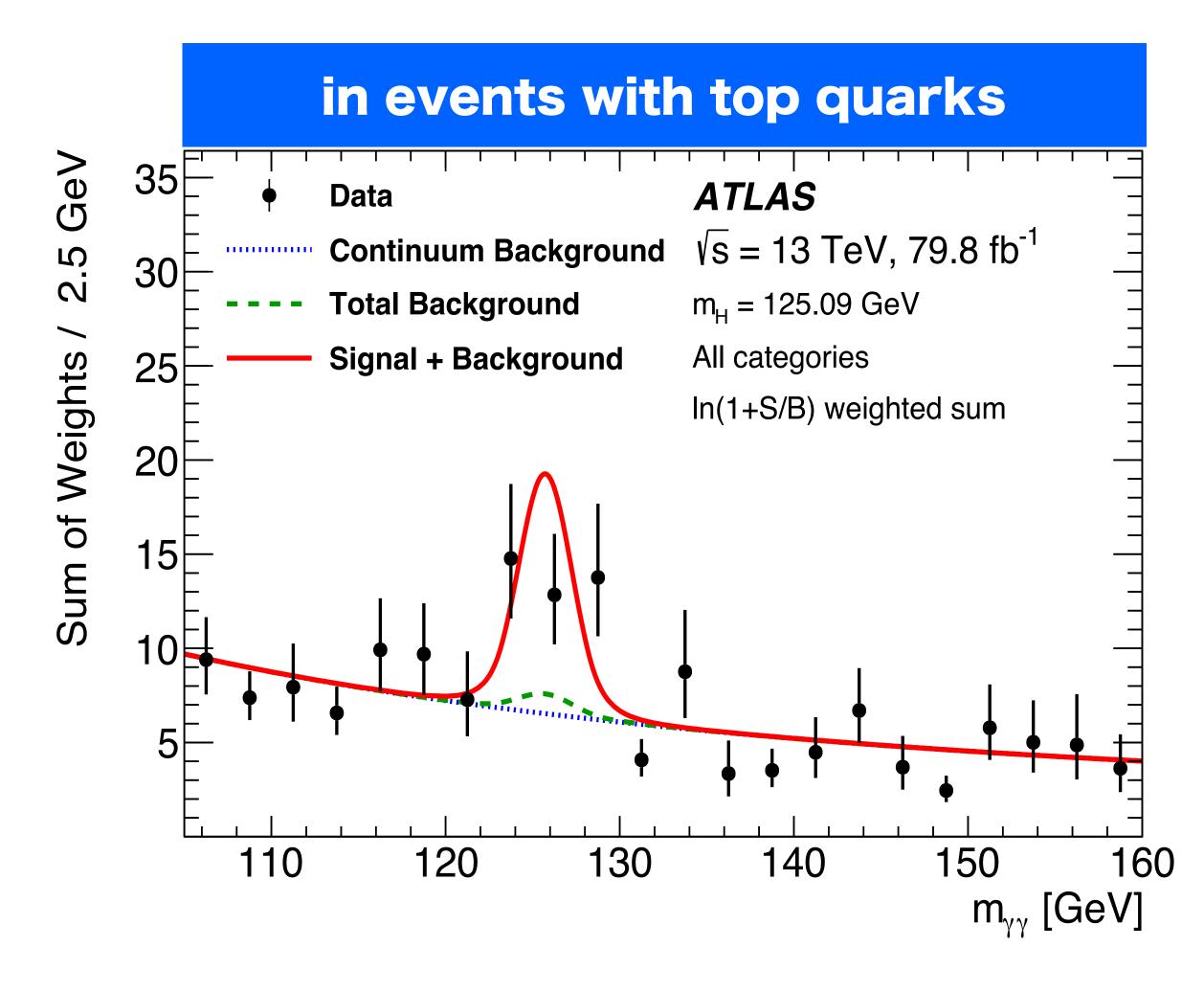


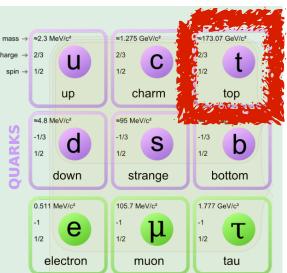




the news of the past 18 months: ATLAS & CMS see events with top-quarks & Higgs simultaneously



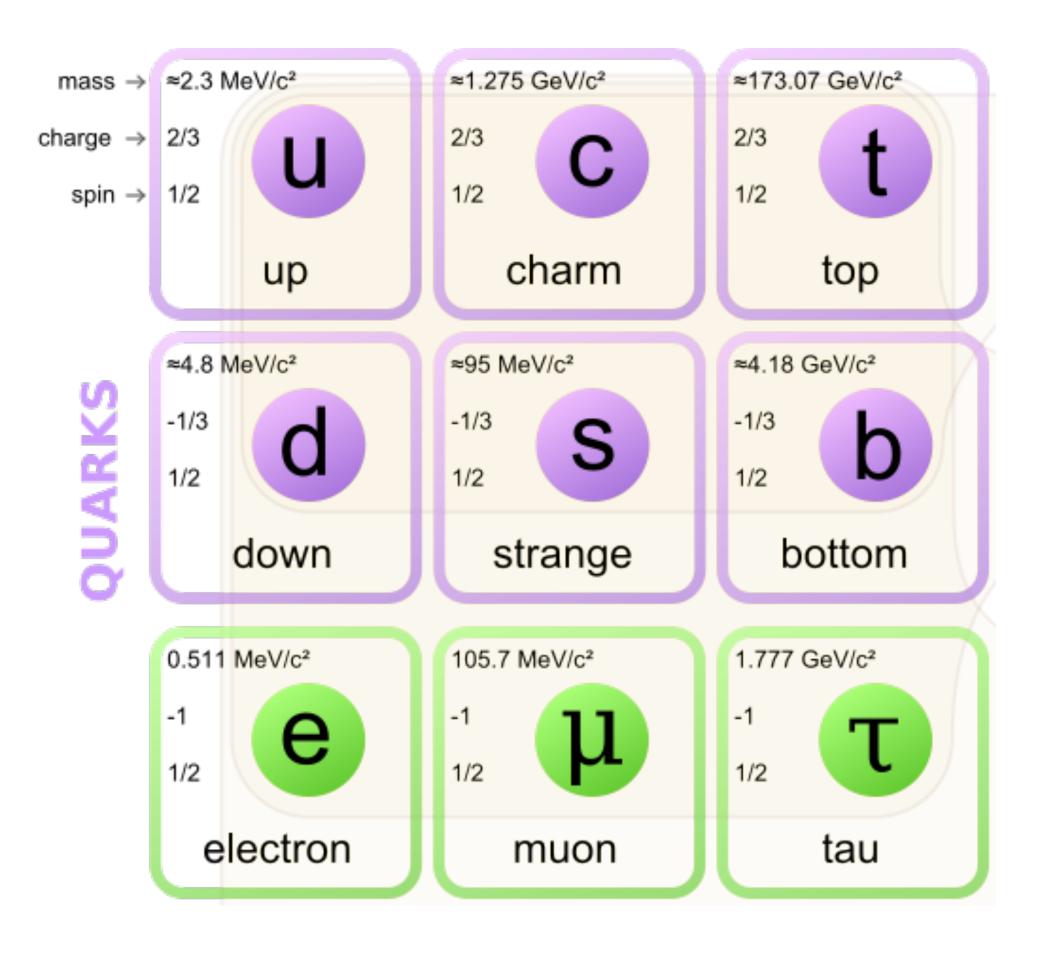




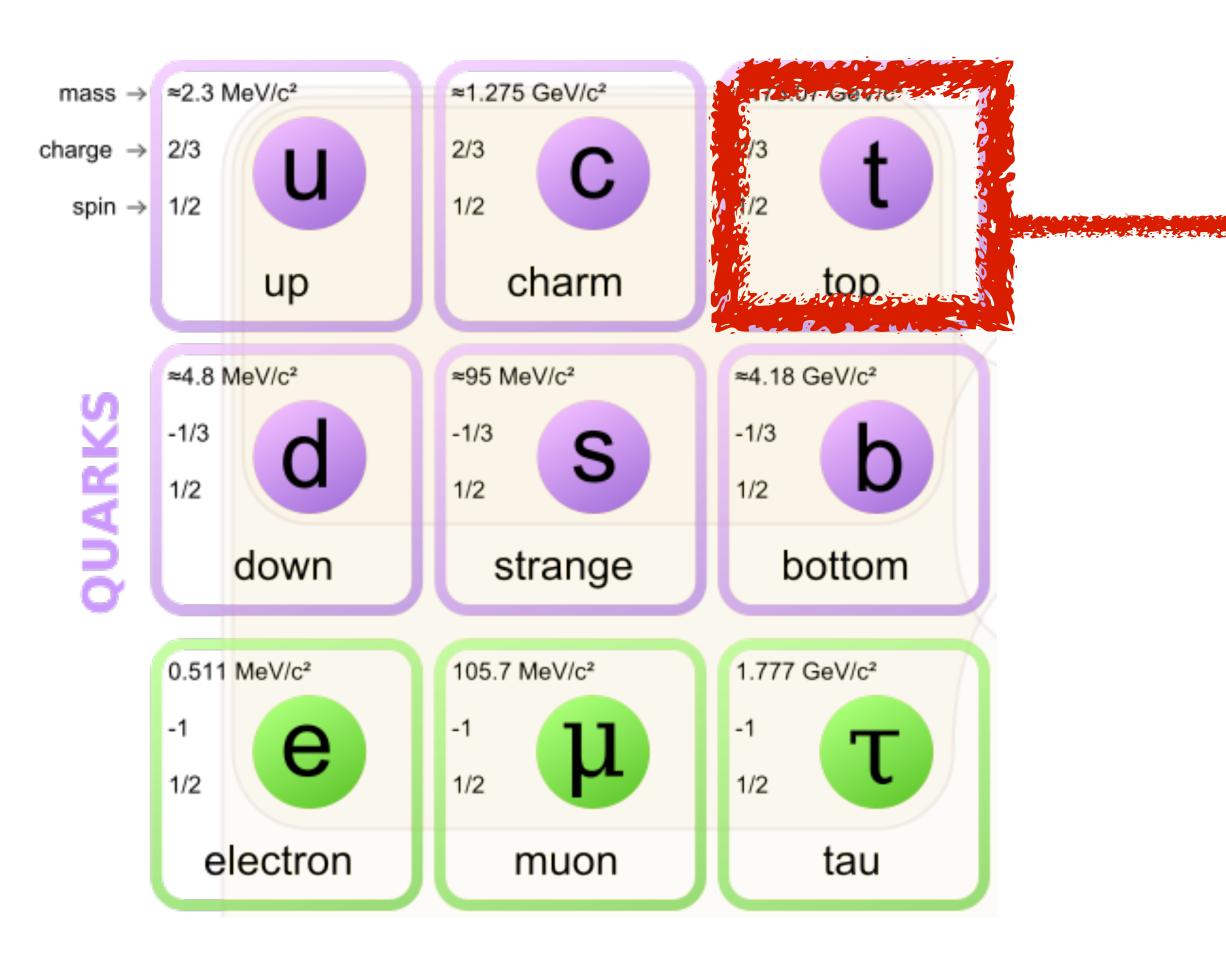
enhanced fraction of Higgs bosons in events with top quarks

→ direct observation of Higgs interaction with tops

(consistent with SM to c. $\pm 20\%$)

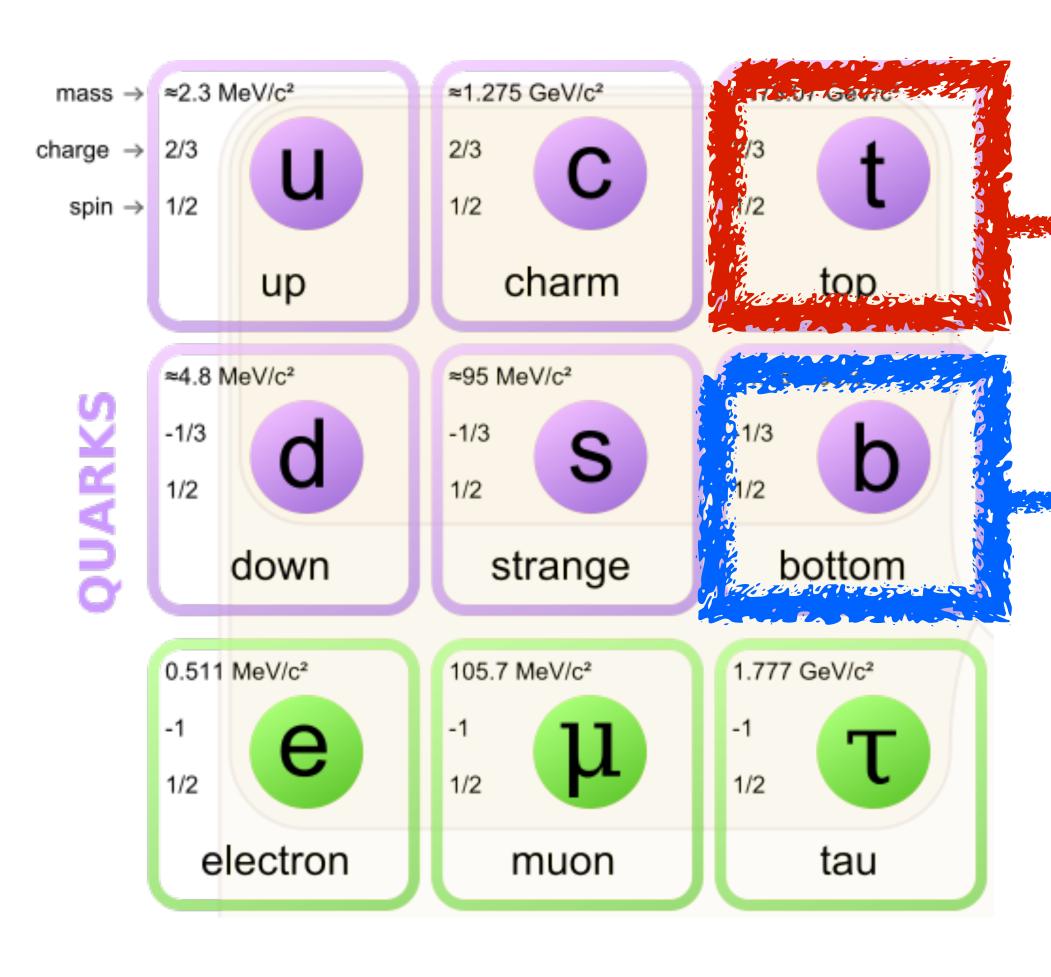


Discovery $\equiv 5\sigma \simeq \pm 20\%$



Discovery $\equiv 5\sigma \simeq \pm 20\%$

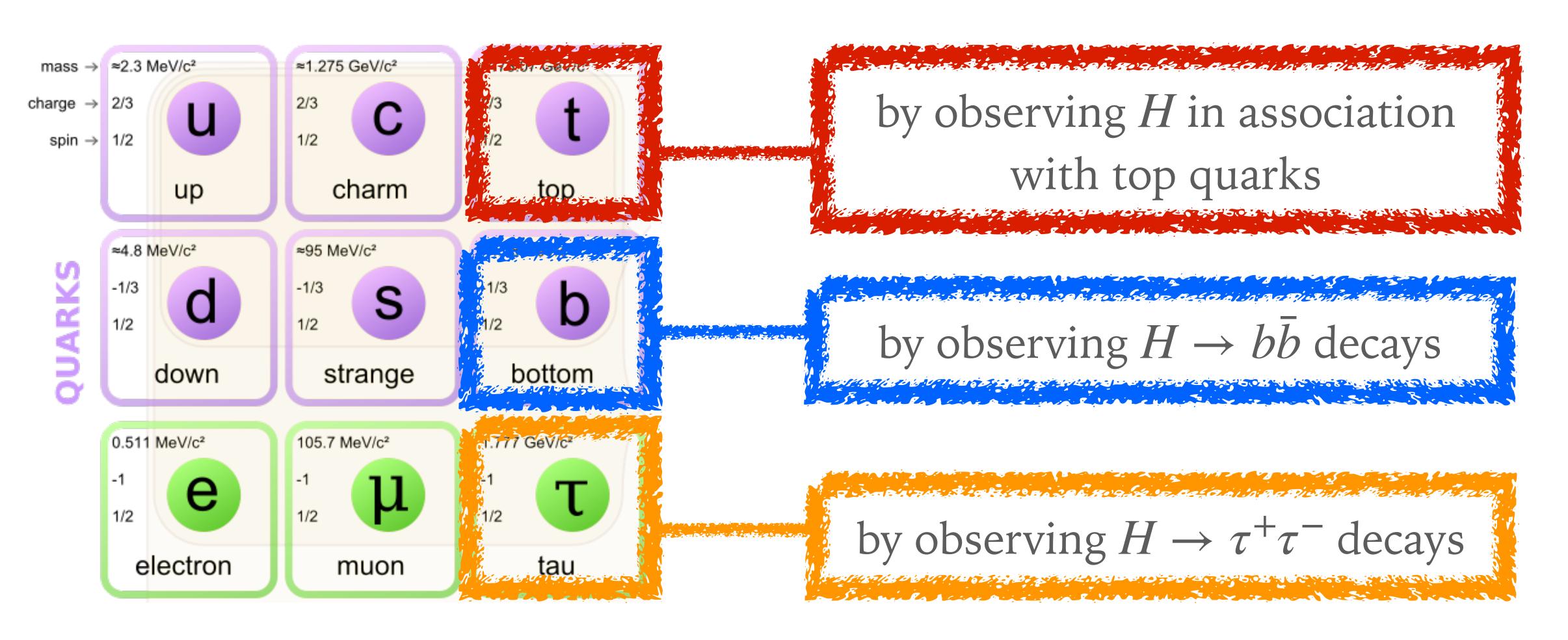
by observing H in association with top quarks



by observing H in association with top quarks

by observing $H \to b\bar{b}$ decays

Discovery
$$\equiv 5\sigma \simeq \pm 20\%$$



Discovery
$$\equiv 5\sigma \simeq \pm 20\%$$

what's the message?

The >5 σ observations of the ttH process and of H \rightarrow tt and H \rightarrow bb decays, independently by ATLAS and CMS, firmly establish the existence of a new kind of fundamental interaction, Yukawa interactions.

Yukawa interactions are important because they are:

- (1) qualitatively unlike any quantum interaction probed before (effective charge not quantised),
- (2) hypothesized to be responsible for the stability of hydrogen, and for determining the size of atoms and the energy scales of chemical reactions.

Establishing the pattern of Yukawa couplings across the full remaining set of quarks and charged leptons is one of the major challenges for particle physics today.

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Establishing the pattern of Yukawa couplings across the full remaining set of quarks and charged leptons is one of the major challenges for particle physics today.

Is this any less important than the discovery of the Higgs boson itself?

My opinion: no, because fundamental interactions are as important as fundamental particles

what could one be saying about it?

LHC discovers fifth force, the "Higgs force"

(up to you to decide whether you prefer to talk about new interactions or new force)

Is this any less important than the discovery of the Higgs boson itself?

My opinion: no, because fundamental interactions are as important as fundamental particles

metric for success going forwards [one possible view]

Long term:

can we observe Higgs self coupling?

I.e. get an experimental window on the Higgs potential, which underpins the rest of the SM

> Medium term:

evolve today's c. 10-20% constraints on Higgs sector towards accuracy (we wouldn't consider QED established if it had only been tested to 10%)

> Bonuses:

maximise our sensitivity to new physics at colliders and smaller experiments, (what form it takes and whether it's even accessible is in Nature's hands, not ours)

metric for success going forwards [one possible view]

ABINATE STATES OF SOLE OF SOLE

Long term:

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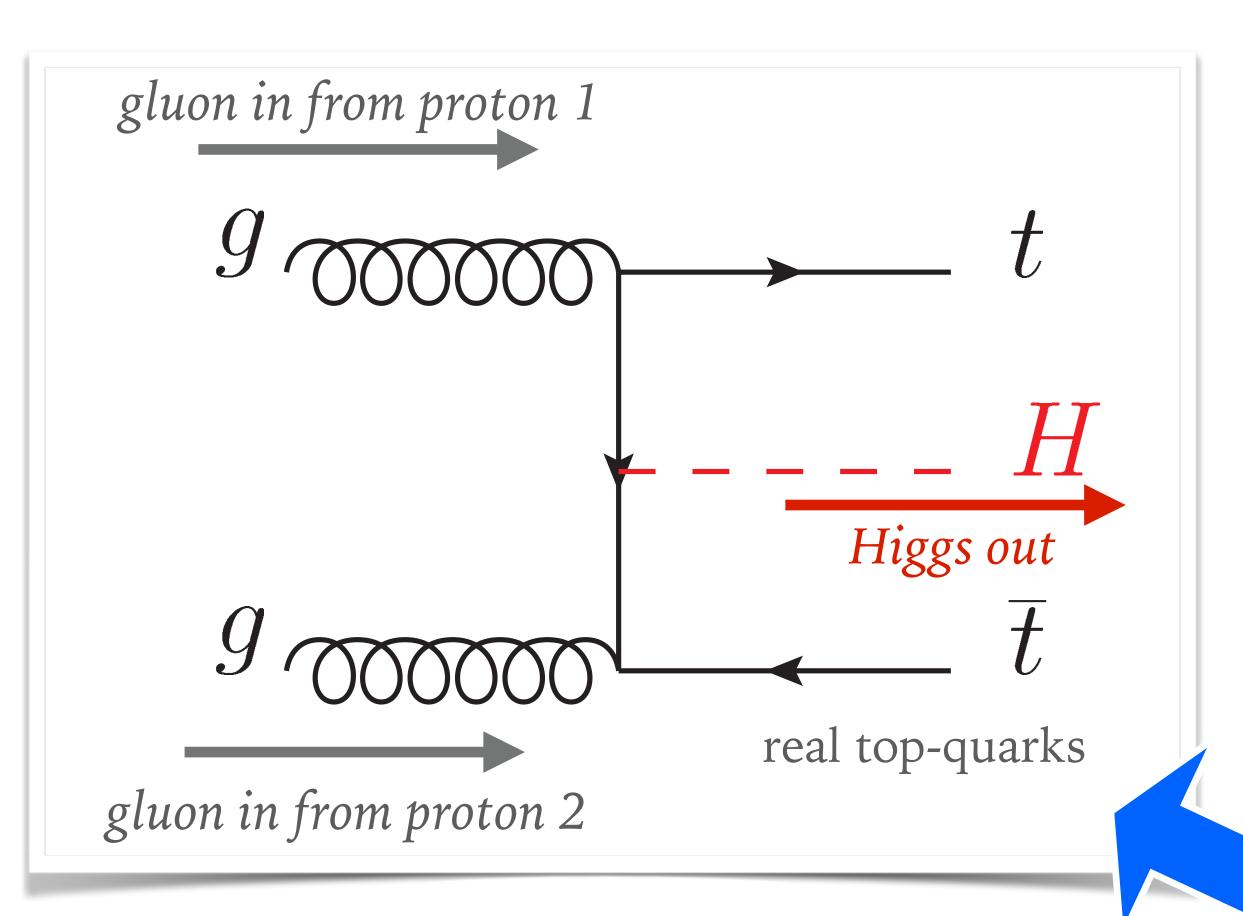
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Medium term:

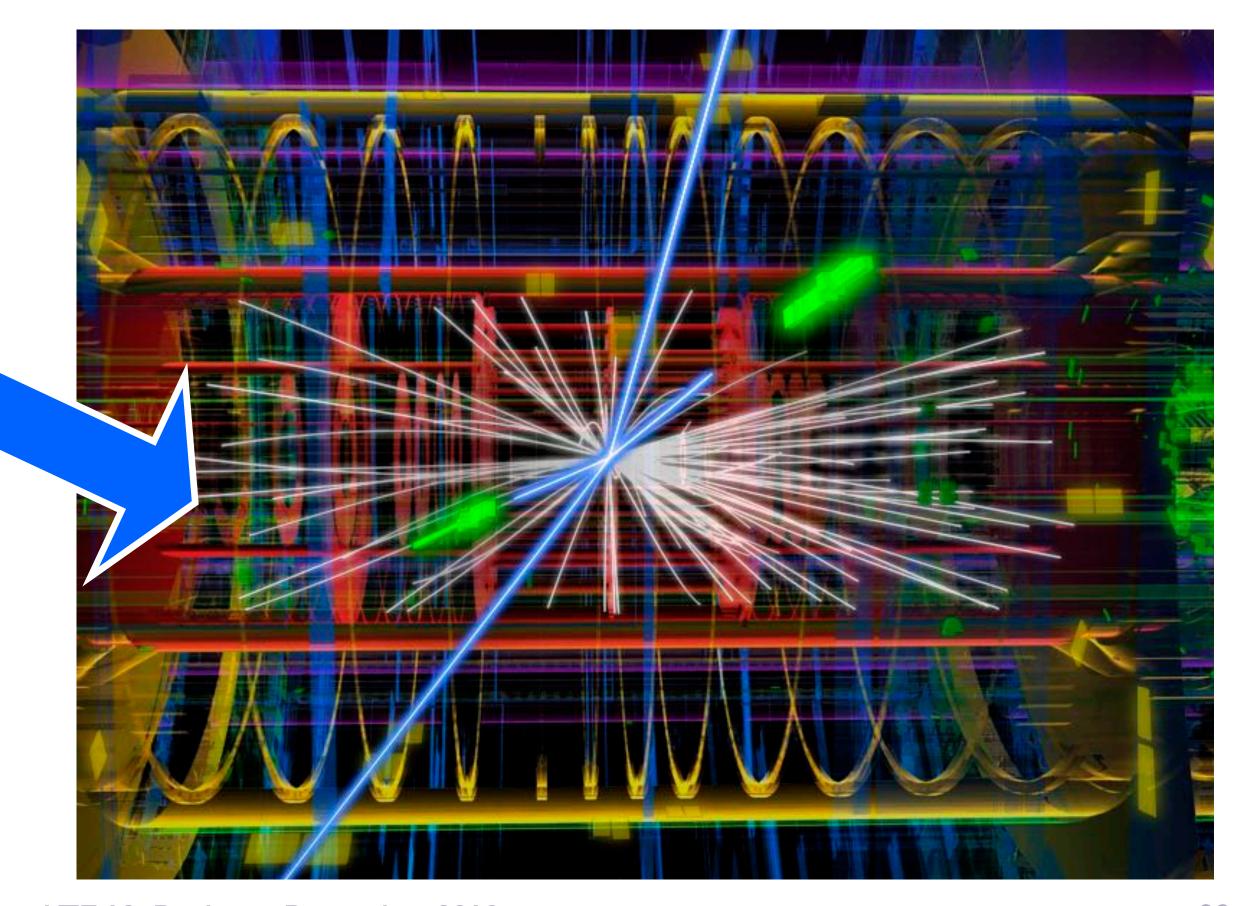
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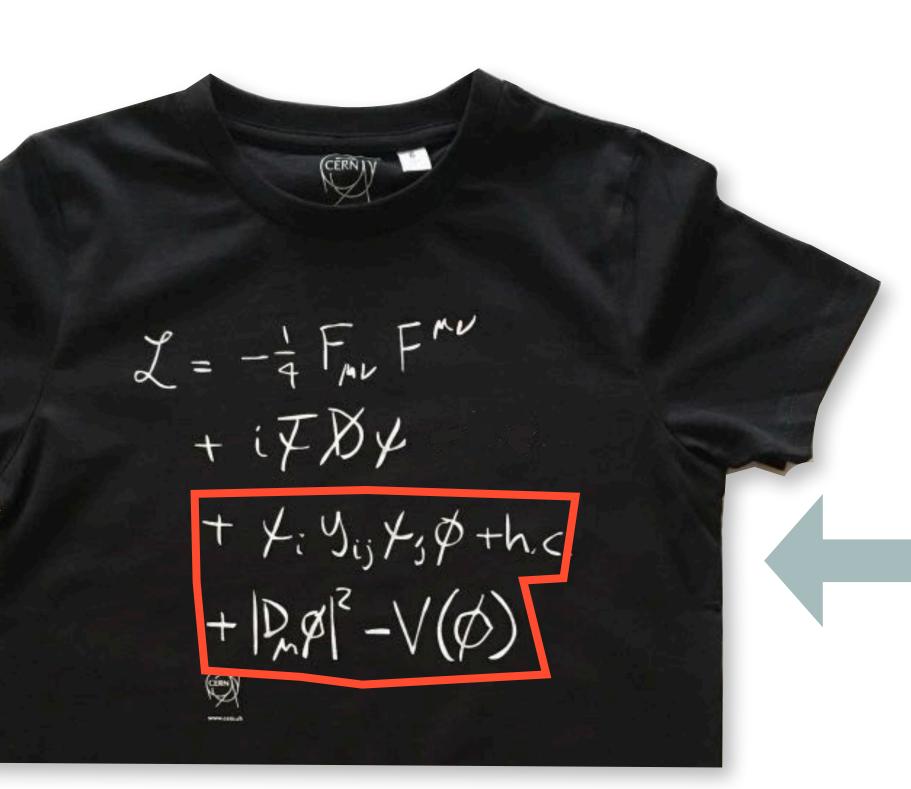


how can one claim a connection, let alone a quantitative one?

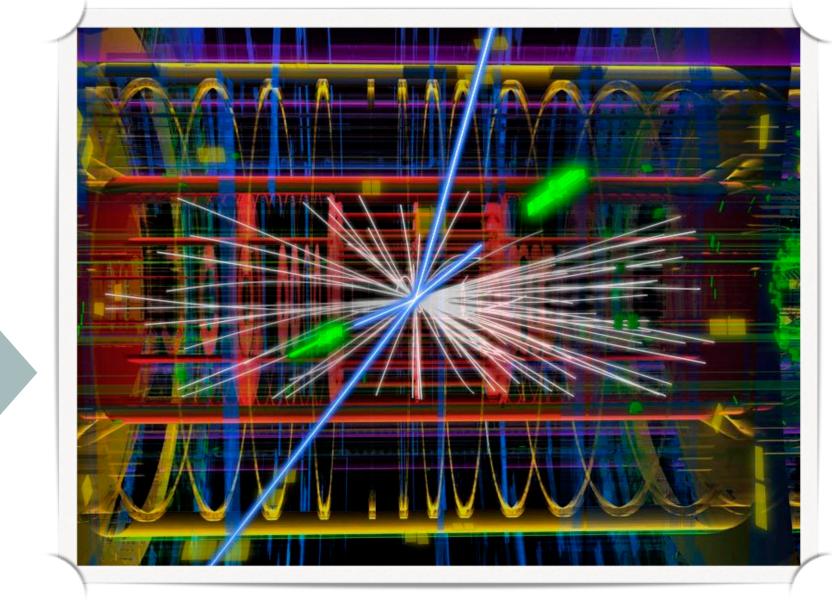


UNDERLYING THEORY

EXPERIMENTAL DATA

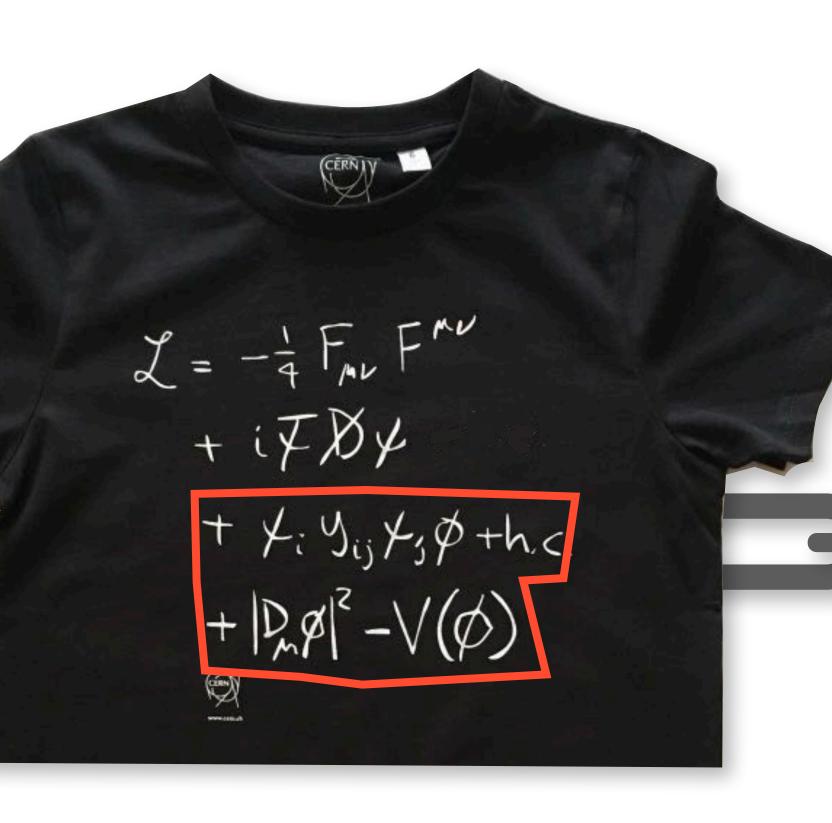


how do you make quantitative connection?



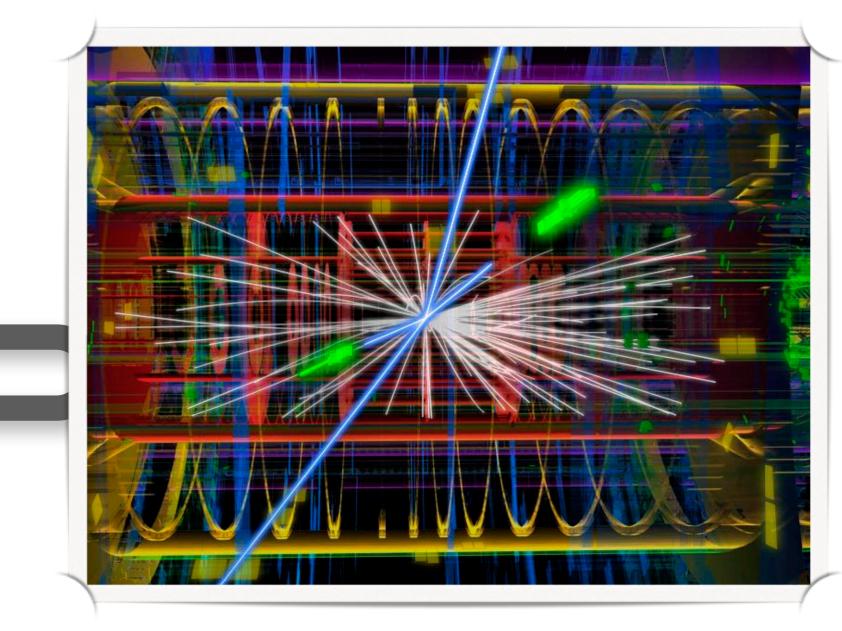
UNDERLYING THEORY

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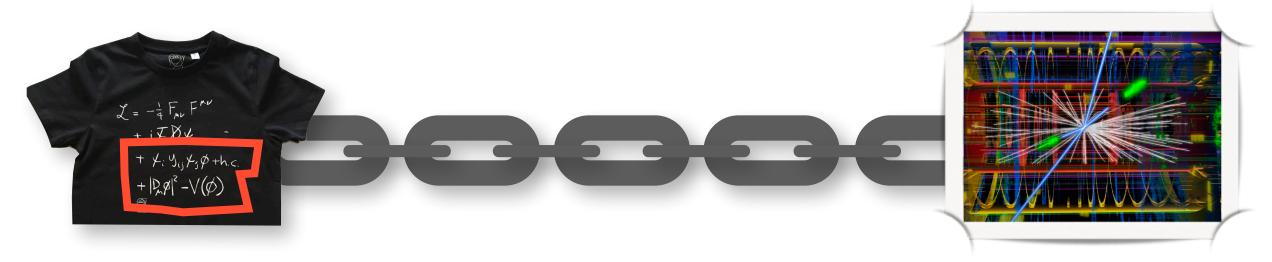


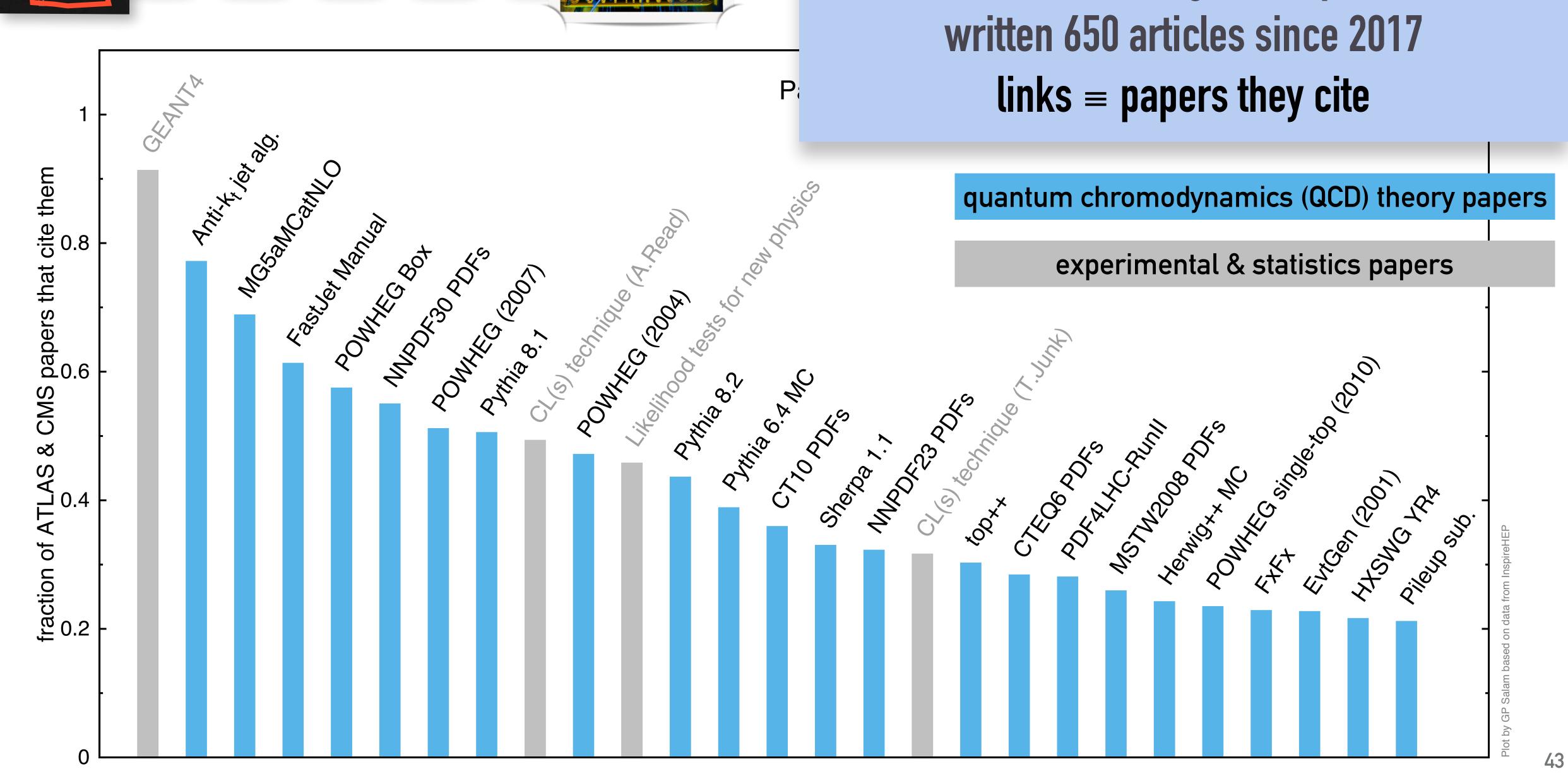
how do you make quantitative connection?

through a chain of experimental and theoretical links



quantum chromodynamics the theory of the strong interaction

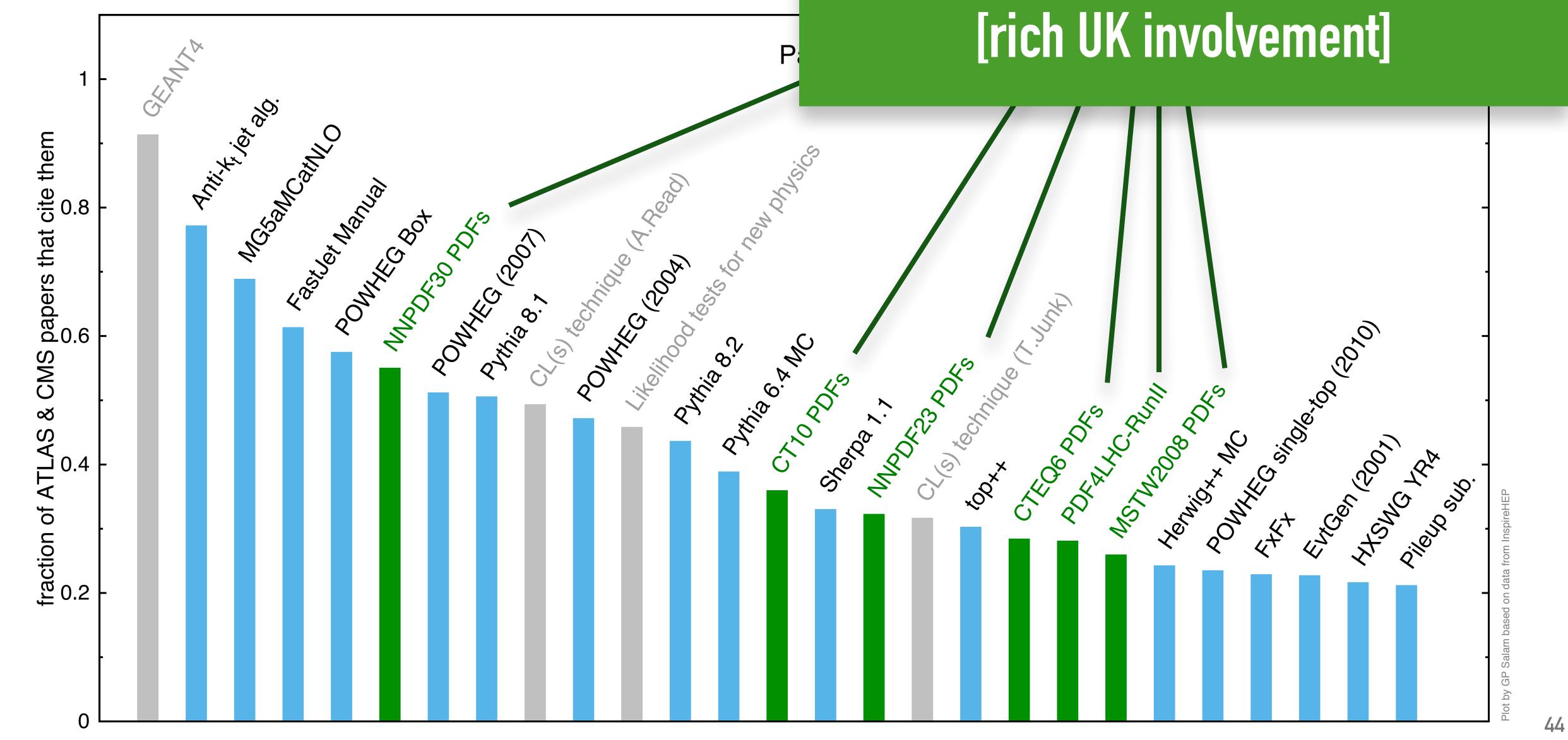


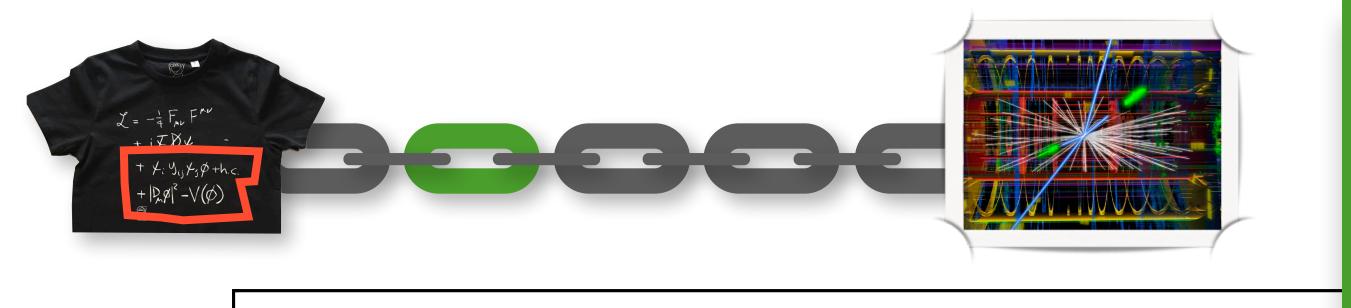


What are the links?

ATLAS and CMS (big LHC expts.) have

knowing what goes into a collision i.e. proton structure





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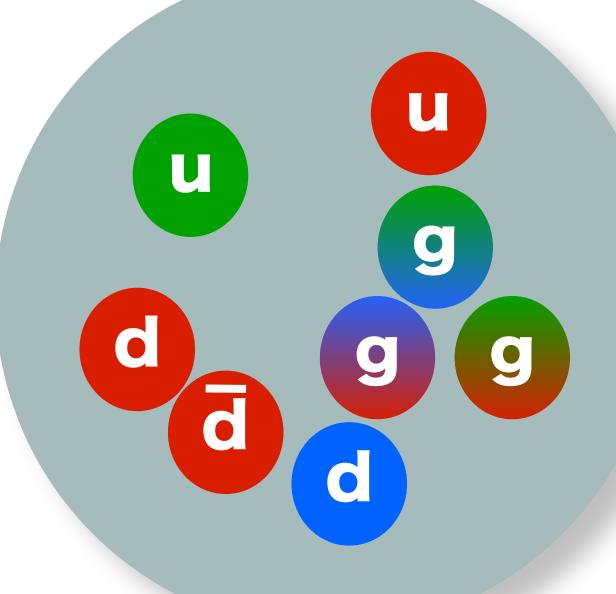
knowing what goes into a collision i.e. proton structure [rich UK involvement]

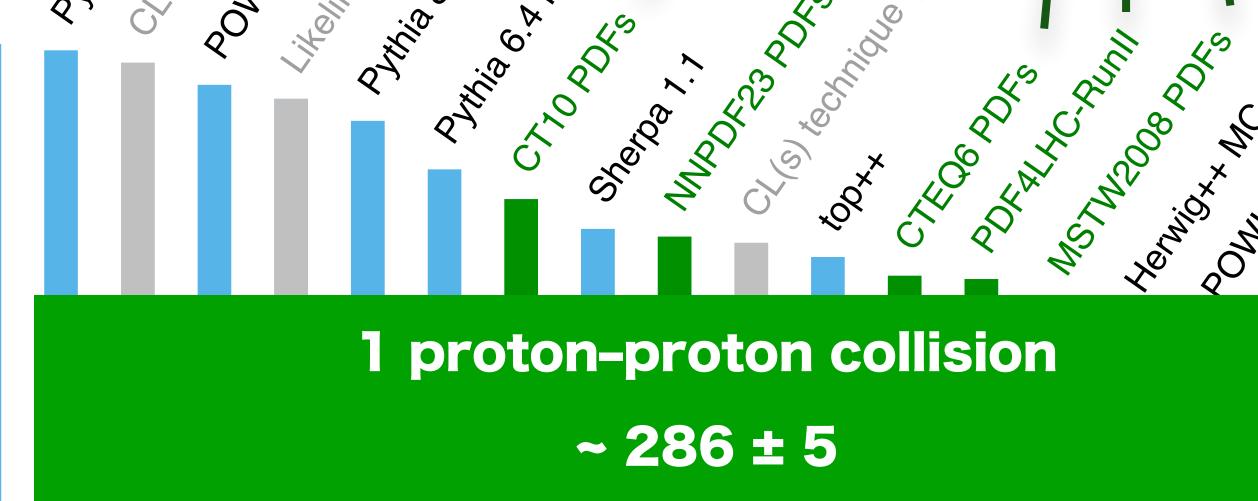
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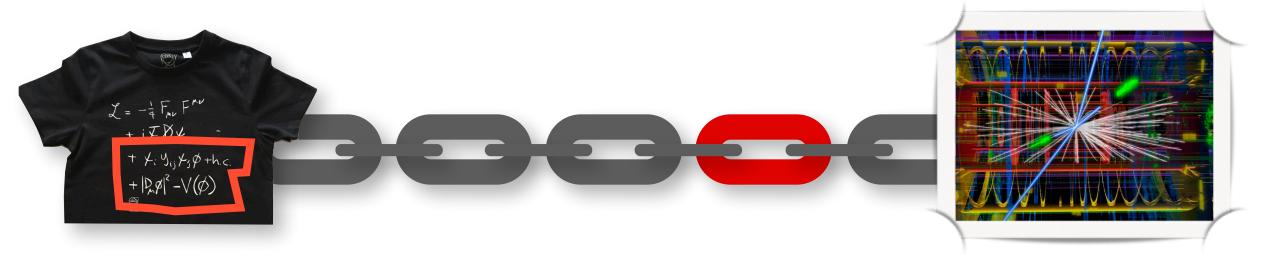
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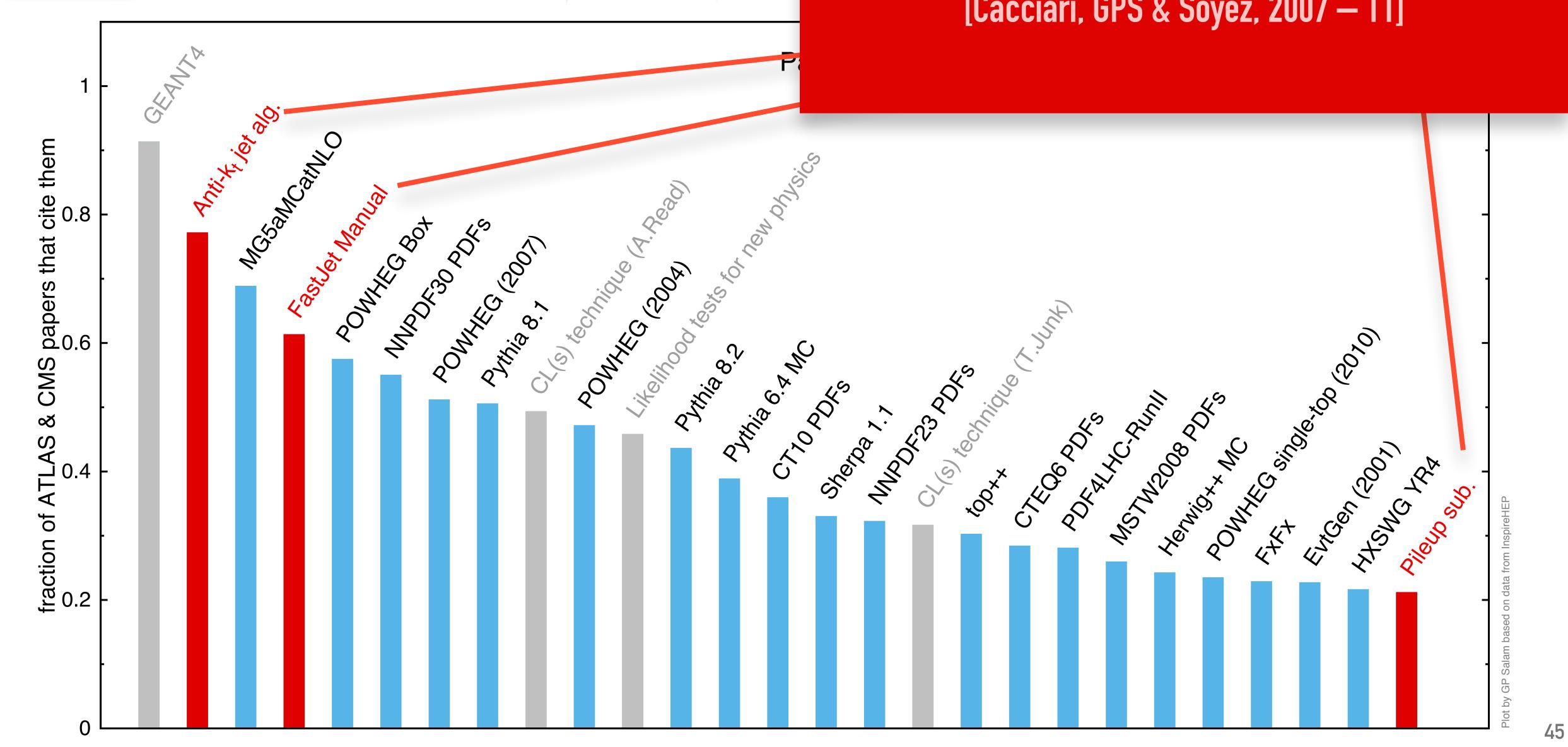
Origina S.

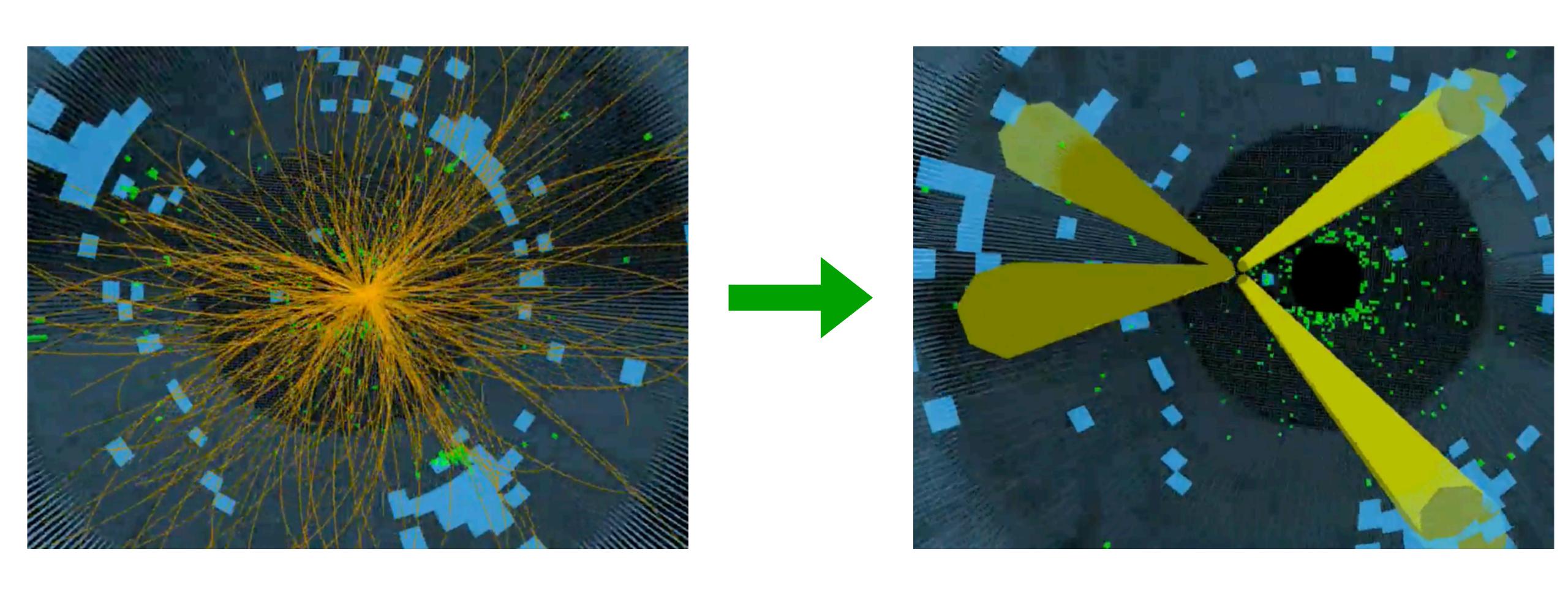
gluon-gluon collisions around the Higgs mass



organising event information ("jets")

[Cacciari, GPS & Soyez, 2007 — 11]





the question of organising information from hundreds of particles will come back later

SCIENTIFIC REPORTS

Article Open Access Published: 09 May 2018

qSR: a quantitative super-resolution analysis tool reveals the cell-cycle dependent organization of RNA Polymerase I in live human cells

J. O. Andrews, W. Conway, W -K. Cho, A. Narayanan, J -H. Spille, N. Jayanth, T. Inoue, S. Mullen, J. Thaler & I. I. Cissé ⊡

Scientific Reports 8, Article number: 7424 (2018) | Cite this article

899 Accesses 3 Citations 11 Altmetric Metrics

Abstract

We present qSR, an analytical tool for the quantitative analysis of single molecule based super-resolution data. The software is created as an

"For identifying spatial clusters, we have implemented both centroid-linkage hierarchical clustering using FastJet [...]"

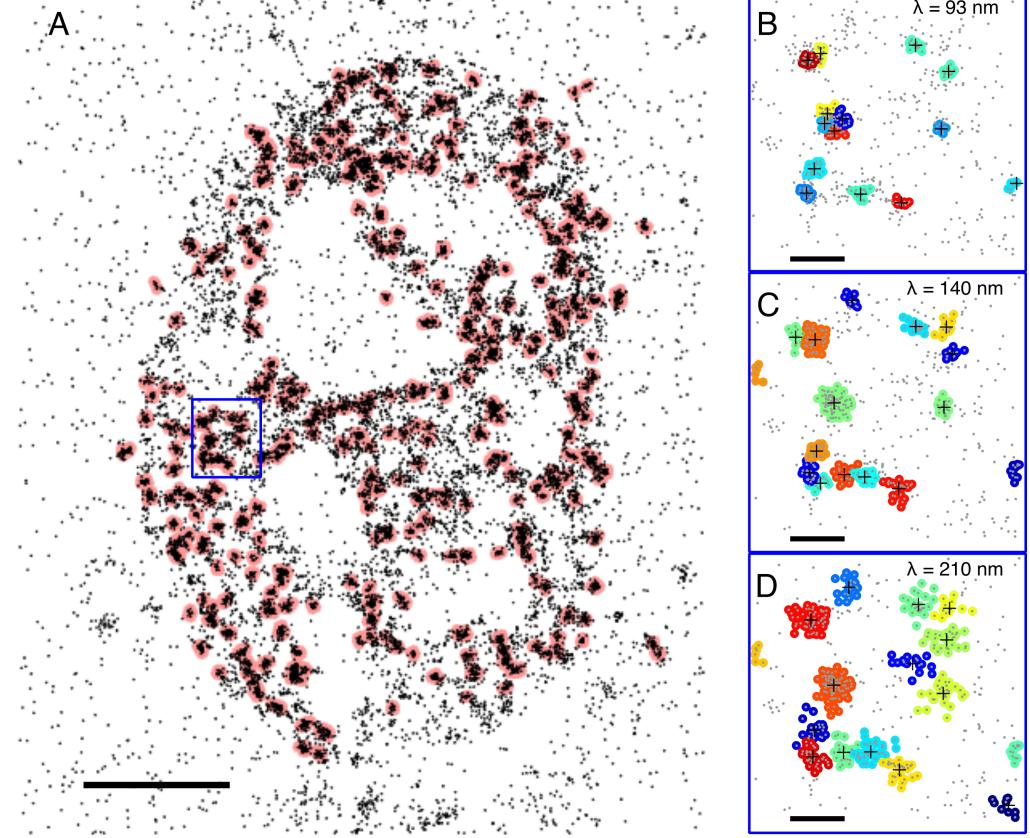
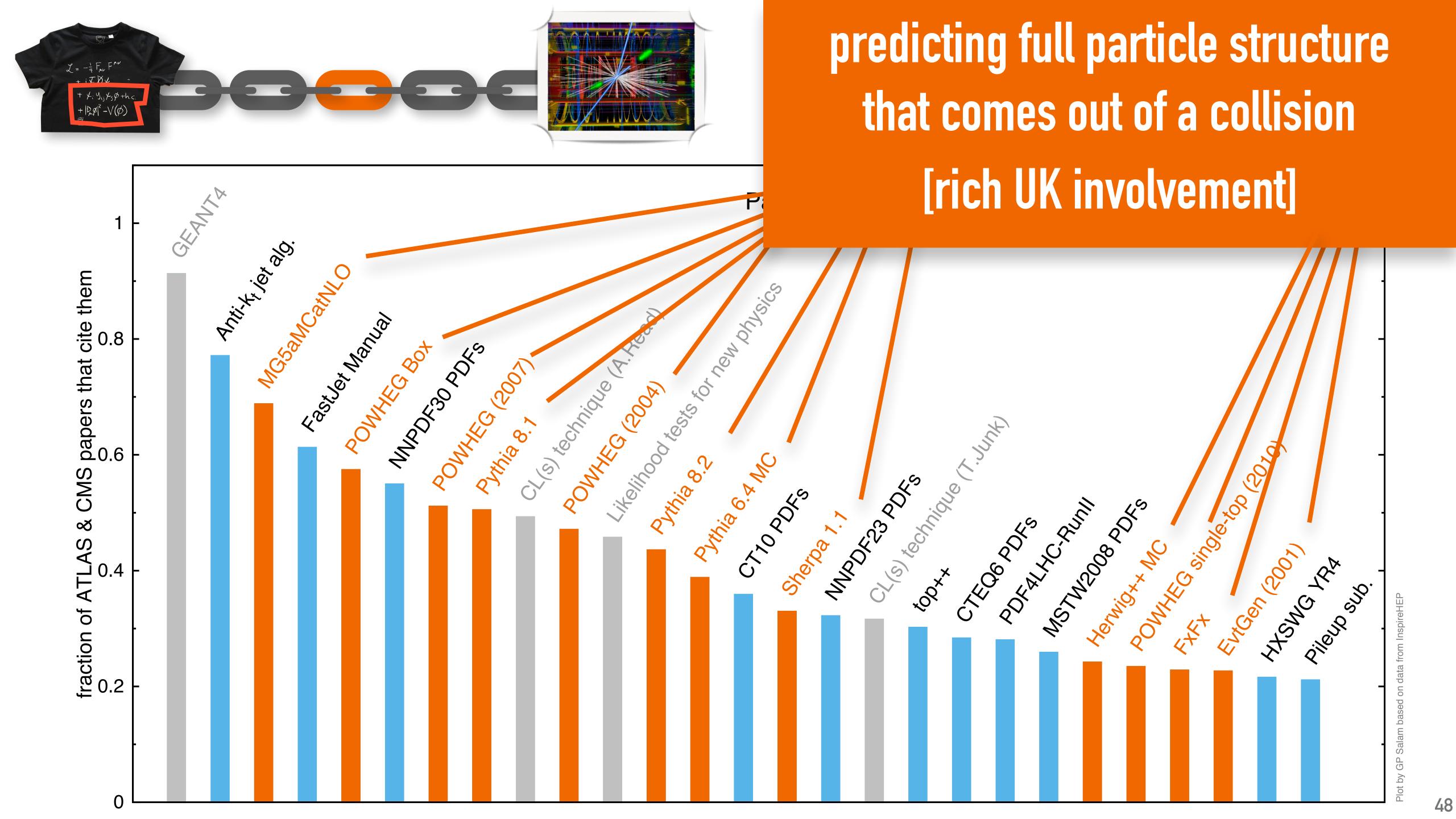
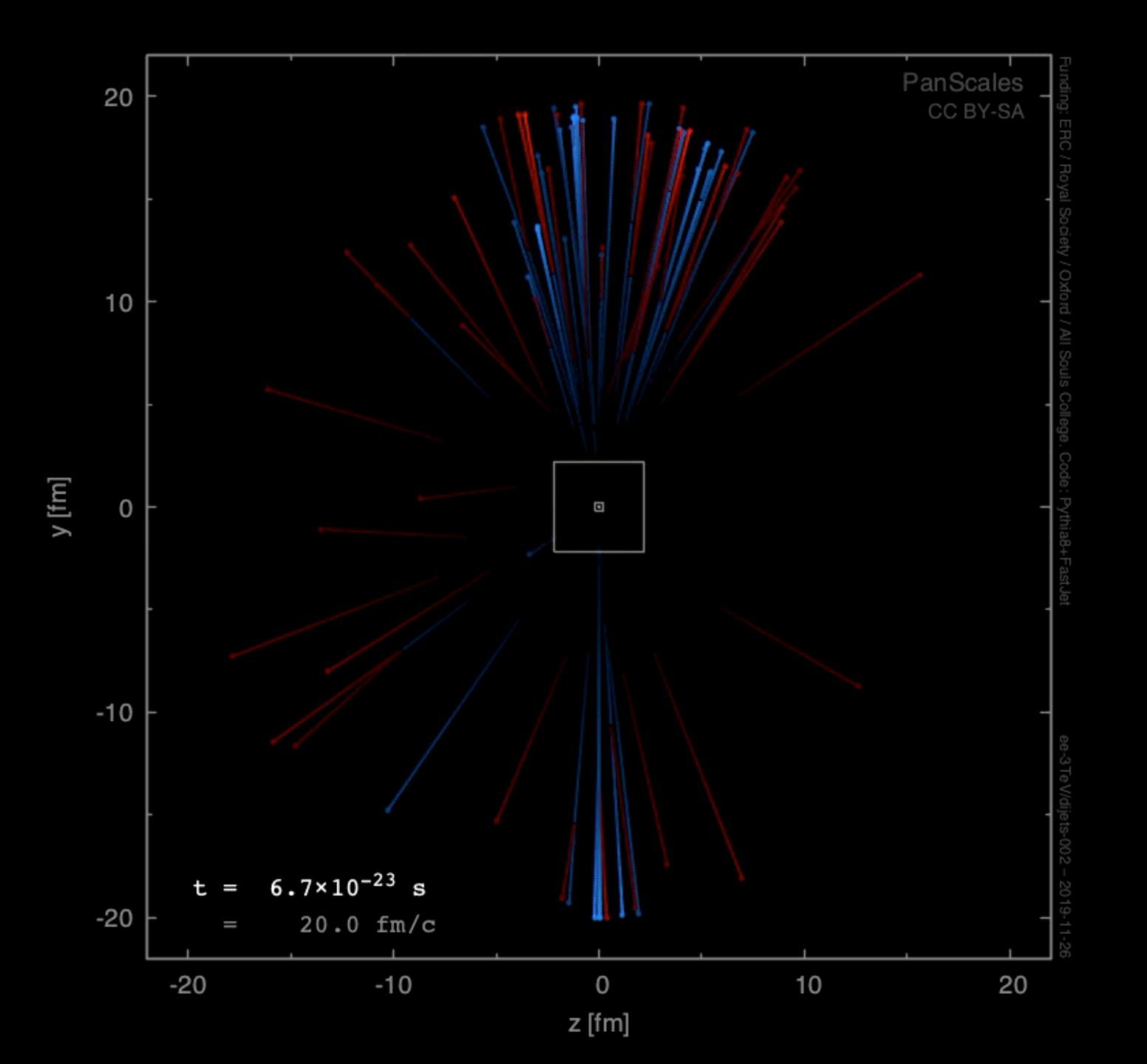


Figure S6: FastJet hierarchical clustering. (A) FastJet clusters found with a length scale of 140nm. (B-D) Zoomed in view of the region in the blue box from A. The clusters were generated by cutting the tree with a length scale of 93 nm, 140 nm, and 210 nm respectively. The black + signs mark the centroids of each cluster. Scale Bars – A: 5 µm B - D: 500 nm



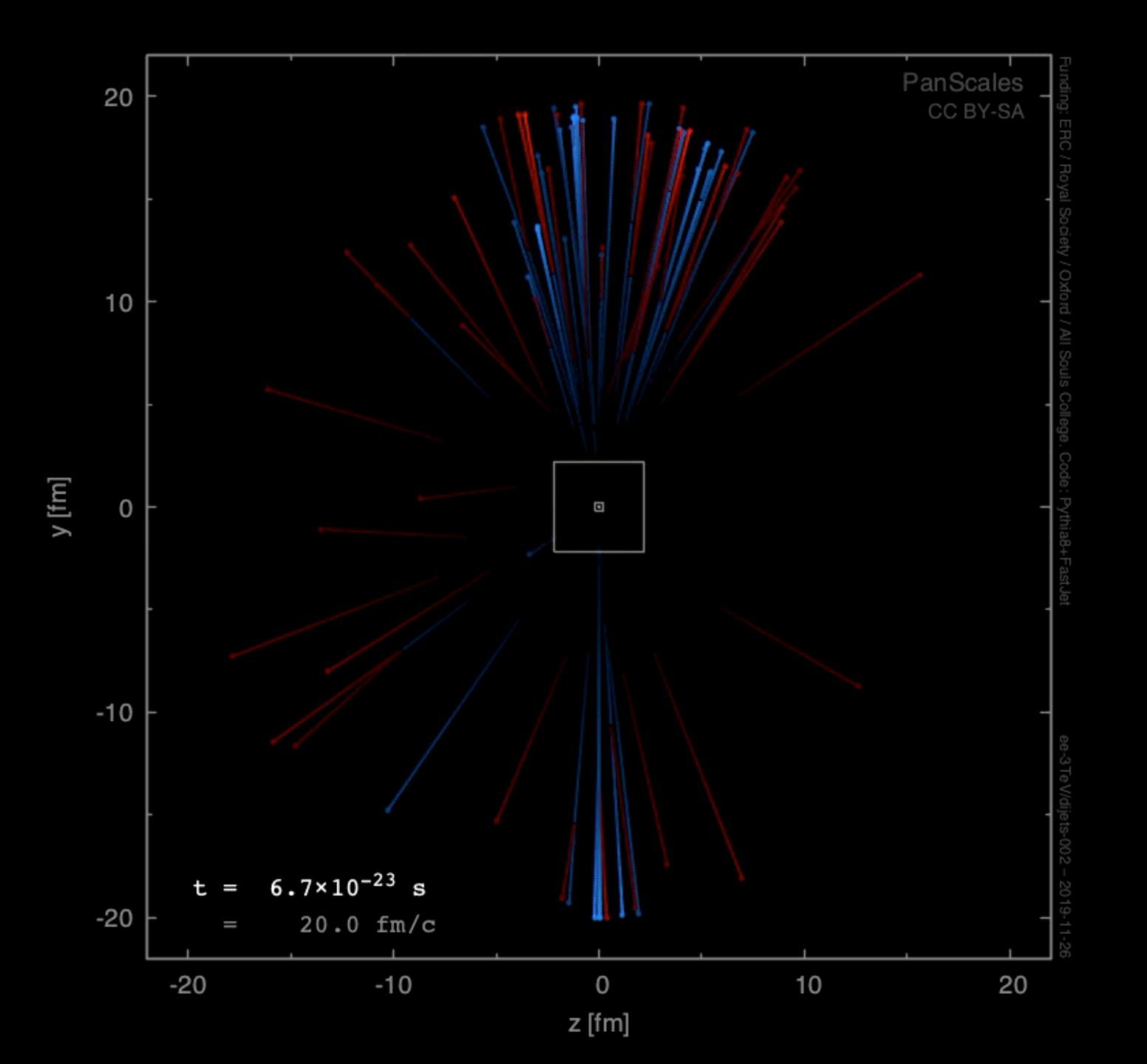


incoming beam particle

intermediate particle

final particle

Event evolution spans 7 orders of magnitude in space-time



incoming beam particle

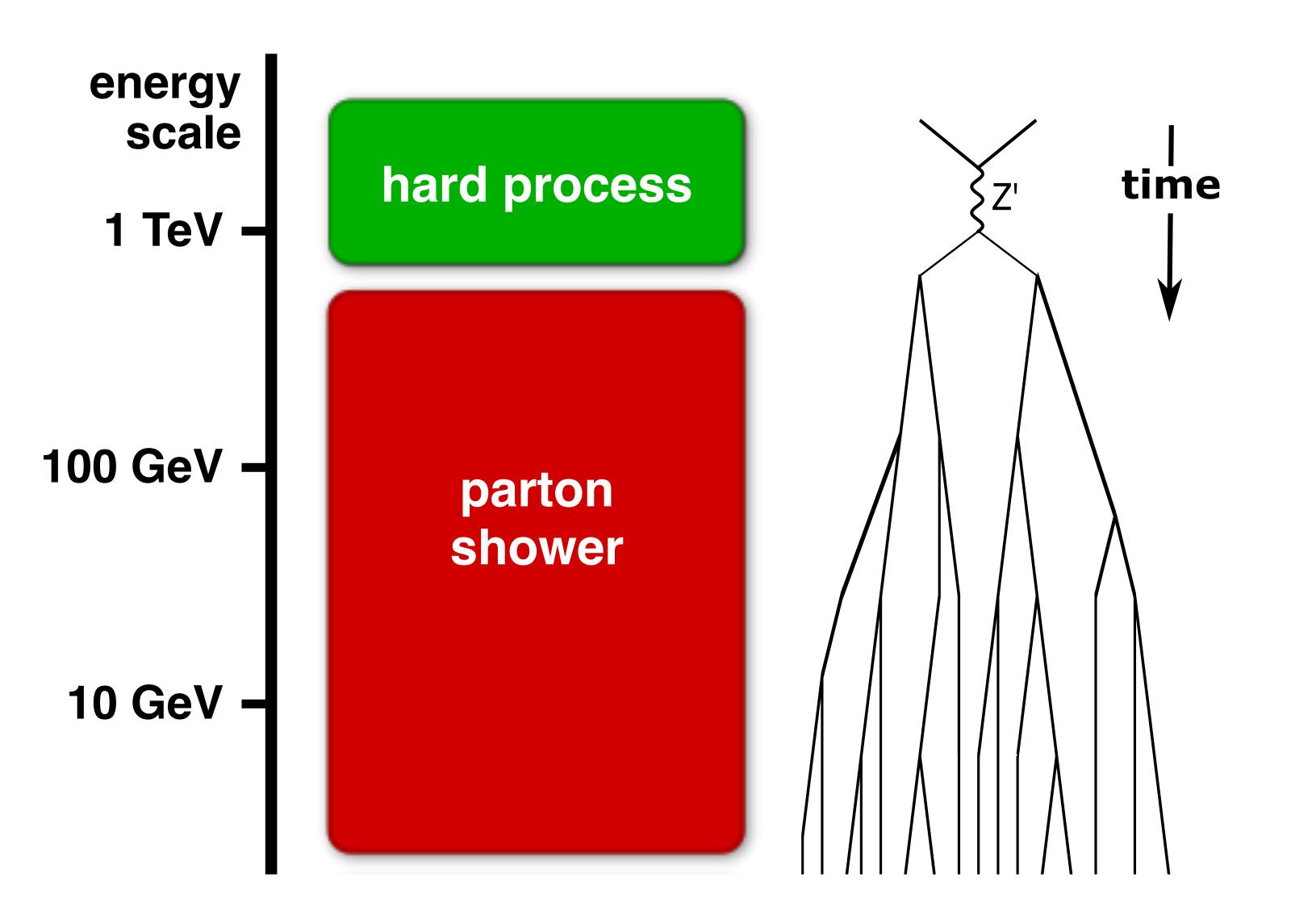
intermediate particle

final particle

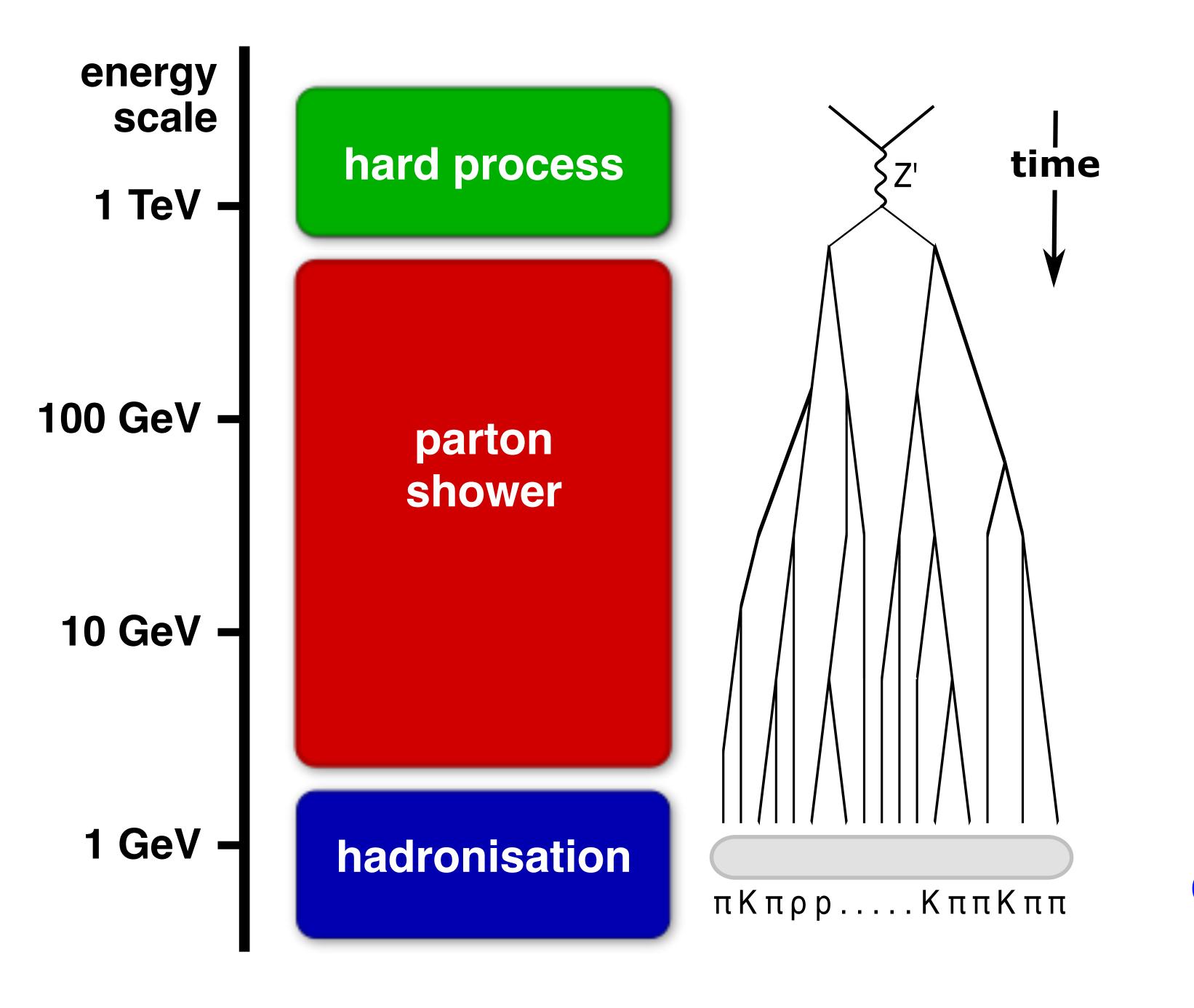
Event evolution spans 7 orders of magnitude in space-time



schematic view of key components of QCD predictions and Monte Carlo event simulation



schematic view of key components of QCD predictions and Monte Carlo event simulation



schematic view of key components of QCD predictions and Monte Carlo event simulation

pattern of particles in MC can be directly compared to pattern in experiment

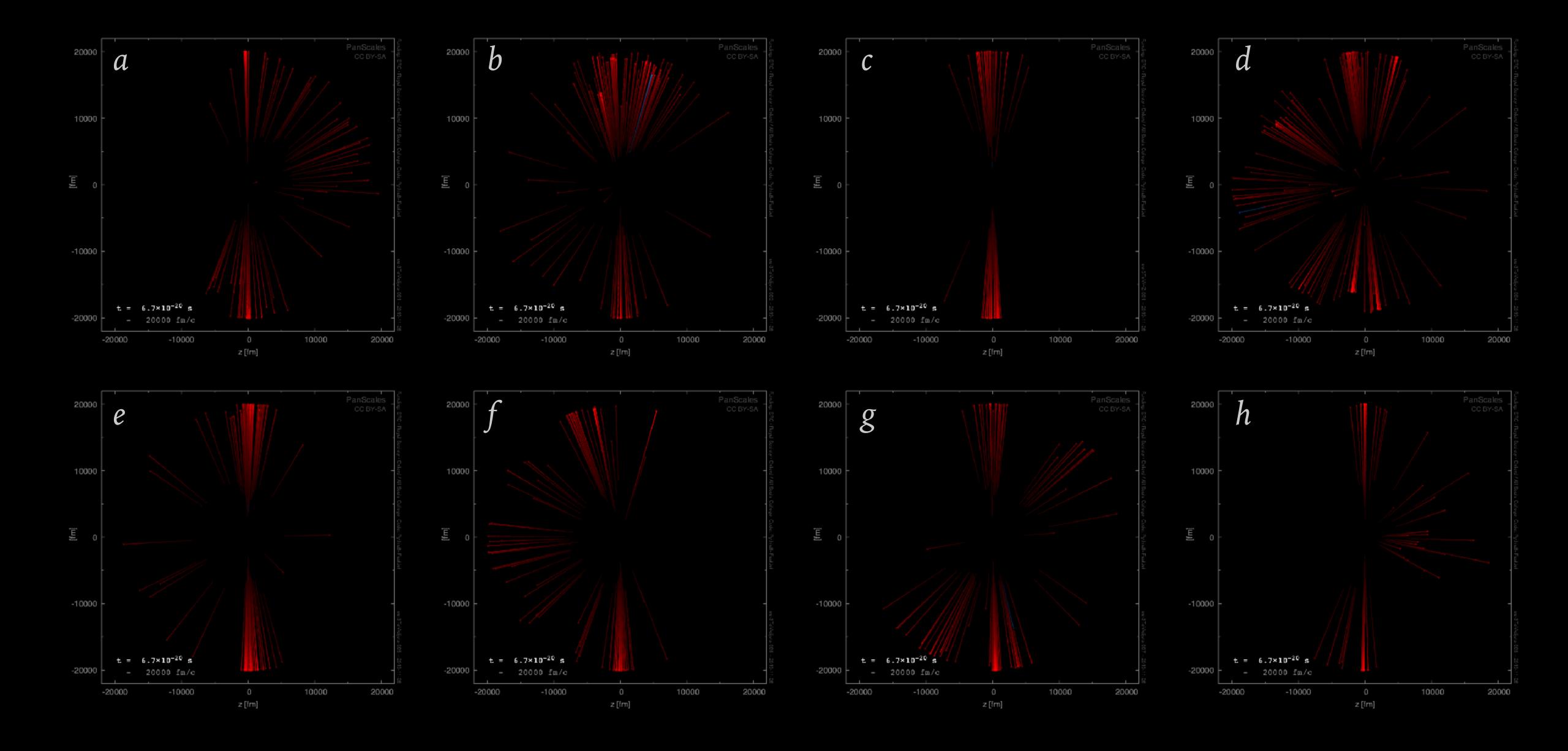
general purpose Monte Carlo event generators: THE BIG 3

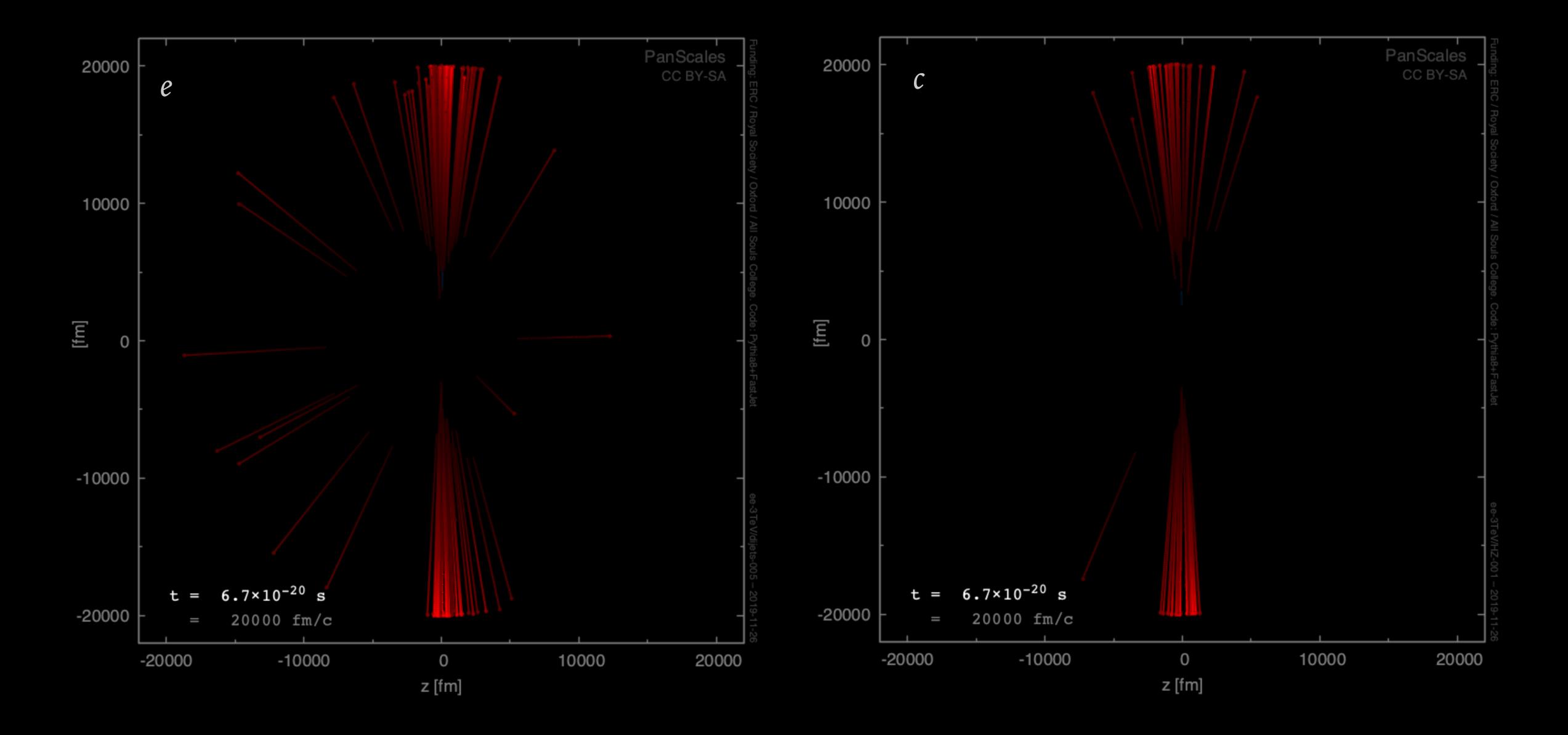


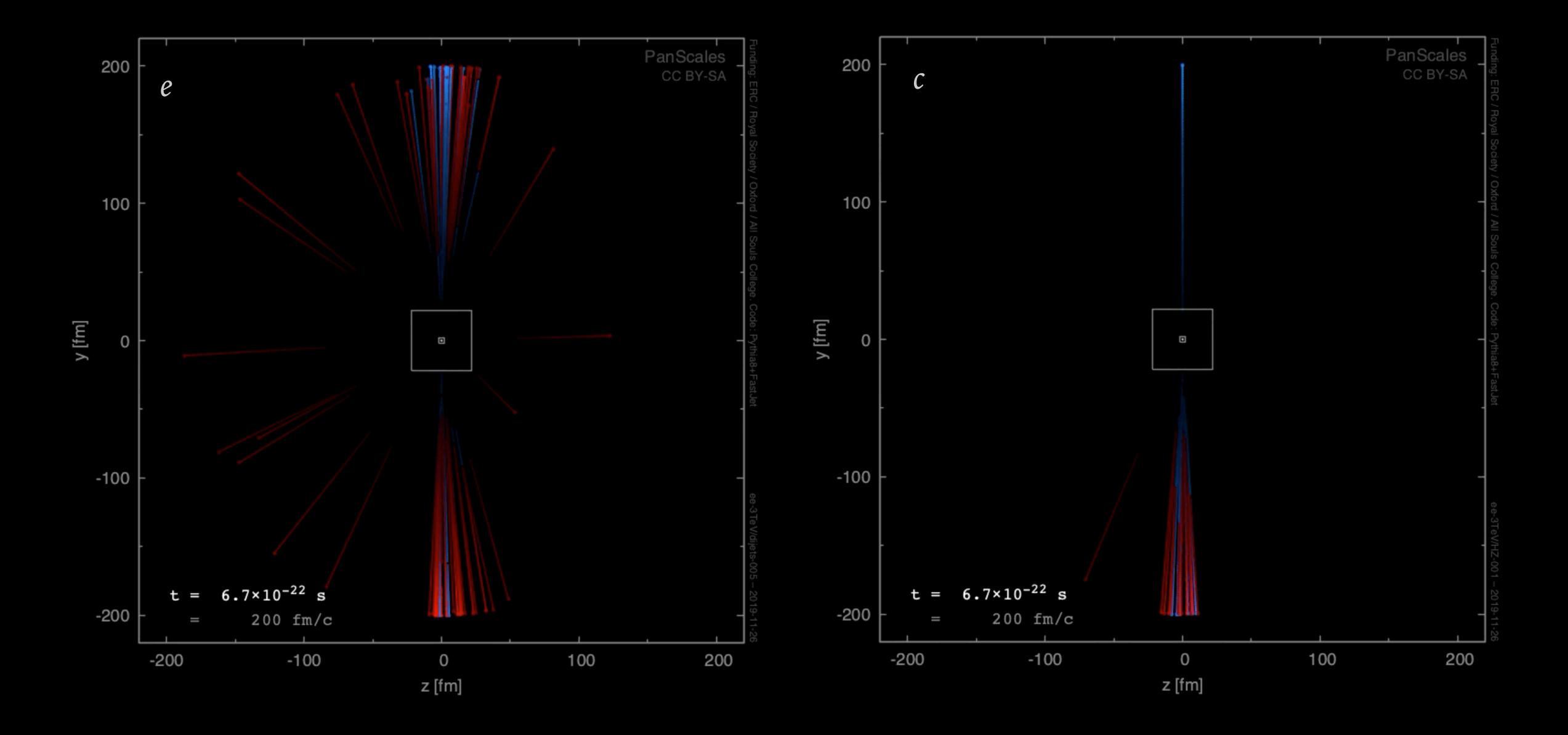
they do an amazing job of simulation vast swathes of data; collider physics would be unrecognisable without them

using full event information

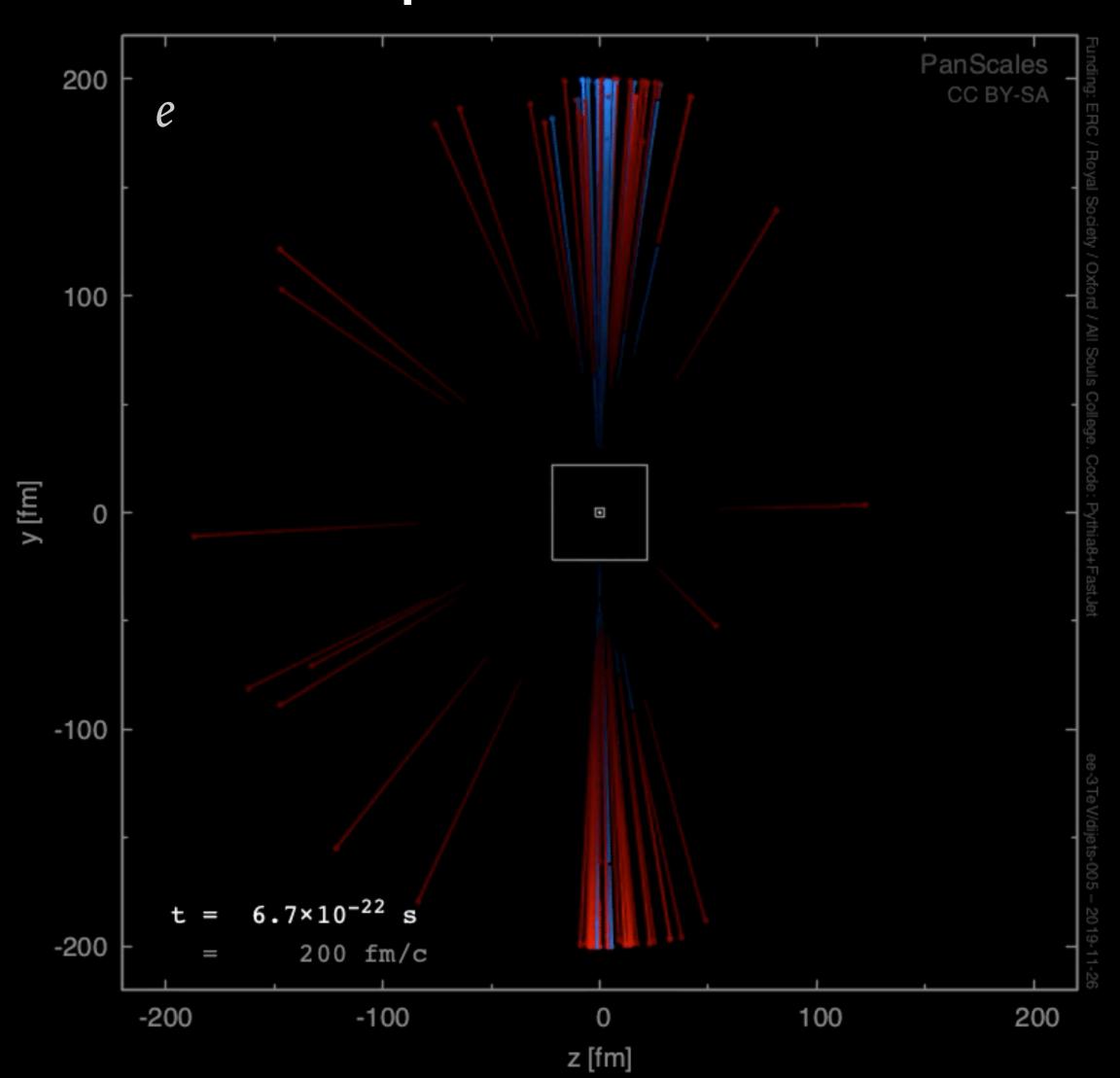
how much information is hidden among the hundreds of particles produced in a collisions?



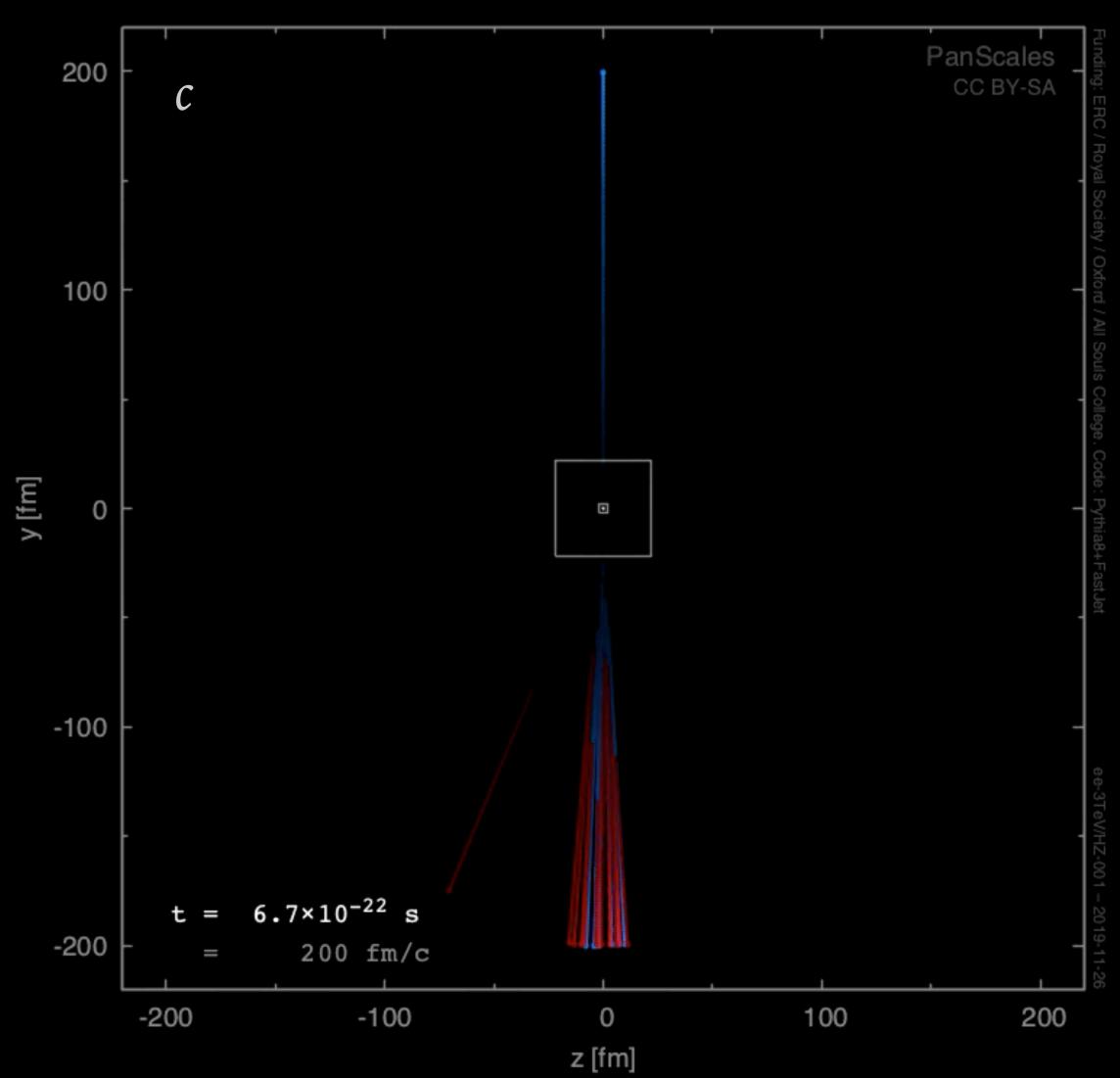




pure QCD event



event with Higgs & Z boson decays



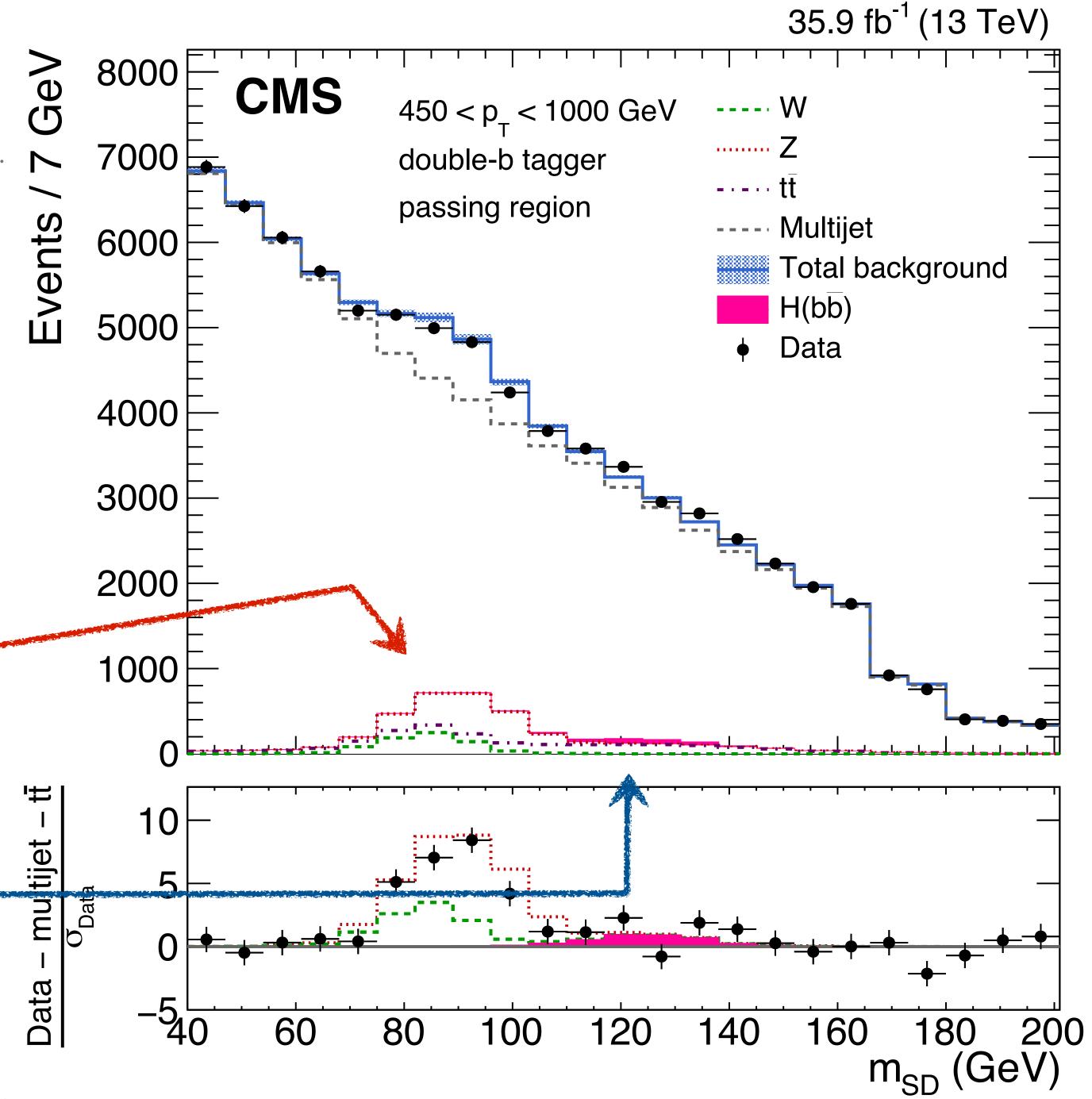
high pt Higgs & [SD] jet mass

We wouldn't trust electromagnetism if we'd only tested at one length/momentum scale.

New Higgs interactions need testing at both low and (here) high momenta.

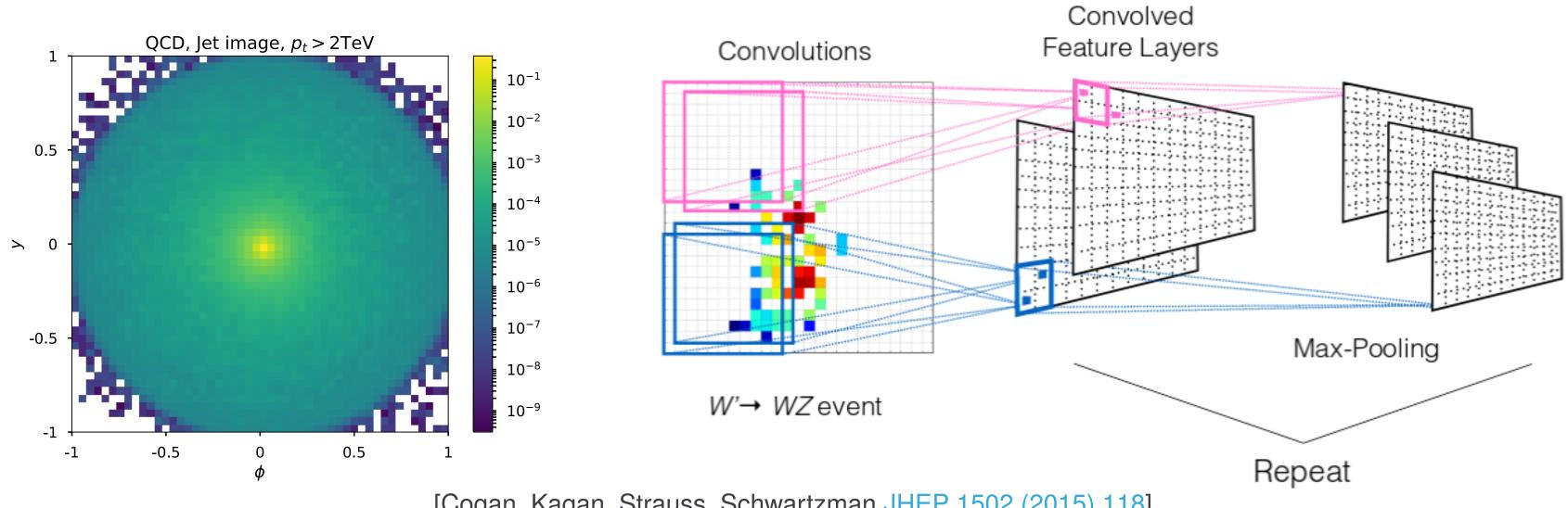
high- $p_T Z \rightarrow bb (5\sigma)$

high-p_T H \rightarrow bb ($\sim 1\sigma$)



Convolutional neural networks and jet images

- Project a jet onto a fixed $n \times n$ pixel image in rapidity-azimuth, where each pixel intensity corresponds to the momentum of particles in that cell.
- Can be used as input for classification methods used in computer vision, such as deep convolutional neural networks.



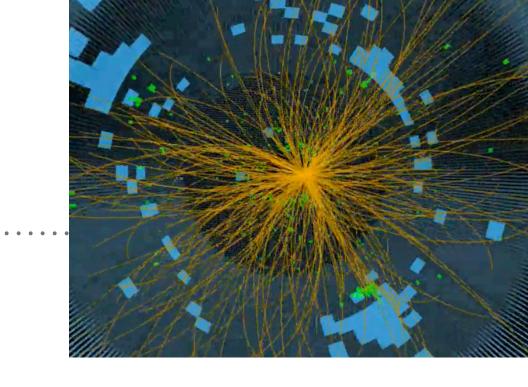
powerful

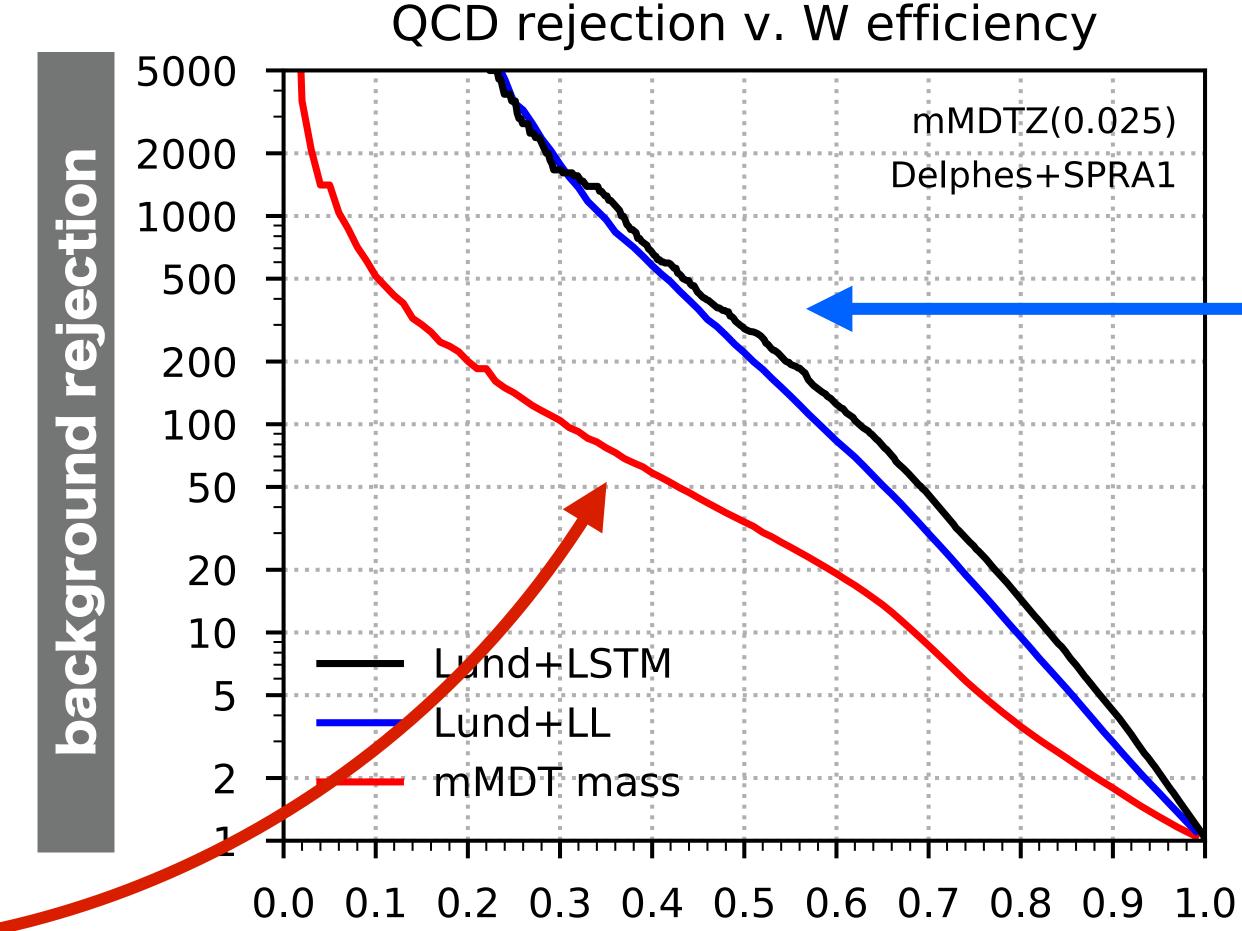
but black box

[Cogan, Kagan, Strauss, Schwartzman JHEP 1502 (2015) 118]
[de Oliveira, Kagan, Mackey, Nachman, Schwartzman JHEP 1607 (2016) 069]

Frédéric Dreyer 11/42

using full event information for H/etc. boson tagging





signal efficiency

QCD rejection with use of full jet substructure (2018 tools)

5–10x better

First started to be exploited by Thaler & Van Tilburg with "N-subjettiness" (2010/11)

QCD rejection with just jet mass (SD/mMDT)i.e. 2008 tools & their 2013/14 descendants

from Dreyer, GPS & Soyez 2018 60

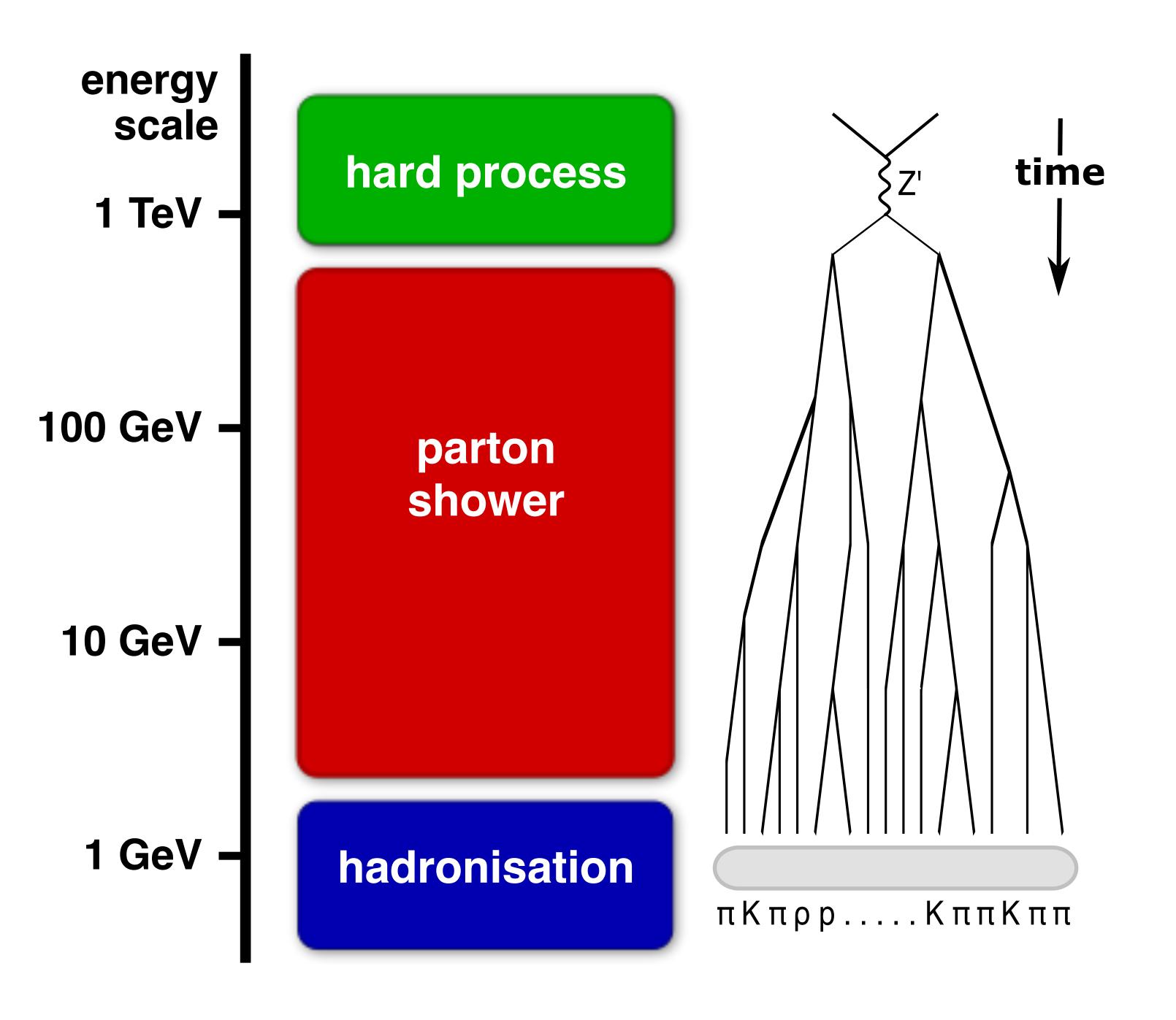
can we trust machine learning? A question of confidence in the training...



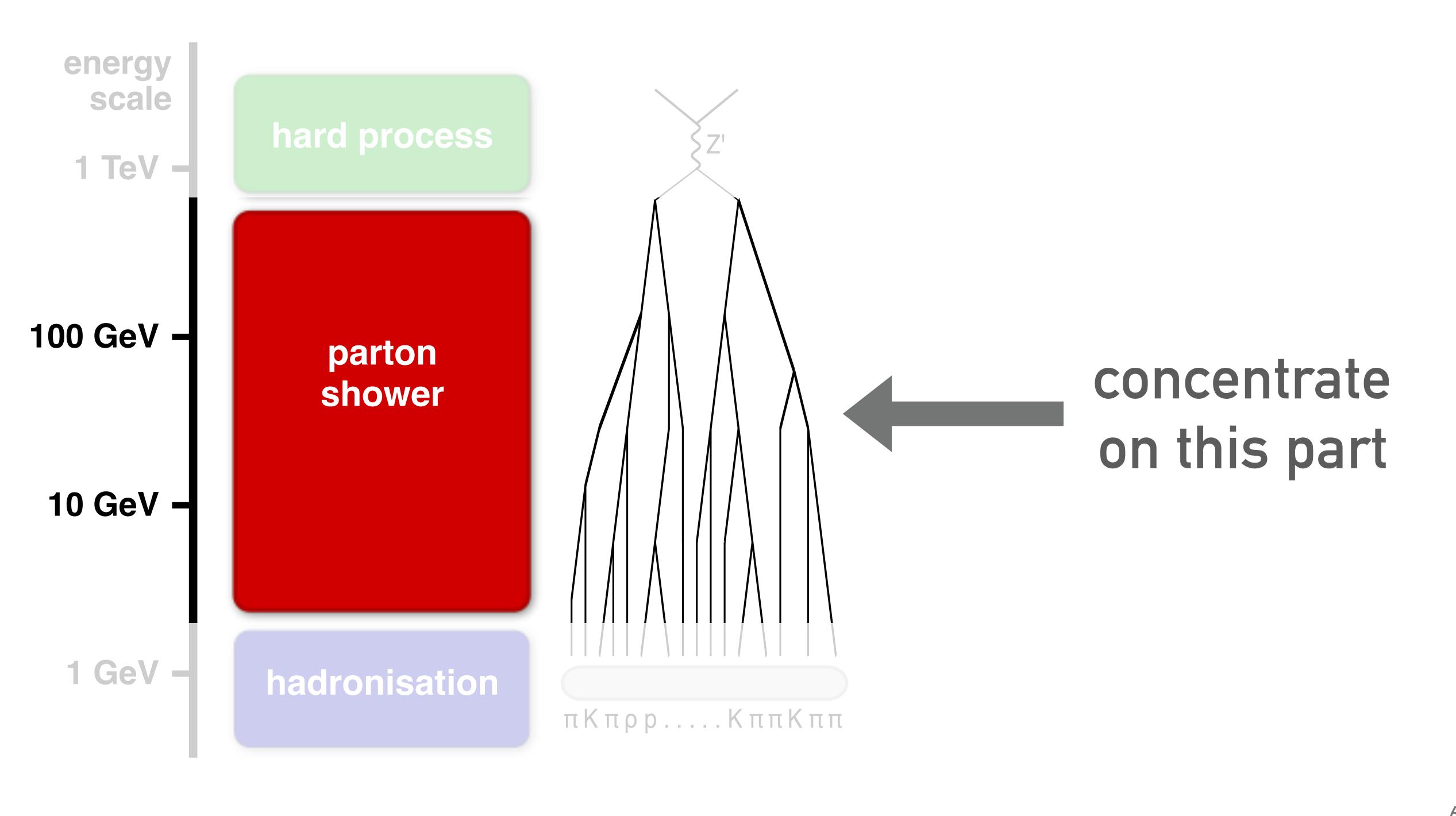
Unless you are highly confident in the information you have about the markets, you may be better off ignoring it altogether

- Harry Markowitz (1990 Nobel Prize in Economics)

[via S Gukov]



machine-learning gets trained on QCD simulations



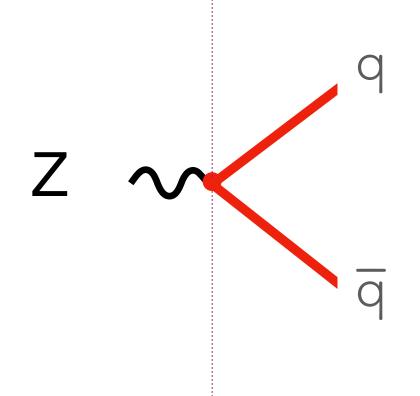
A parton shower, at its simplest

$$\sum_{n=0}^{\infty} \prod_{i=1}^{n} \left(\left\langle + \right\rangle \right) = \cdots$$

iteration of $2\rightarrow 3$ (or $1\rightarrow 2$) splitting kernel

Start with q-qbar state.

Evolve a step in v and throw a random number to decide if state remains unchanged



V

$$\frac{dP_2(v)}{dv} = -f_{2\to 3}^{q\bar{q}}(v) P_2(v)$$

V

Start with q-qbar state.

Evolve a step in v and throw a random number to decide if state remains unchanged

$$\frac{dP_2(v)}{dv} = -f_{2\to 3}^{q\bar{q}}(v) P_2(v)$$

V0

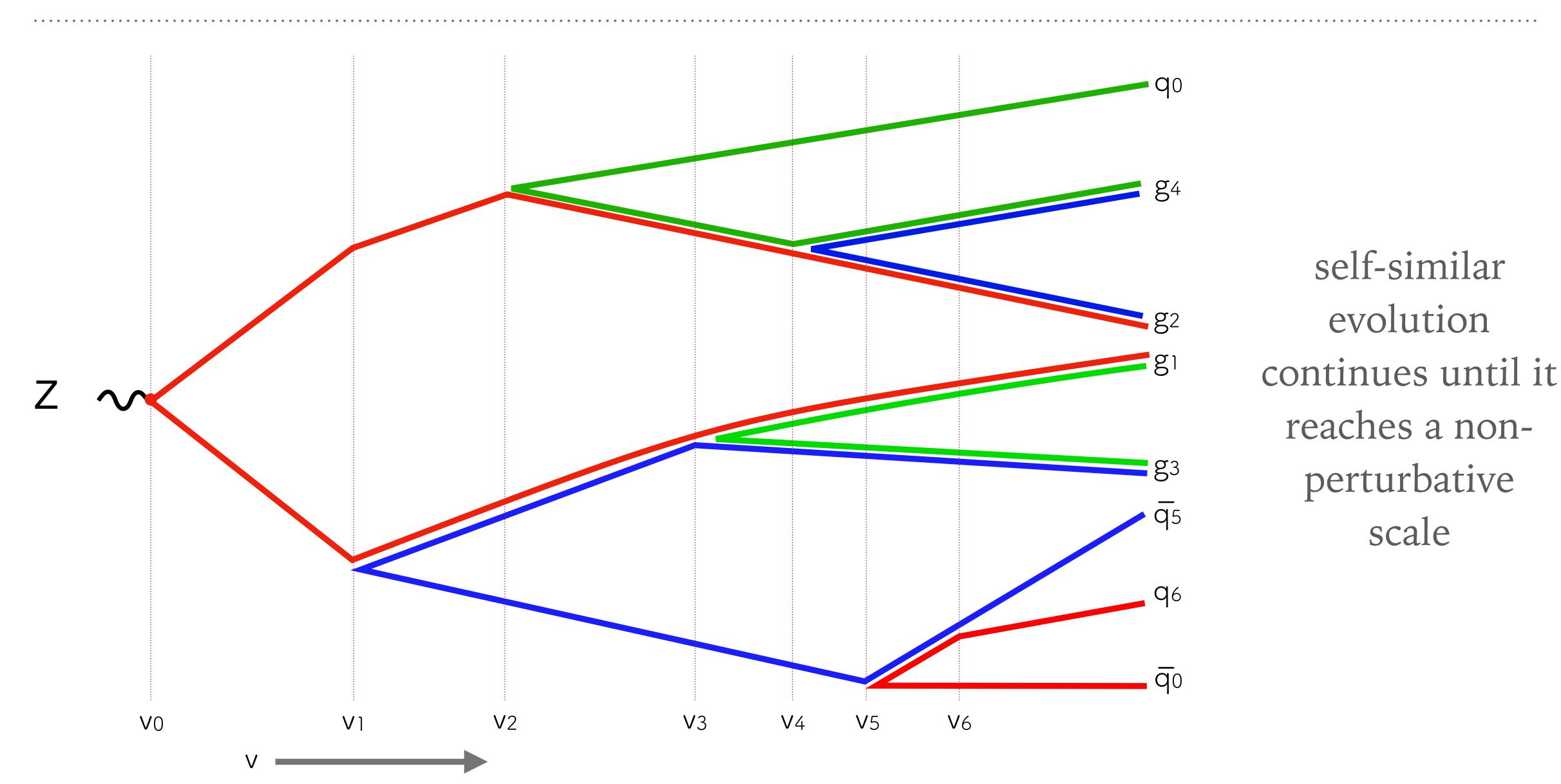
Start with q-qbar state.

Evolve a step in v and throw a random number to decide if state remains unchanged

At some point, rand.numb. is such that **state splits** $(2\rightarrow 3$, i.e. emits gluon). Evolution equation changes

$$\frac{dP_3(v)}{dv} = -\left[f_{2\to 3}^{qg}(v) + f_{2\to 3}^{g\bar{q}}(v)\right] P_3(v)$$

gluon is part of two dipoles $(qg, \bar{q}g)$



metric for "success" for parton showers?

- you can use it to predict anything:
 i.e. pattern of N-particle production for any N,
 there's no way of getting this right all the time
- ➤ we need to identify a criterion for "success" that is within reach lack of criterion → lack of clear guideline for parton shower development

Dipole showers

Dasgupta, Dreyer, Hamilton, Monni & GPS, 1805.09327 Dasgupta, Dreyer, Hamilton, Monni, GPS & Soyez (in progress) Nagy & Soper (a series of article since ~ 2008)

Angular-ordered showers:

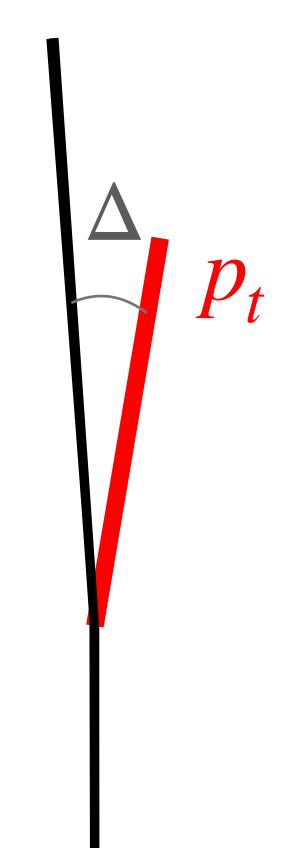
Banfi, Corcella, Dasgupta, hep-ph/0612282 Bewick, Ravasio-Ferrario, Richardson & Seymour 1904.11866

Gavin Salam 69

the "Lund plane"

one crucial element to build a metric of success for parton showers

Phase space: two key variables (+ azimuth)



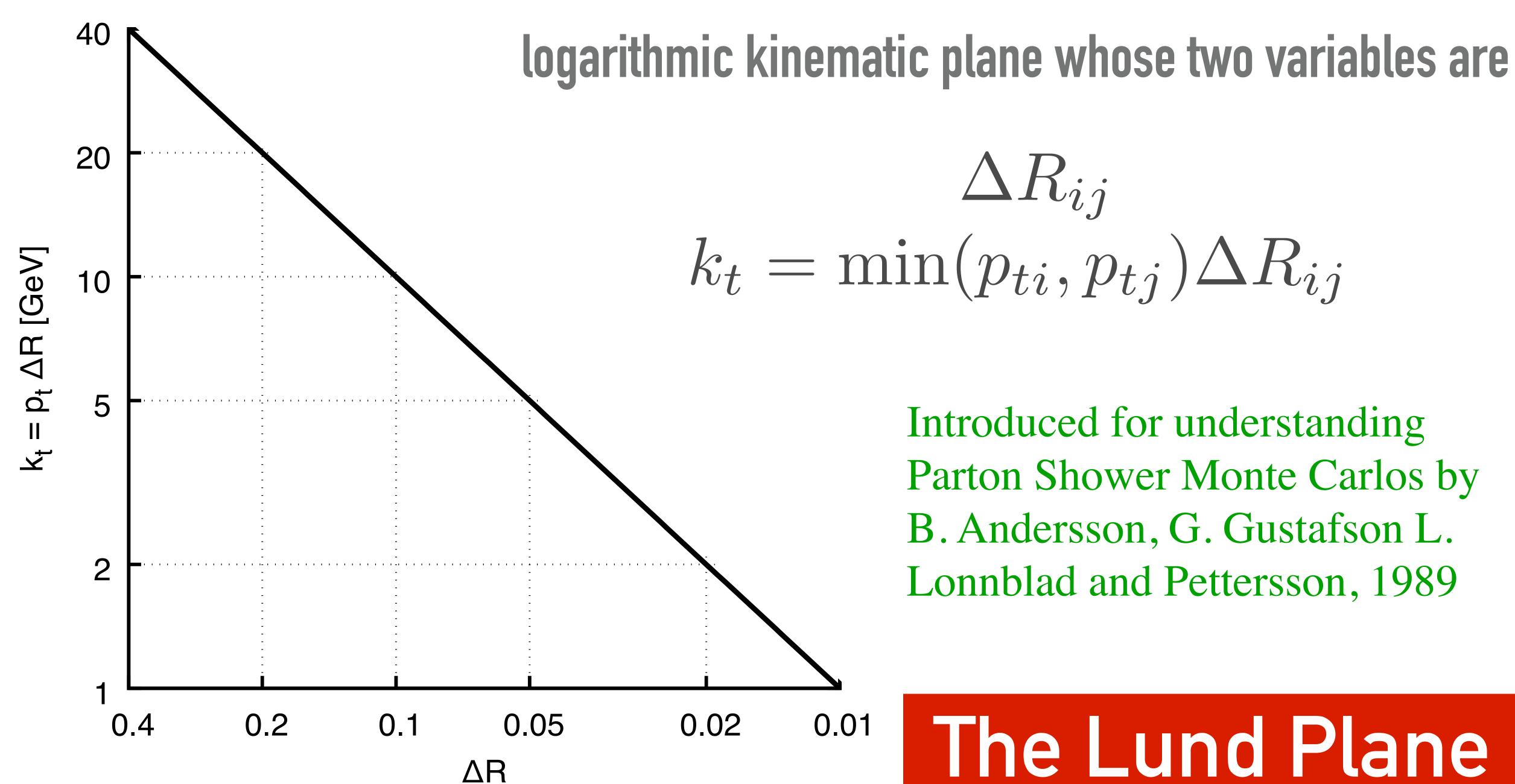
$$\Delta R$$
 (or just Δ)

$$k_t = p_t \Delta$$

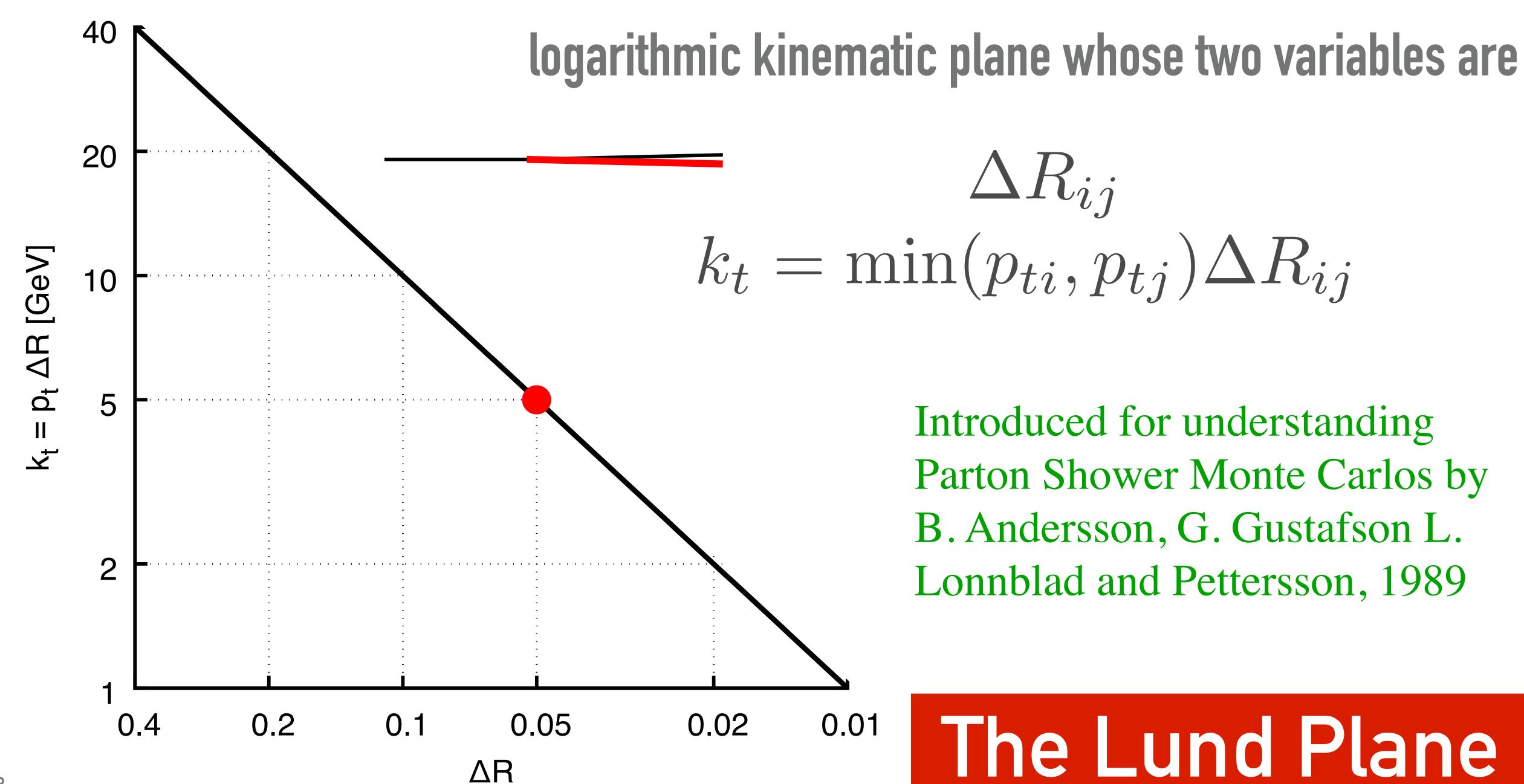
opening angle of a splitting

 p_t (or p_{\perp}) is transverse momentum wrt beam

 k_t is \sim transverse momentum wrt jet axis

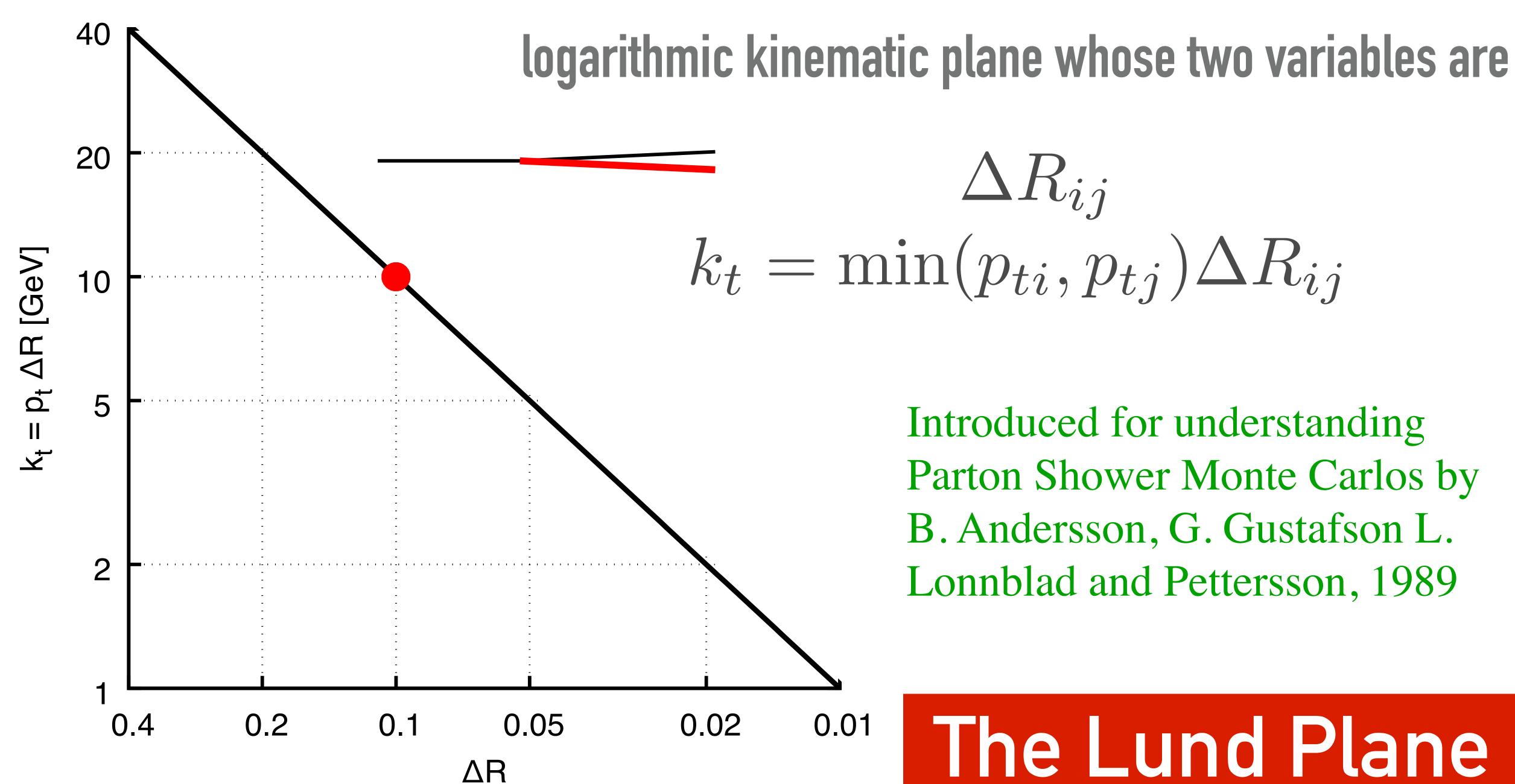


 ΔR_{ij}



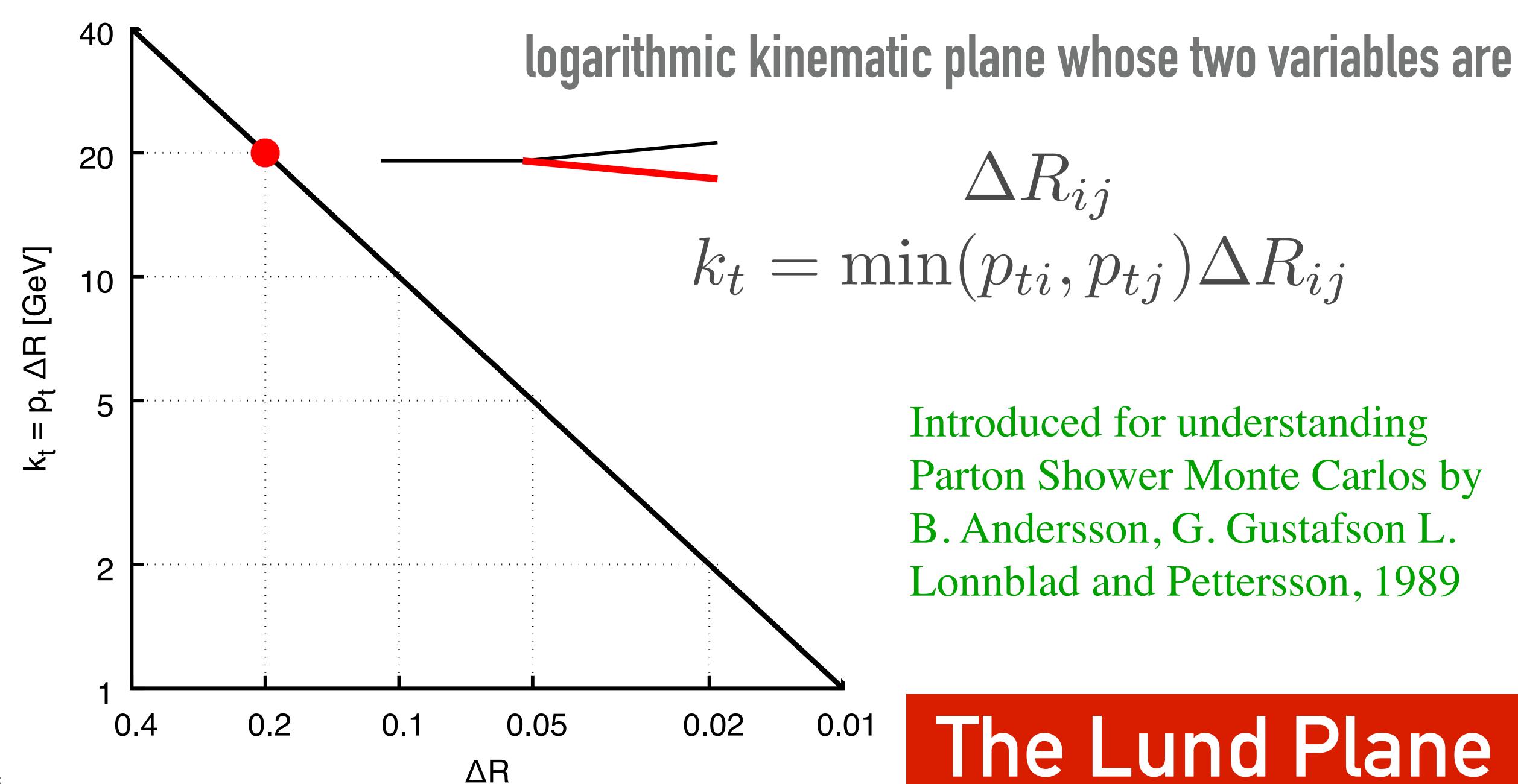
$k_t = \min(p_{ti}, p_{ti}) \Delta R_{ii}$ Introduced for understanding

 ΔR_{ij}

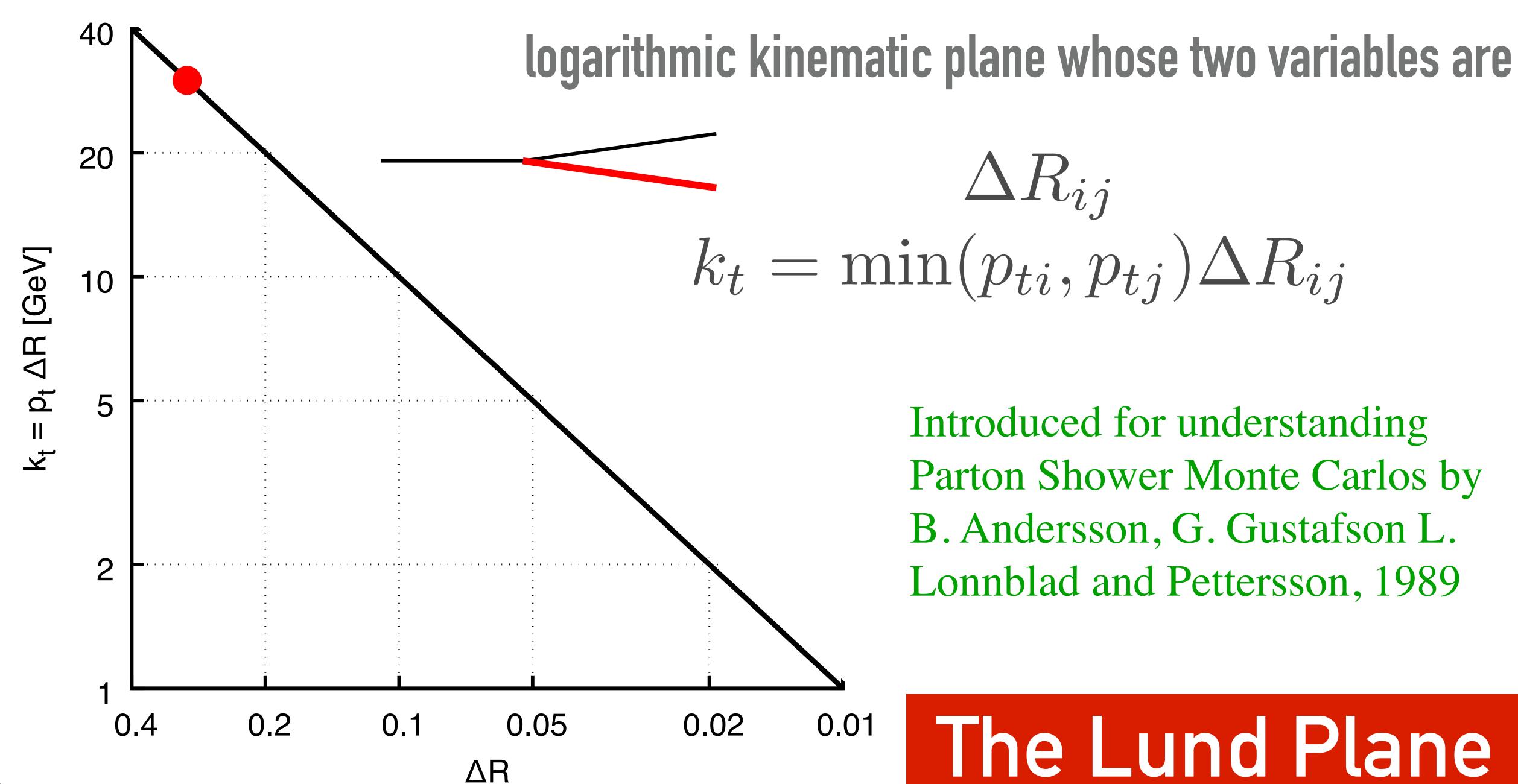


Introduced for understanding Parton Shower Monte Carlos by

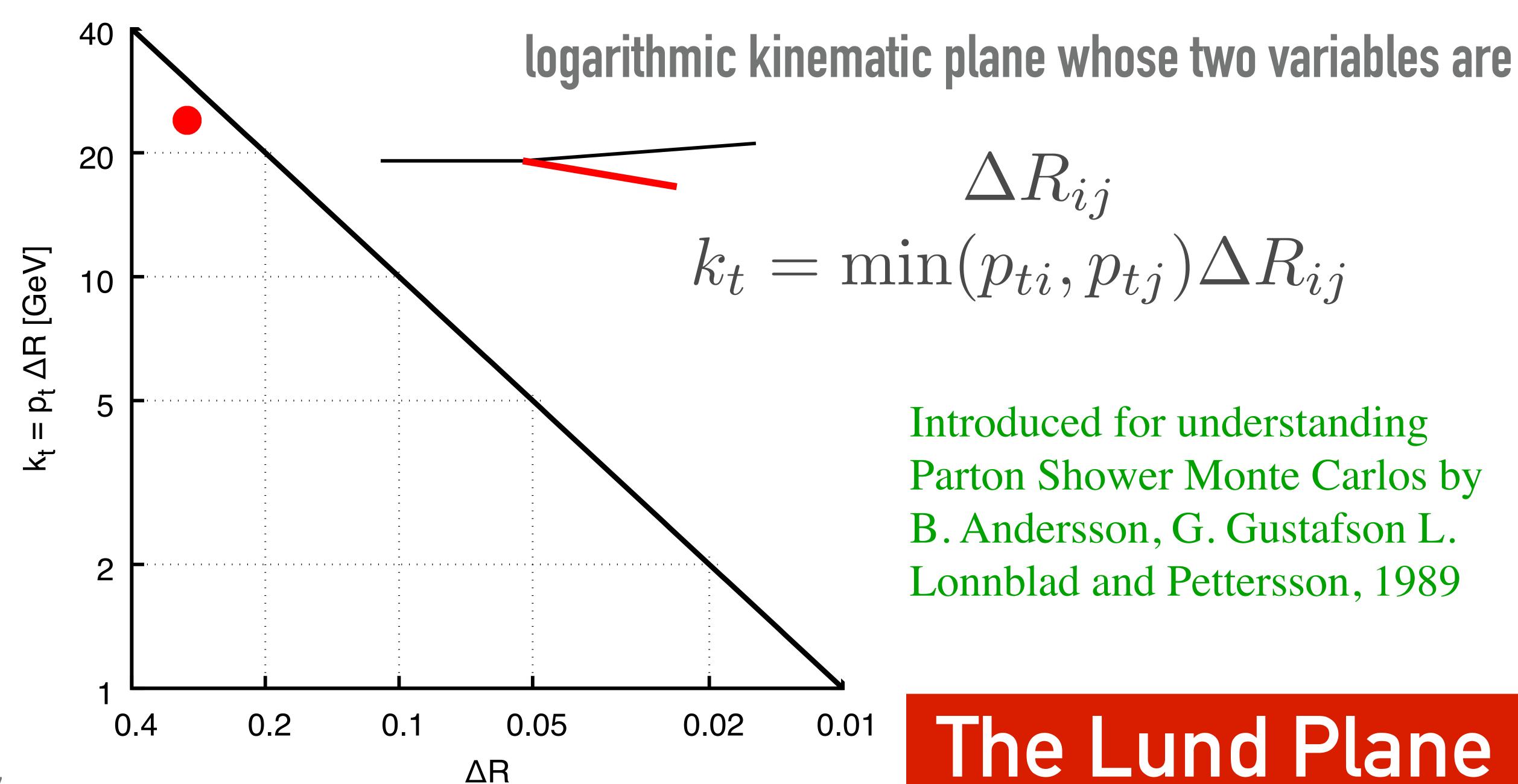
 ΔR_{ij}



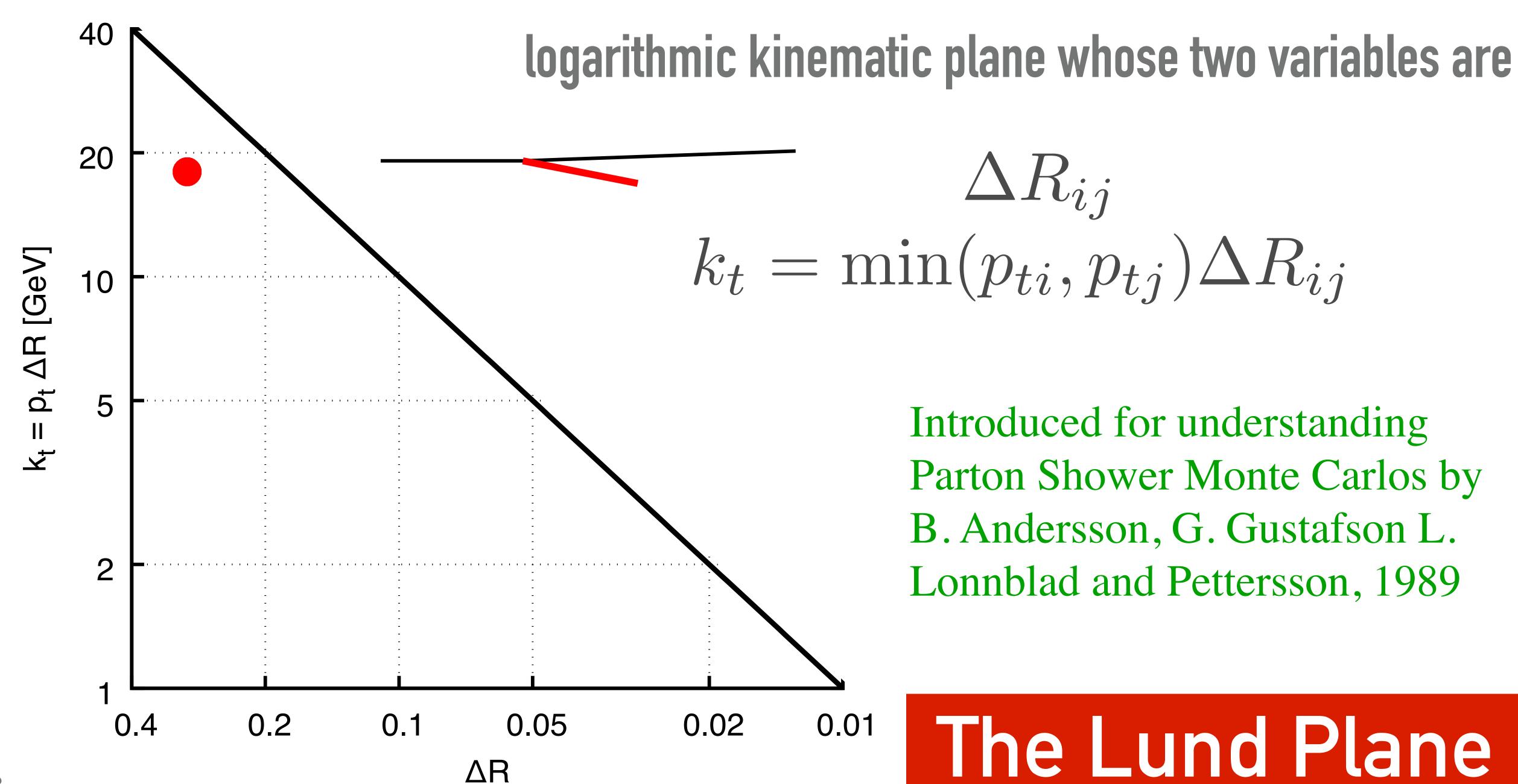
 ΔR_{ij}



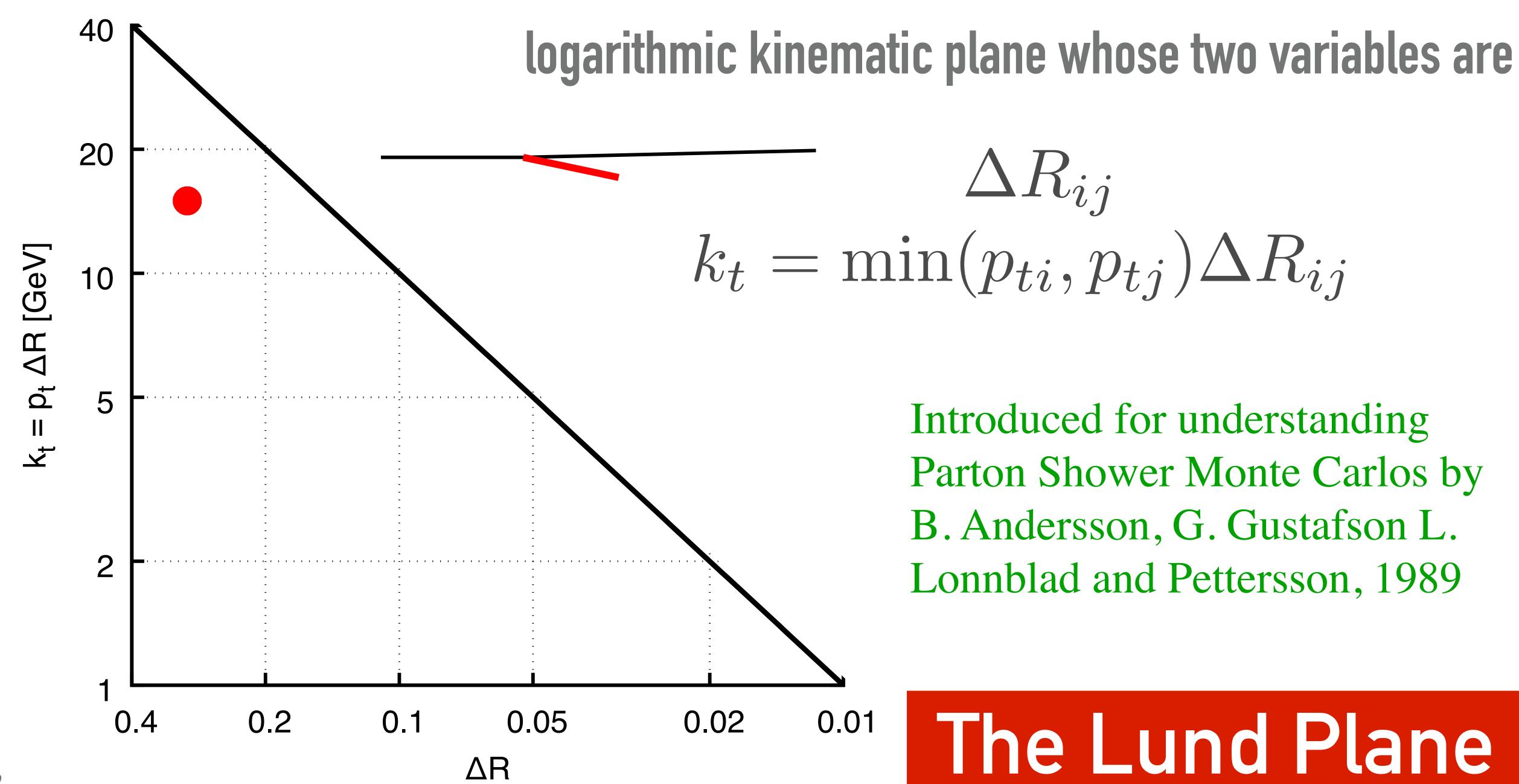
 ΔR_{ij}



 ΔR_{ij}

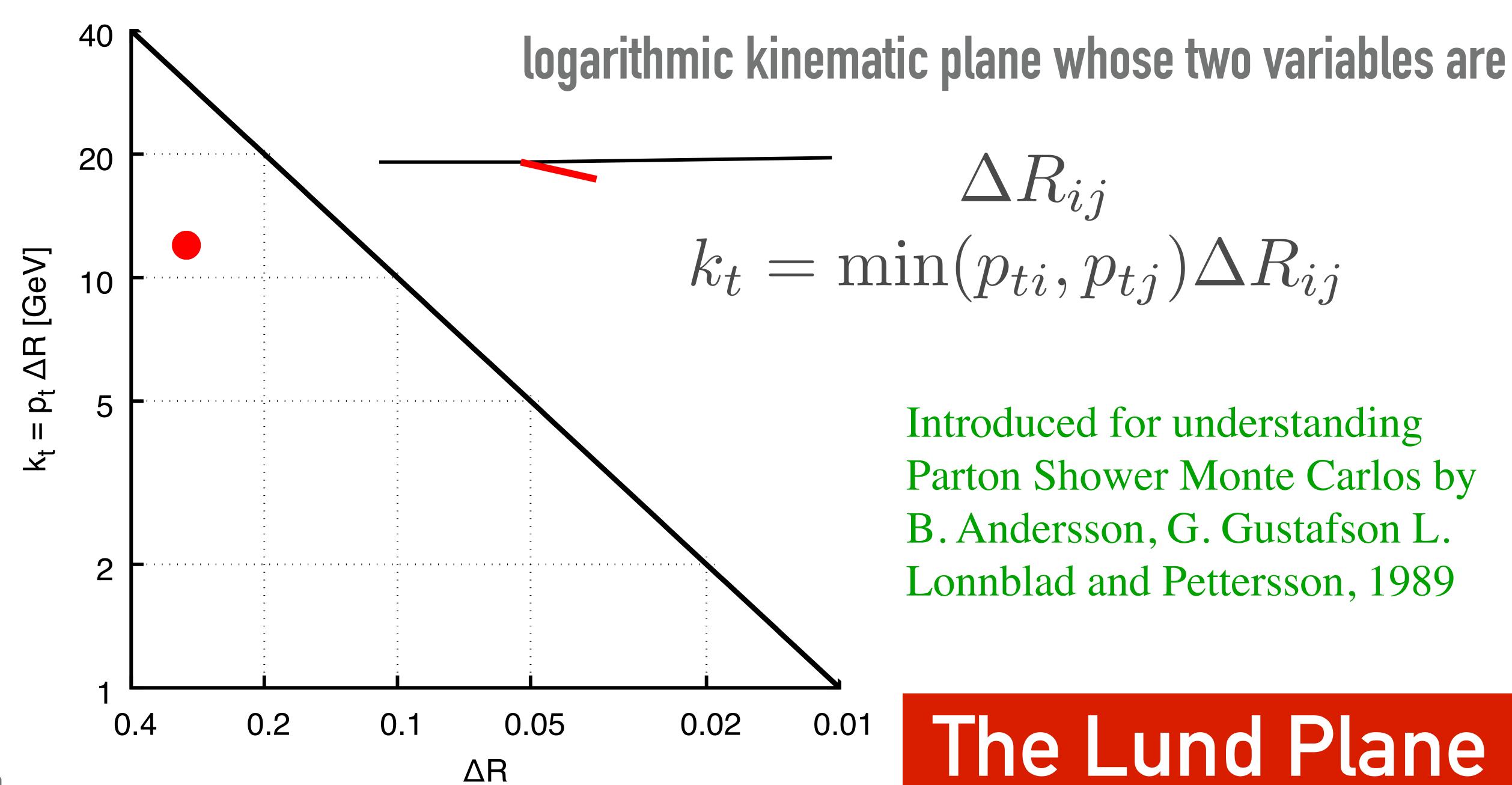


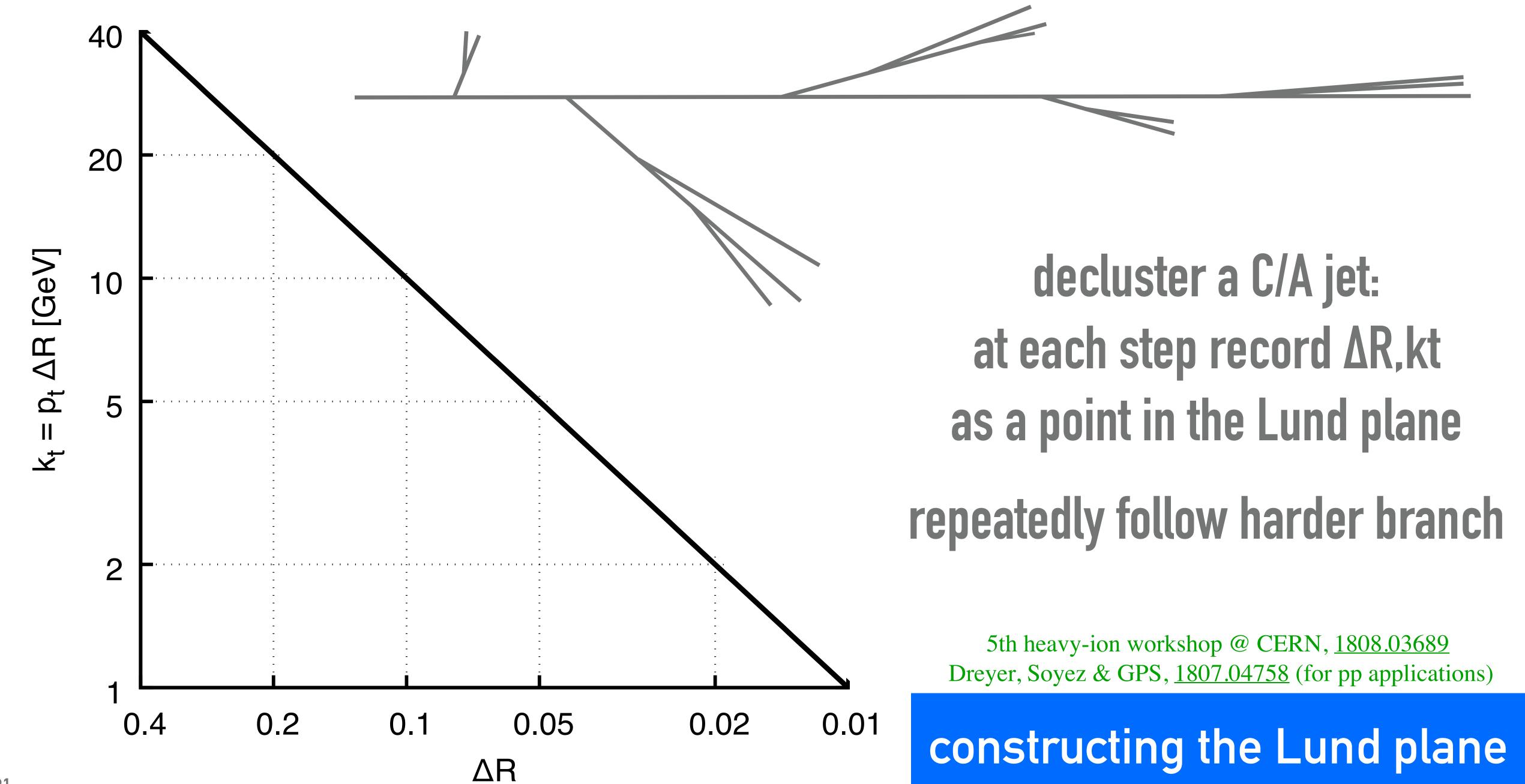
 ΔR_{ij}

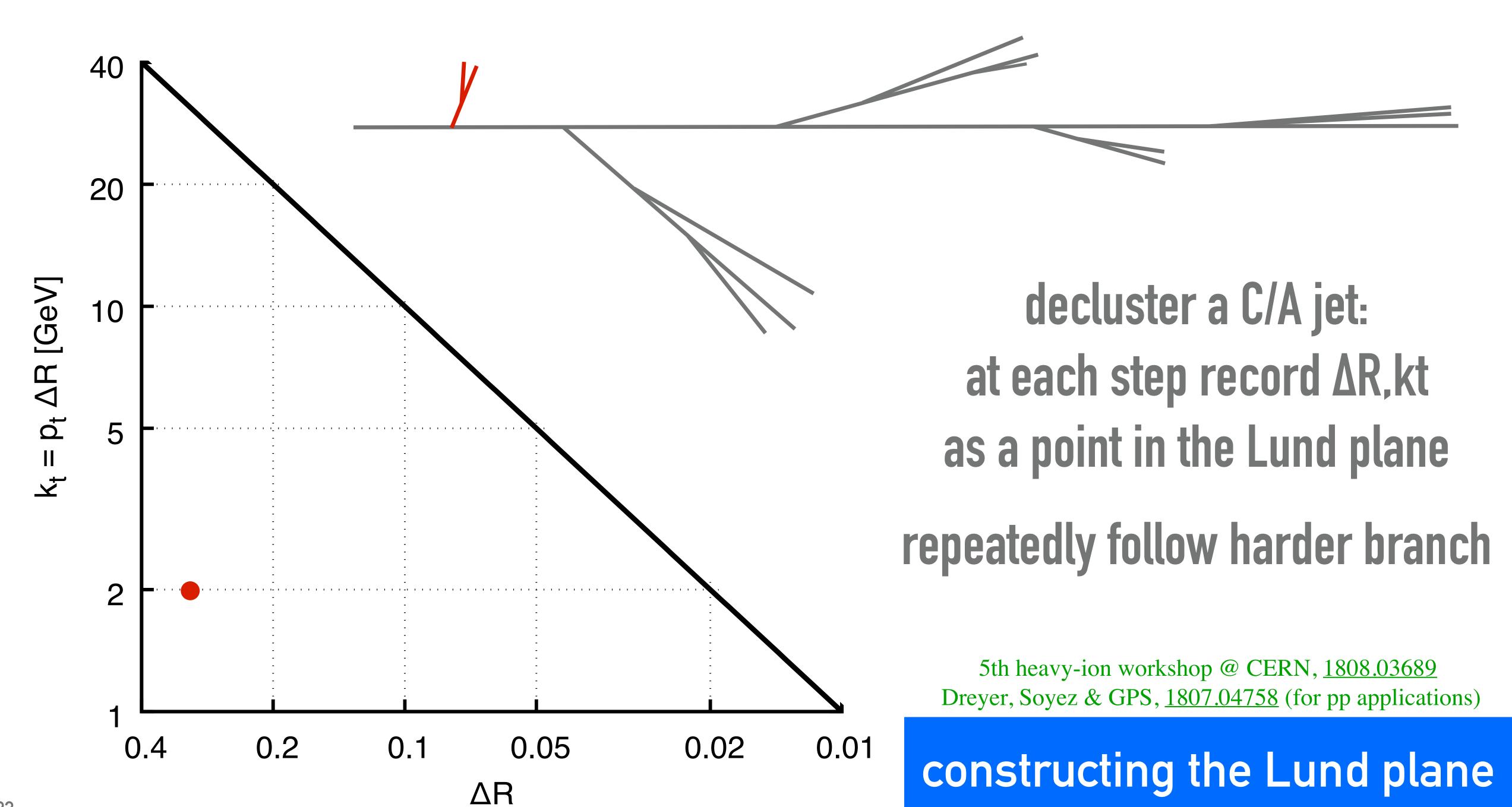


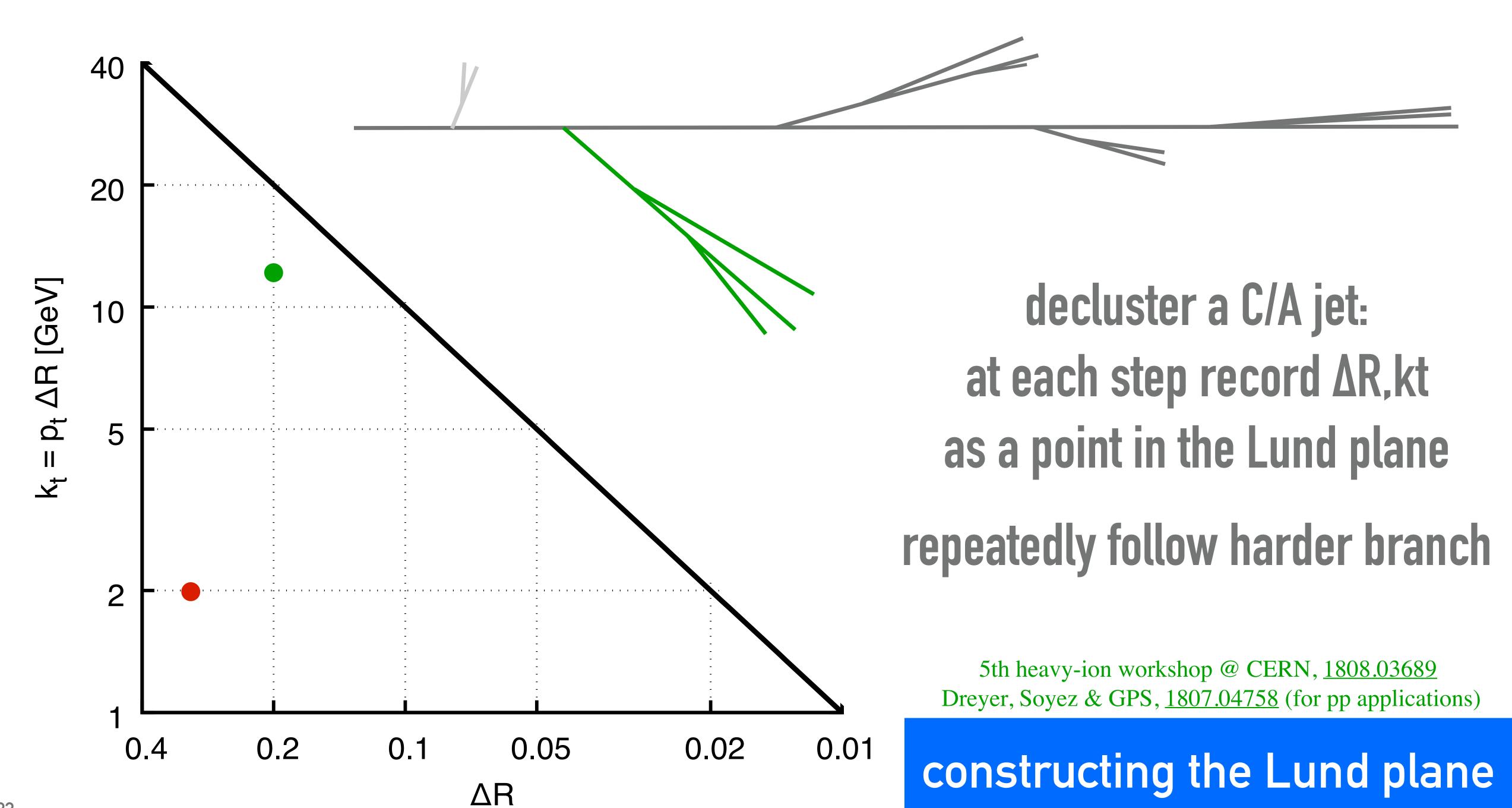
Introduced for understanding Parton Shower Monte Carlos by

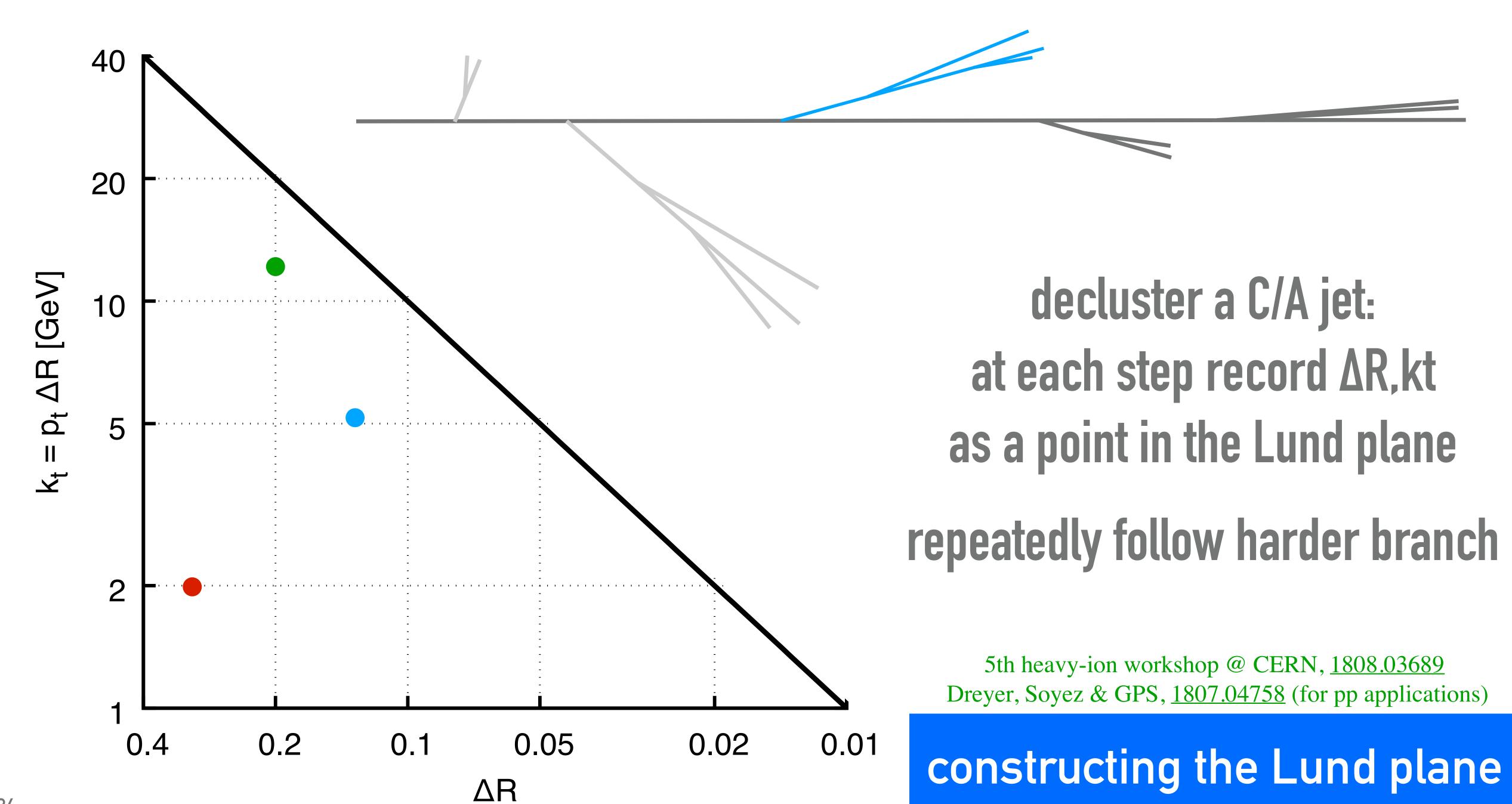
 ΔR_{ij}

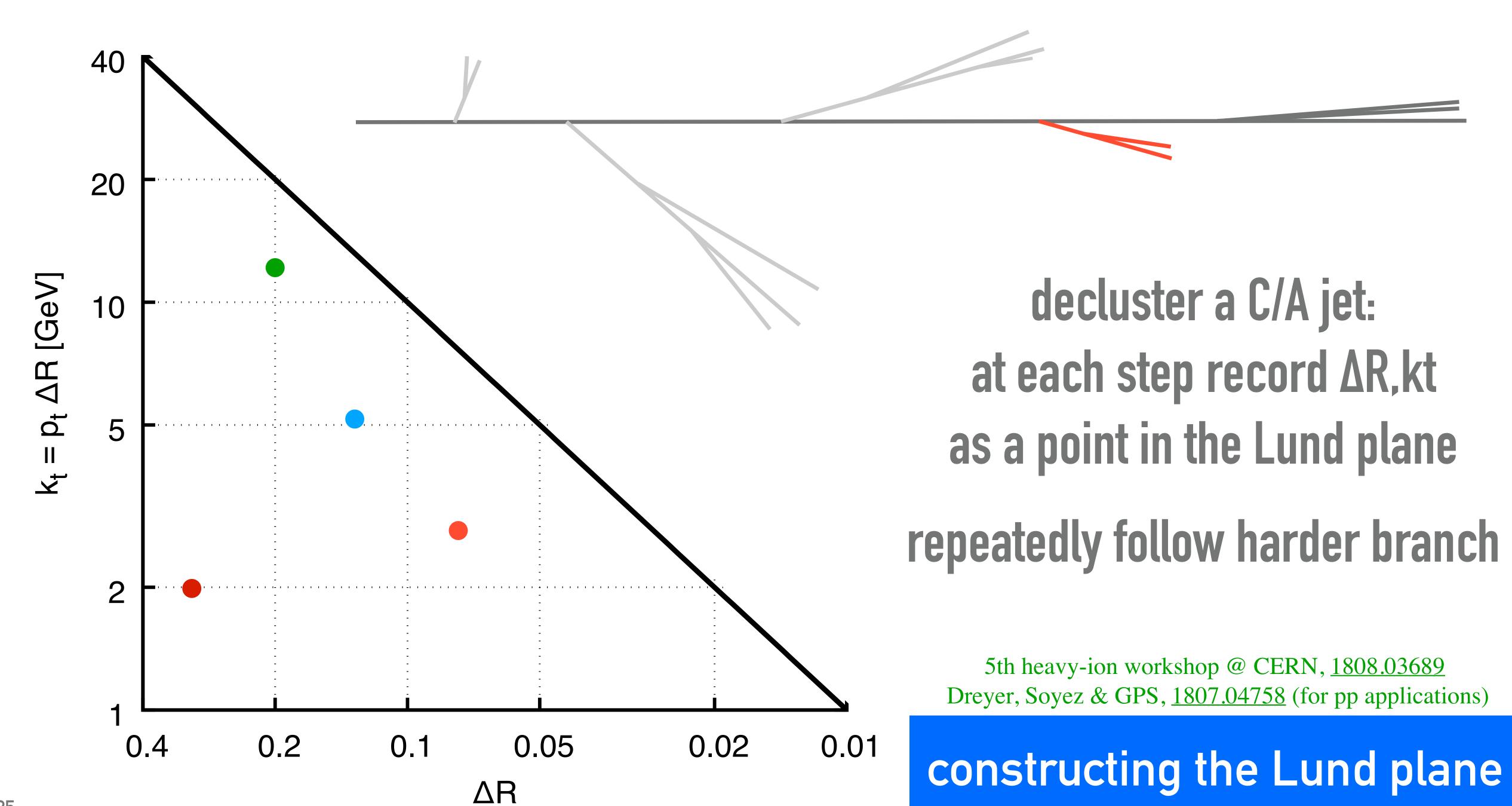


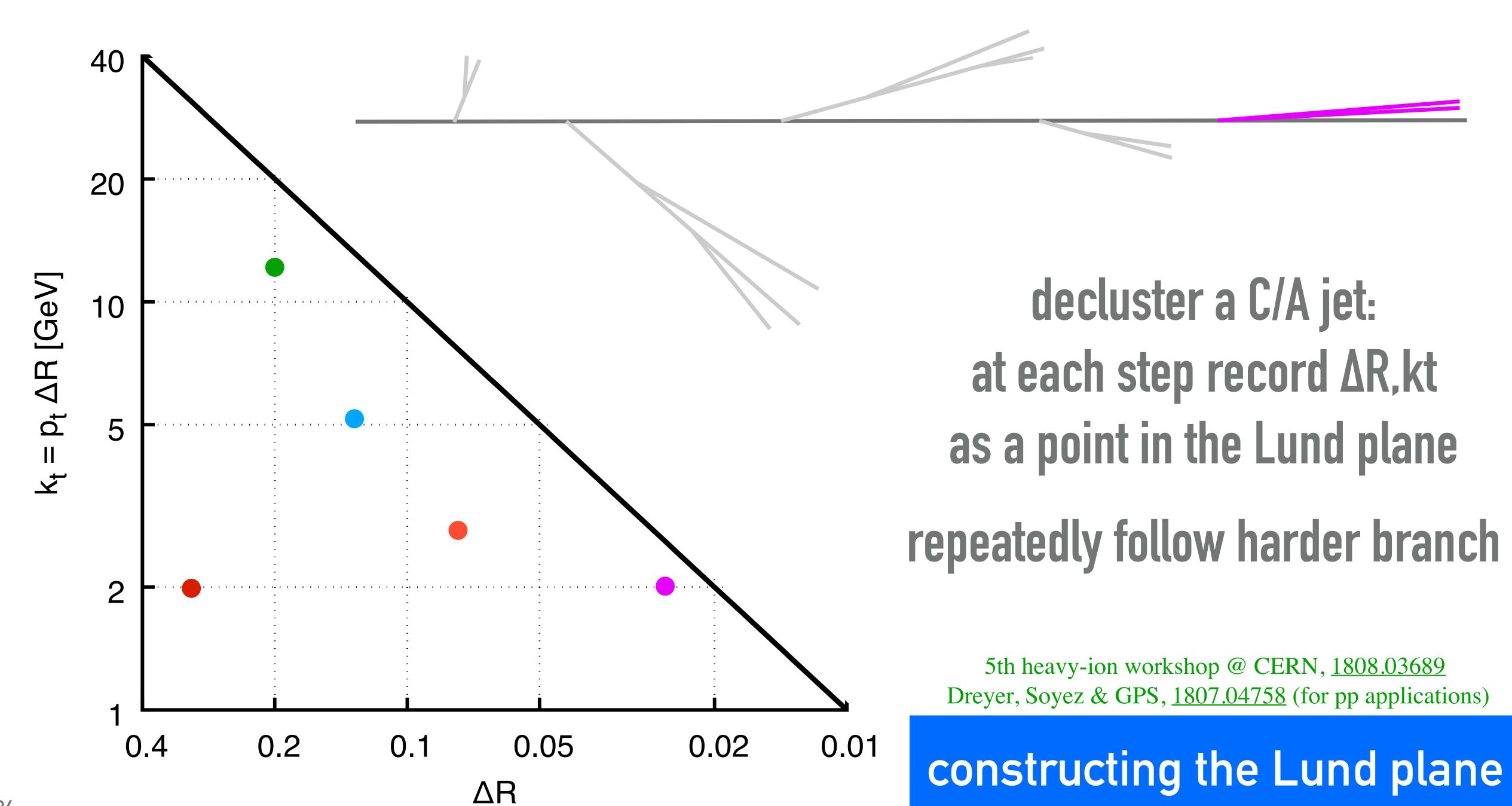


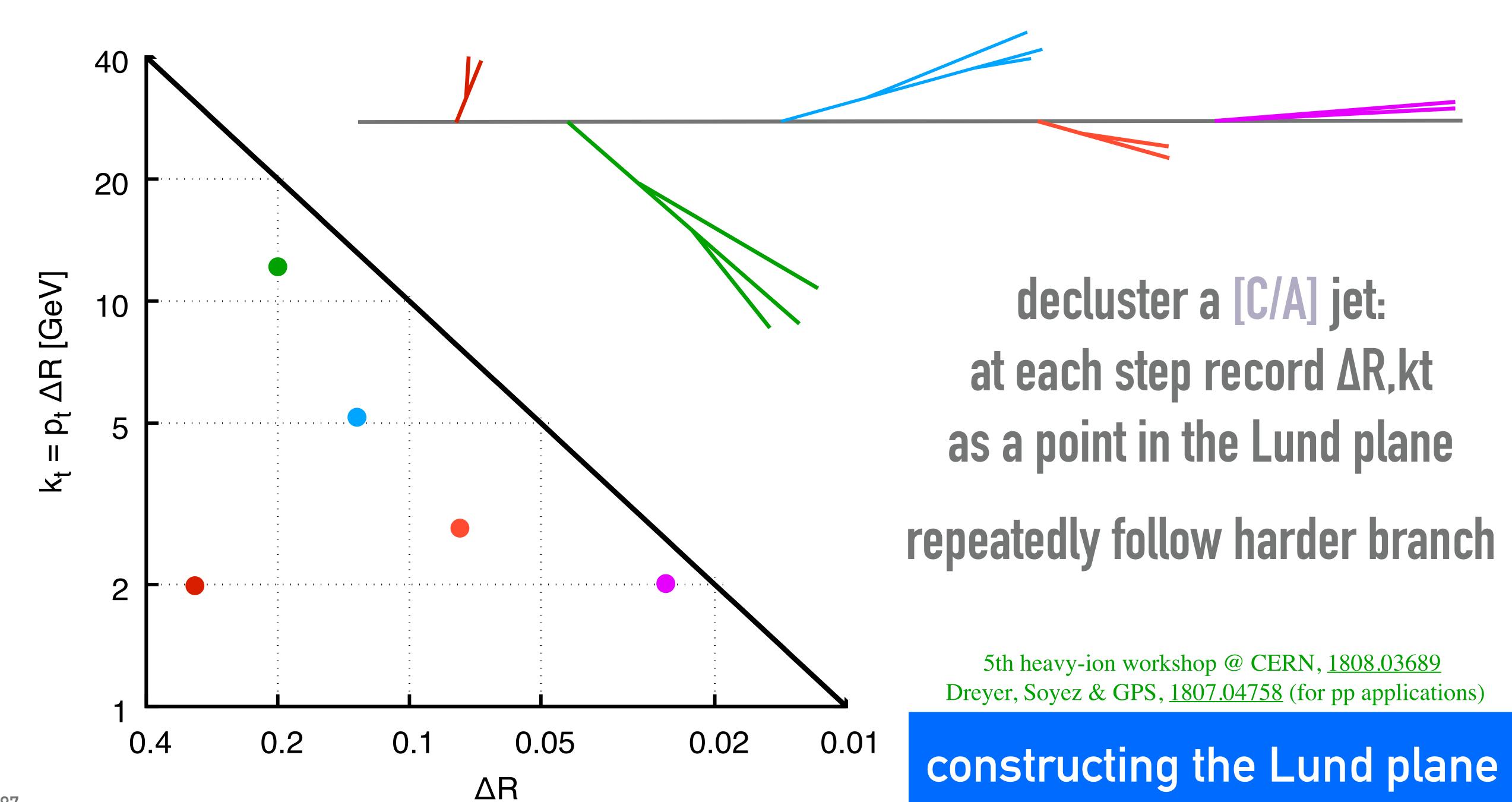


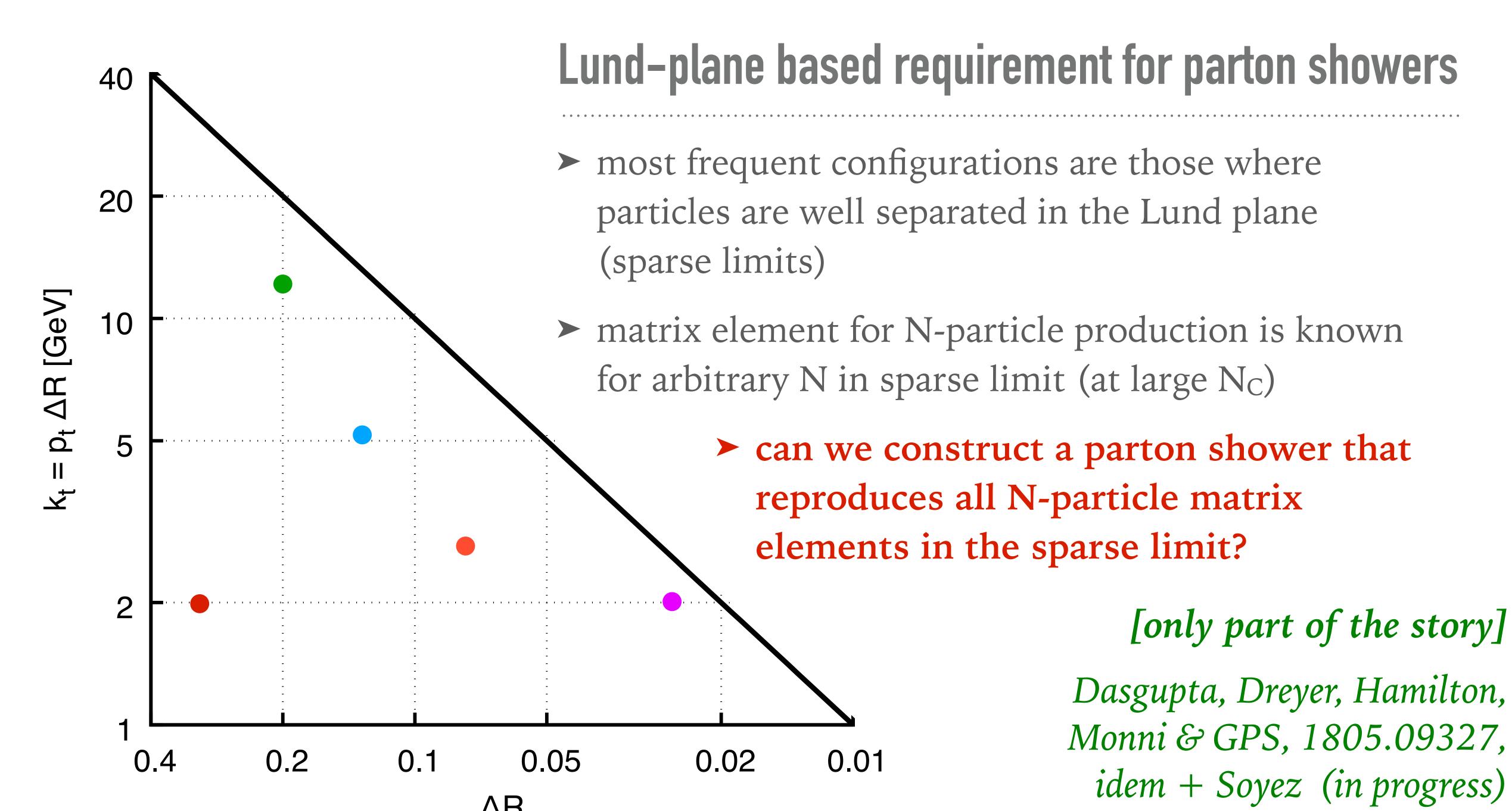








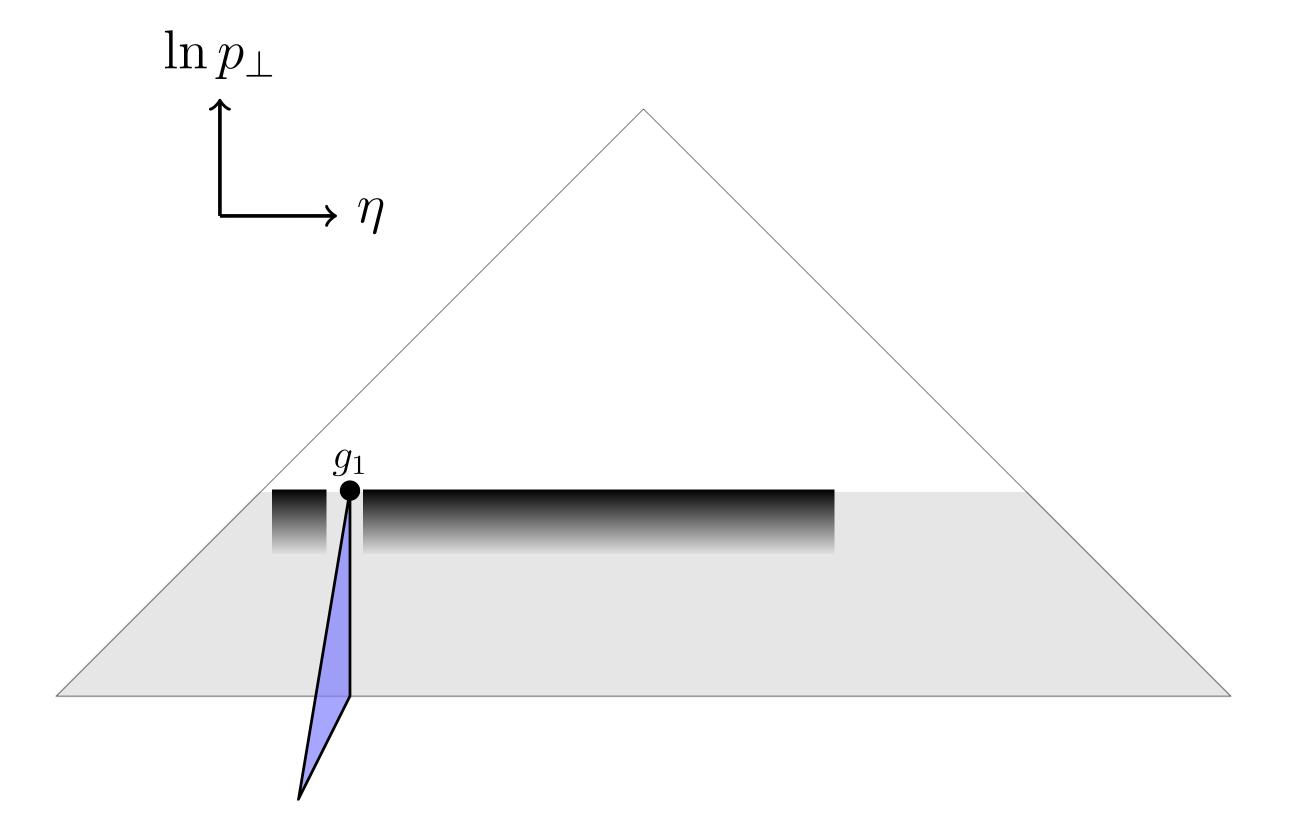




G.P. Salam

Check whether common ("dipole") showers already satisfy this condition

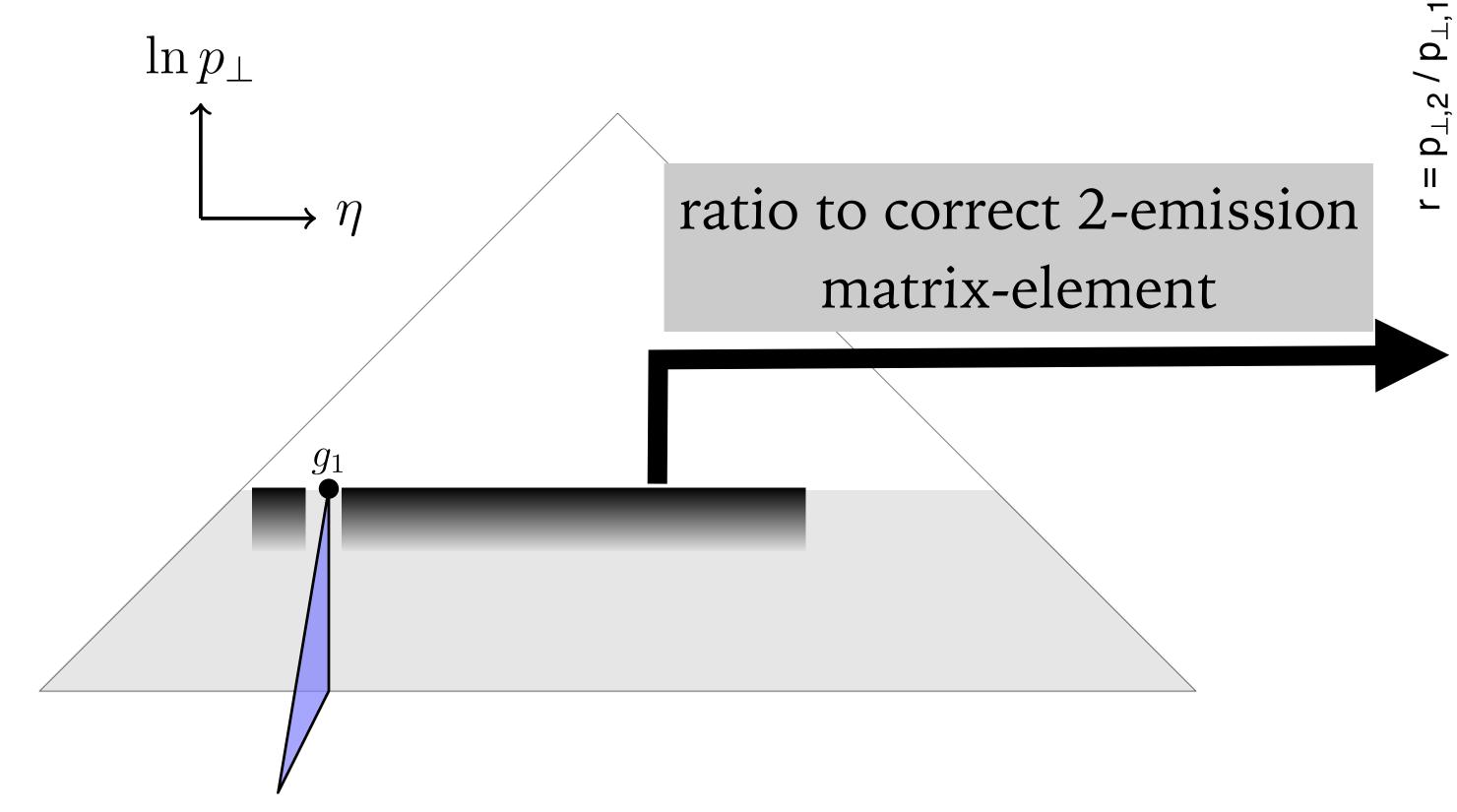
Lund phasespace map



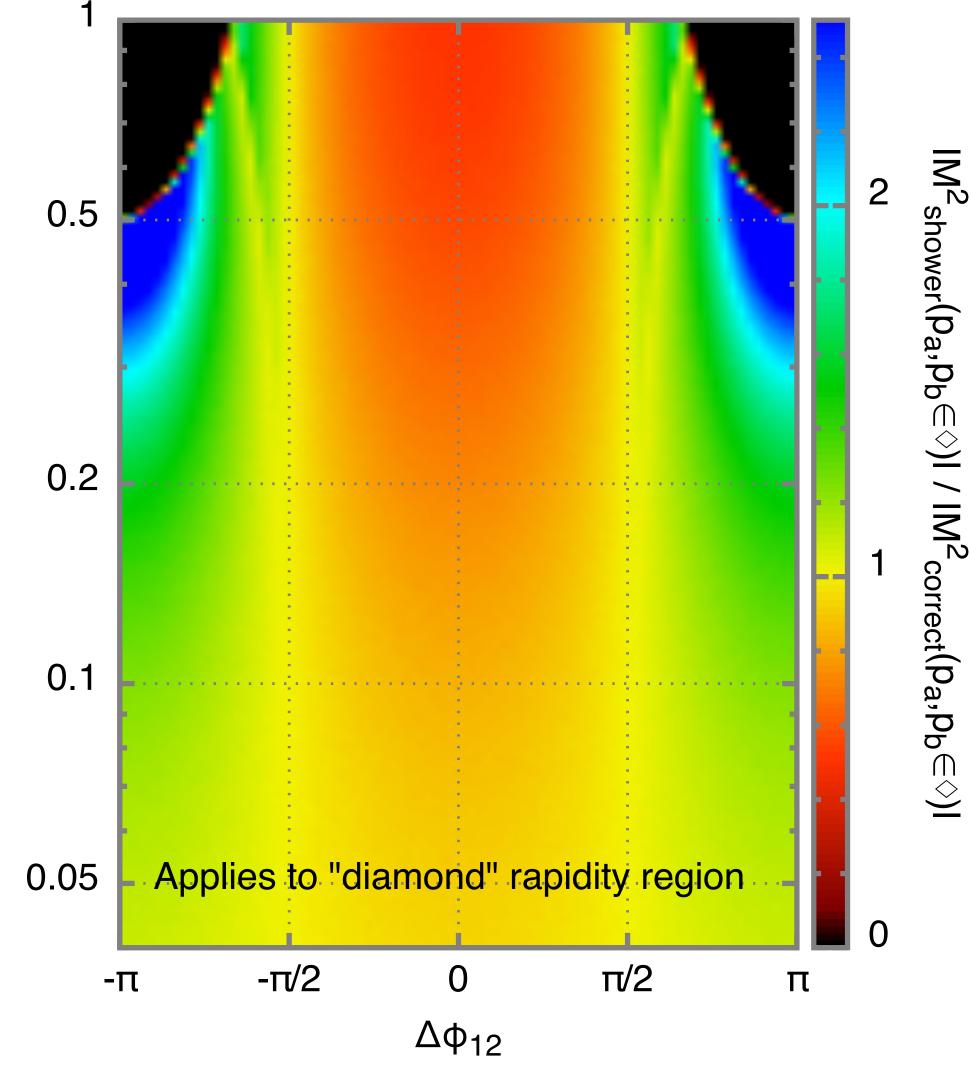
analogous effect commented on by Nagy & Soper for Drell-Yan recoil, but wider relevance not appreciated?

Check whether common ("dipole") showers already satisfy this condition

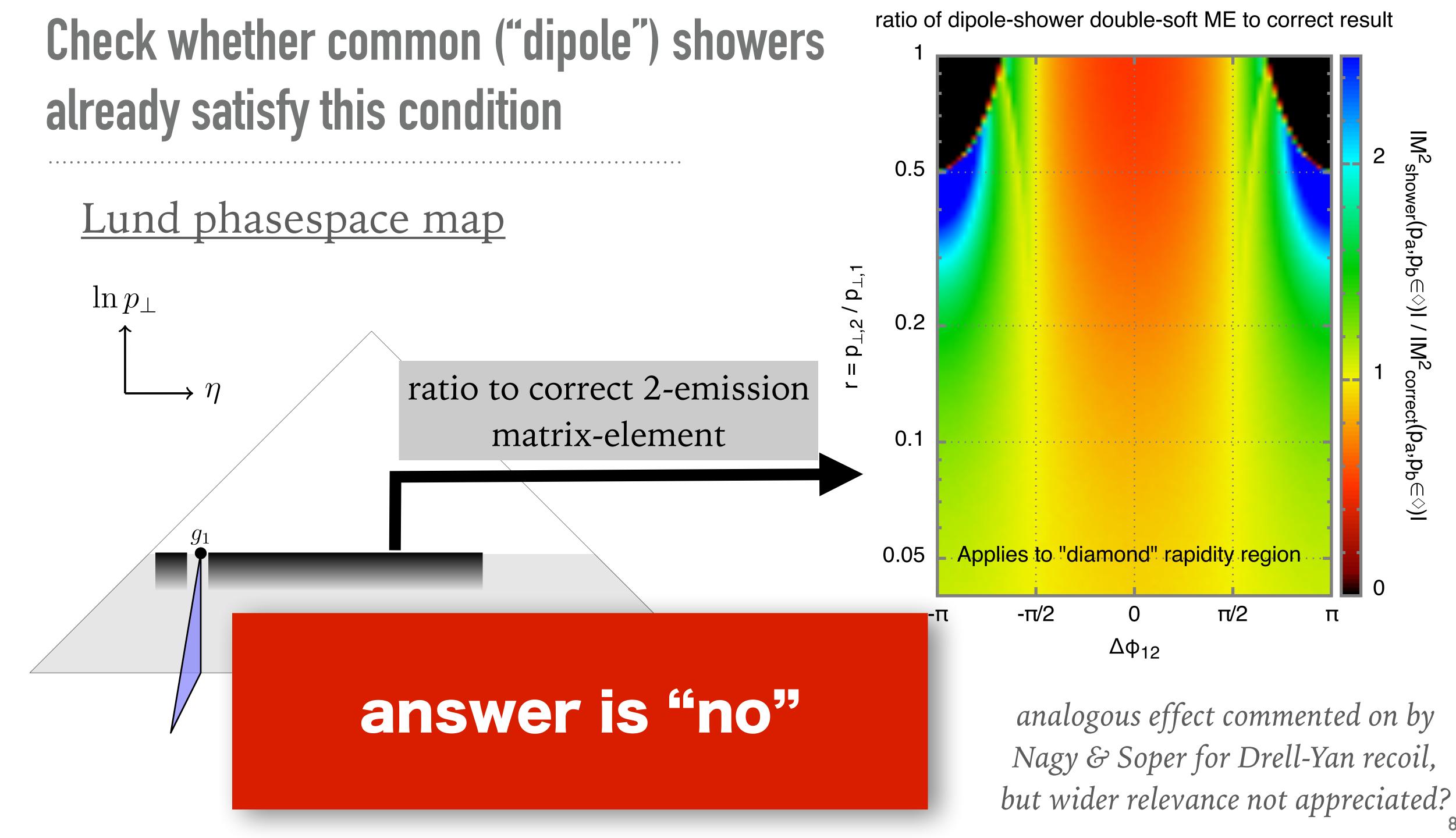
Lund phasespace map



ratio of dipole-shower double-soft ME to correct result



analogous effect commented on by Nagy & Soper for Drell-Yan recoil, but wider relevance not appreciated?



Parton showering as an inverse problem

updated n updated parton shower new branching state particle particle state particle info info momentum momenta momenta operator $B(\{r\}): \{k_1, \dots, k_n; s\} \to \{k'_1, \dots, k'_n, k'_{n+1}; s'\}$

- > Repeated application of operator B generates an event
- ➤ What classes of B reproduces correct matrix element for N emissions (sparse in the Lund plane)?

random

numbers

OUTLOOK

I think Nature is smarter than physicists. We should have the courage to say: "Let Nature tell us what is going on."

-Carlo Rubbia [2008]

What should particle physics expect of itself?

- ➤ Many fascinating challenges (e.g. dark matter, hierarchy of scales). We should think about solutions & search for them experimentally, but be wary of promising breakthroughs
- The biggest [accessible] challenge for the future is to see what we can learn, experimentally, about the Higgs potential, $V(\phi)$ (one of strongest drivers for a new collider)
- ➤ Don't stop thinking about how to come up with the "right" questions to ask
 - > whether for the big picture
 - > or smaller problems that might, one day, help with that big picture