

Global Fits of Flavour Anomalies

Presented by Sébastien Descotes-Genon & Peter Stangl



Outline

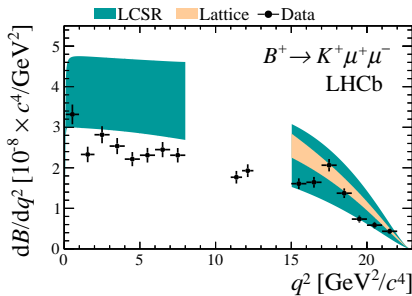
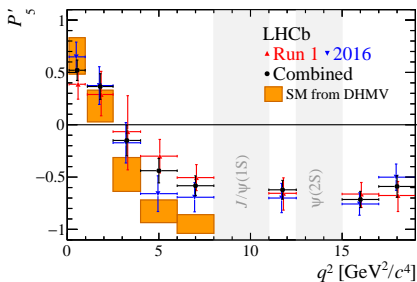
- 1 Flavour Anomalies
- 2 Theoretical Framework
- 3 Analysis Inputs
- 4 Results
- 5 Conclusions

Flavour Anomalies

$b \rightarrow s \mu^+ \mu^-$ anomaly

Several LHCb measurements deviate from Standard model (SM) predictions by 2-3 σ :

- ▶ Angular observable P'_5 in $B \rightarrow K^* \mu^+ \mu^-$. LHCb, arXiv:2003.04831
- ▶ Branching ratios of $B \rightarrow K \mu^+ \mu^-$, $B \rightarrow K^* \mu^+ \mu^-$, and $B_s \rightarrow \phi \mu^+ \mu^-$. LHCb, arXiv:1403.8044, arXiv:1506.08777, arXiv:1606.04731

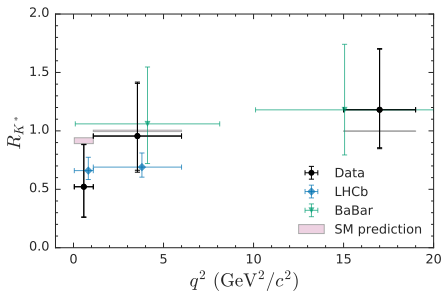
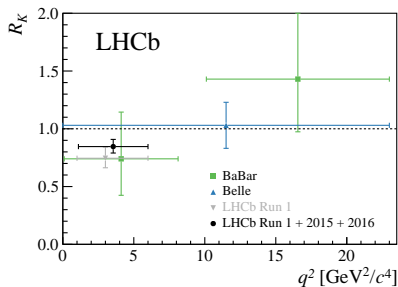


Hints for LFU violation in $b \rightarrow s \ell^+ \ell^-$ decays

Measurements of lepton flavour universality (LFU) ratios $R_K^{[1,6]}$, $R_{K^*}^{[0.045,1.1]}$, $R_{K^*}^{[1.1,6]}$ show deviations from SM by about 2.5σ each.

LHCb, arXiv:1705.05802, arXiv:1903.09252
Belle, arXiv:1904.02440, arXiv:1908.01848

$$R_{K^{(*)}} = \frac{BR(B \rightarrow K^{(*)} \mu^+ \mu^-)}{BR(B \rightarrow K^{(*)} e^+ e^-)}$$



Hints for LFU violation in $b \rightarrow c \ell \nu$ decays

Measurements of LFU ratios R_D and R_{D^*} by BaBar, Belle, and LHCb show combined deviation from SM by about 3σ .

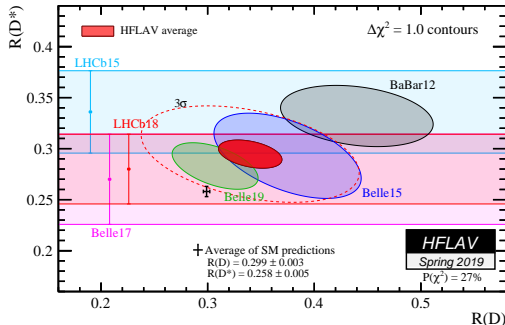
BaBar, arXiv:1205.5442, arXiv:1303.0571

LHCb, arXiv:1506.08614, arXiv:1708.08856

Belle, arXiv:1507.03233, arXiv:1607.07923, arXiv:1612.00529, arXiv:1904.08794

$$R_{D^{(*)}} = \frac{BR(B \rightarrow D^{(*)} \tau \nu)}{BR(B \rightarrow D^{(*)} \ell \nu)}$$

$$\ell \in \{e, \mu\}$$



HFLAV, hflav.web.cern.ch

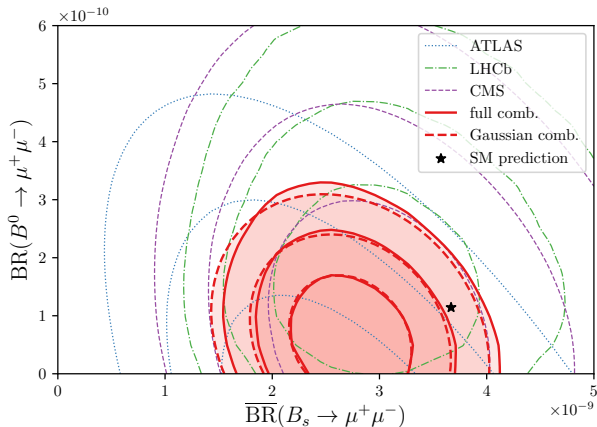
Combination of $B_{s,d} \rightarrow \mu^+ \mu^-$ measurements

Measurements of $\text{BR}(B_{s,d} \rightarrow \mu^+ \mu^-)$ by LHCb, CMS, and ATLAS show combined deviation from SM by about 2σ .

LHCb, arXiv:1703.05747

CMS, arXiv:1910.12127

ATLAS, arXiv:1812.03017



Theoretical Framework

$b \rightarrow s\ell\ell$ in the weak effective theory

- Effective Hamiltonian at scale m_b : $\mathcal{H}_{\text{eff}}^{bs\ell\ell} = \mathcal{H}_{\text{eff, SM}}^{bs\ell\ell} + \mathcal{H}_{\text{eff, NP}}^{bs\ell\ell}$

$$\mathcal{H}_{\text{eff, NP}}^{bs\ell\ell} = -\mathcal{N} \sum_{\ell=e,\mu} \sum_{i=9,10,S,P} (C_i^{bs\ell\ell} O_i^{bs\ell\ell} + C_i'^{bs\ell\ell} O_i'^{bs\ell\ell}) + \text{h.c.}$$

- Operators considered here ($\ell = e, \mu$)

$$\begin{aligned} O_9^{bs\ell\ell} &= (\bar{s}\gamma_\mu P_L b)(\bar{\ell}\gamma^\mu \ell), & O_9'^{bs\ell\ell} &= (\bar{s}\gamma_\mu P_R b)(\bar{\ell}\gamma^\mu \ell), \\ O_{10}^{bs\ell\ell} &= (\bar{s}\gamma_\mu P_L b)(\bar{\ell}\gamma^\mu \gamma_5 \ell), & O_{10}'^{bs\ell\ell} &= (\bar{s}\gamma_\mu P_R b)(\bar{\ell}\gamma^\mu \gamma_5 \ell), \\ O_S^{bs\ell\ell} &= m_b(\bar{s}P_R b)(\bar{\ell}\ell), & O_S'^{bs\ell\ell} &= m_b(\bar{s}P_L b)(\bar{\ell}\ell), \\ O_P^{bs\ell\ell} &= m_b(\bar{s}P_R b)(\bar{\ell}\gamma_5 \ell), & O_P'^{bs\ell\ell} &= m_b(\bar{s}P_L b)(\bar{\ell}\gamma_5 \ell). \end{aligned}$$

- Not considered here

- Dipole operators: strongly constrained by radiative decays. e.g. [arXiv:1608.02556]
- Four quark operators: dominant effect from RG running above m_B .

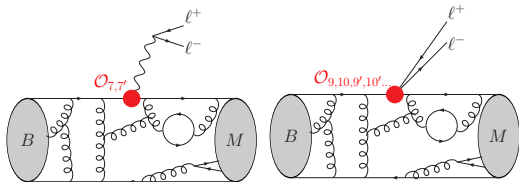
Jäger, Leslie, Kirk, Lenz [arXiv:1701.09183]

Two sources of hadronic uncertainties for exclusive

$$A(B \rightarrow M\ell\ell) = \frac{G_F \alpha}{\sqrt{2}\pi} V_{tb} V_{ts}^* [(A_\mu + T_\mu) \bar{u}_\ell \gamma^\mu v_\ell + B_\mu \bar{u}_\ell \gamma^\mu \gamma_5 v_\ell]$$

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Form factors (local)

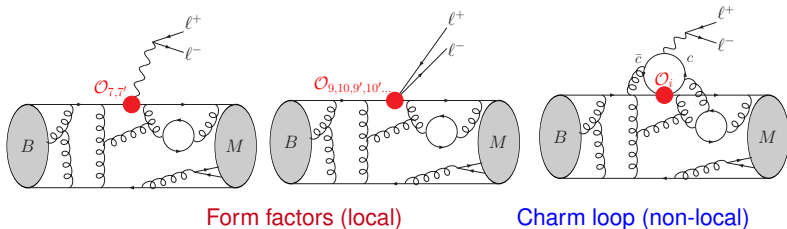
- ▶ Local contributions (more terms if NP in non-SM C_i): **form factors**

$$A_\mu = -\frac{2m_b q^\nu}{q^2} C_7 \langle M | \bar{s} \sigma_{\mu\nu} P_R b | B \rangle + C_9 \langle M | \bar{s} \gamma_\mu P_L b | B \rangle$$

$$B_\mu = C_{10} \langle M | \bar{s} \gamma_\mu P_L b | B \rangle$$

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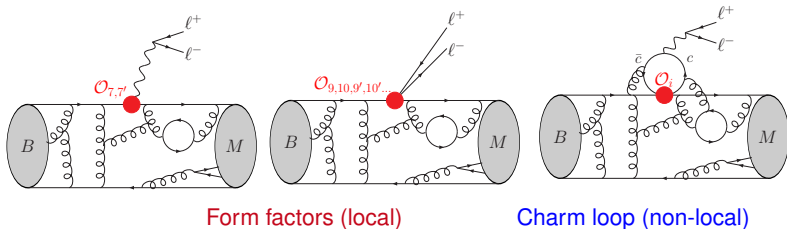
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- ▶ Non-local contributions (charm loops): **hadronic contribs.**

T_μ contributes like $O_{7,9}$, but depends on q^2 and external states

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- ▶ Non-local contributions (charm loops): **hadronic contribs.**

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- ▶ Overall agreement about both contributions, using various tools

Hadronic uncertainties: form factors

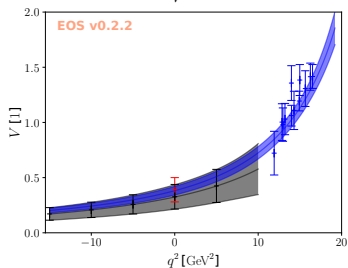
3 form factors for K , 7 form factors for K^* and ϕ

▶ low recoil: **lattice QCD**

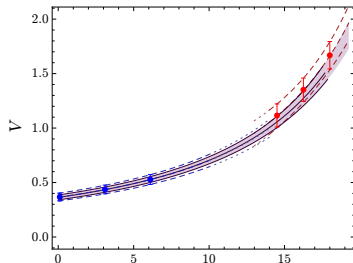
[Horgan, Liu, Meinel, Wingate; HPQCD collab]

▶ large recoil: **Light-Cone Sum Rules** (B-meson or light-meson DAs)

[Khodjamirian, Mannel, Pivovarov, Wang; Bharucha, Straub, Zwicky; Gubernari, Kokulu, van Dyk]



B-meson LCSR + lattice



Light-meson LCSR + lattice

▶ correlations among the form factors needed

▶ known from direct determination and/or combined fit to low and large recoils [PS]

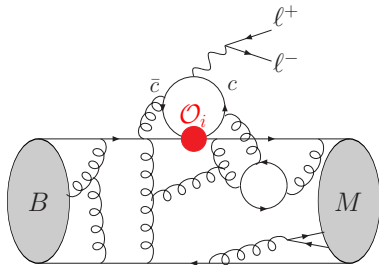
▶ recovered from EFT with $m_b \rightarrow \infty + O(\alpha_s) + O(1/m_b)$ [SDG]

[Jäger, Camalich; Capdevila, SDG, Hofer, Matias; Straub, Altmannshofer; Hurth, Mahmoudi]

▶ optimised observables P_i to reduce the impact of form factor uncertainties

Hadronic uncertainties: charm loops

- ▶ important for resonance regions (charmonia)
- ▶ SM effect contributing to $C_{9\ell}$
- ▶ depends on q^2 , lepton univ.
- ▶ quark-hadron duality approx at large q^2 (syst of few %)

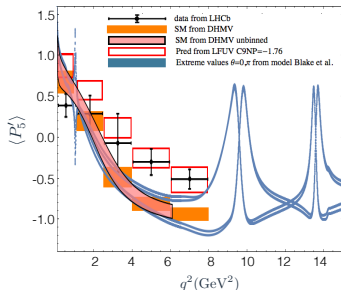


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Several approaches agree at low- q^2

- ▶ LCSR estimates [Khodjamirian, Mannel, Pivovarov, Wang; Gubenari, Van Dyk]
- ▶ order of magnitude estimate for the fits (LCSR or Λ/m_b), check with bin-by-bin fits [Crivellin, Capdevila, SDG, Hofer, Matias; Straub, Altmannshoffer; Hurth, Mahmoudi]
- ▶ fit of sum of resonances to the data [Blake, Egede, Owen, Pomery, Petridis]

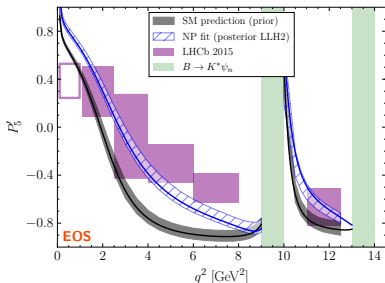


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- ▶ fit of sum of resonances to the data [Blake, Egede, Owen, Pomery, Petridis]
- ▶ fit of q^2 -parametrisation to the data [Ciuchini, Fedele, Franco, Mishima, Paul, Silvestrini, Valli; Capdevila, SDG, Hofer, Matias]
- ▶ dispersive representation + $J/\psi, \psi(2S)$ data [Bobeth, Chrzaszcz, van Dyk, Virto]



Setup

- ▶ PS: Global likelihood from **smelli** python package for comparing theory predictions to experimental data Aebischer, Kumar, PS, Straub, arXiv:1810.07698
- ▶ SDG: Likelihood taking into account experimental and theoretical uncertainties and correlations in Gaussian approximation
[Algueró, Capdevila, Crivellin, SDG, Masuan Matias, Novoa-Brunet, Virto]

Two statistical quantities of interest to asses a NP scenario/hypothesis

- ▶ p -value of a given hypothesis: χ^2_{\min} considering N_{dof} (in %)
goodness of fit: does the hypothesis give an overall good fit ?
and if not, can we exclude it ?
- ▶ $\text{Pull}_{\text{SM}} : \chi^2(\mathcal{C}_i = 0) - \chi^2_{\min}$ considering N_{dof} (in σ units)
metrology: how well does the hypothesis solve SM deviations ?

Analysis Inputs

Experimental inputs

- ▶ R_K, R_{K^*} (large- and low-recoil bins)
- ▶ $B \rightarrow K^* \mu\mu$ (Br and ang obs)
- ▶ $B \rightarrow K^* ee$ (ang obs)
- ▶ $B_s \rightarrow \phi\mu\mu$ (Br and ang obs)
- ▶ $B^+ \rightarrow K^+ \mu\mu, B^0 \rightarrow K^0 \mu\mu$ (Br and ang obs)
- ▶ $B \rightarrow X_s \gamma, B \rightarrow X_s \mu\mu, B_s \rightarrow \mu\mu, B_s \rightarrow \phi\gamma, B \rightarrow K^* \gamma$ (Br)

including LHCb, ATLAS, CMS, Babar and Belle data whenever available

- ▶ SDG: No inclusion of additional observables that are not directly related to $b \rightarrow s\ell\ell$ and $b \rightarrow s\gamma$ (would require extra assumption on NP model)
- ▶ PS: **Global likelihood** contains many other observables not directly sensitive to considered Wilson coefficients
- ▶ PS: Theory **correlations with $\Delta F = 2$ observables** have an effect on the fit

Theoretical inputs

SDG:

- ▶ Form factors: B-meson DA LCSR + lattice + EFT for correlations
- ▶ Charm-loop corrections: Perturbative contribution + magnitude of of long-distance contrib inspired by [Khodjamirian, Mannel, Pivovarov, Wang]
- ▶ Quark-duality violation at high q^2 : 10% effect at the level of the amplitude
- ▶ $Br(B_s \rightarrow \mu\mu)$ modified to include latest corrections from [Misiak ; Beneke, Bobeth, Szafron]

PS:

- ▶ Form factors: For B to light vector meson from [Bharucha, Straub, Zwicky], for $B \rightarrow K$ from [Gubernari, Kokulu, van Dyk]
- ▶ Non-factorizable effects parametrized as in [Bharucha, Straub, Zwicky], [Altmannshofer, Straub], compatible with [Khodjamirian, Mannel, Pivovarov, Wang], [Bobeth, Chrzaszcz, van Dyk, Virto]
- ▶ Additional parametric uncertainties (e.g. CKM) based on [flavio v2.0] with default settings

Results

1D Scenarios for $\mathcal{C}_{i\mu}$ [2020]

1D Hyp.	All			LFUV		
	1σ	Pull_{SM}	p-value	1σ	Pull_{SM}	p-value
$\mathcal{C}_{9\mu}^{\text{NP}}$	$[-1.19, -0.88]$	6.3	37.5%	$[-1.25, -0.61]$	3.3	60.7%
$\mathcal{C}_{9\mu}^{\text{NP}} = -\mathcal{C}_{10\mu}^{\text{NP}}$	$[-0.59, -0.41]$	5.8	25.3%	$[-0.50, -0.28]$	3.7	75.3%
$\mathcal{C}_{9\mu}^{\text{NP}} = -\mathcal{C}_{9'\mu}$	$[-1.17, -0.87]$	6.2	34.0%	$[-2.15, -1.05]$	3.1	53.1%

- ▶ LFUV fit: $R_K, R_{K^*}, Q_{4,5}, B_s \rightarrow \mu\mu, b \rightarrow s\gamma$
- ▶ All : all $b \rightarrow sll$ and $b \rightarrow s\gamma$ observables
- ▶ Pull_{SM} in σ units increased compare to [2019]
- ▶ p-value of SM hyp decreased from 11% to **1.4% (2.5σ)** for the fit “All”

Scenarios with a single Wilson coefficients

Coefficient	type	best fit	1σ	$\text{pull}_{1D} = \sqrt{\Delta\chi^2}$
$C_9^{bs\mu\mu}$	$L \otimes V$	-0.93	$[-1.07, -0.79]$	6.2σ
$C_9^{'bs\mu\mu}$	$R \otimes V$	+0.14	$[-0.02, +0.31]$	0.9 σ
$C_{10}^{bs\mu\mu}$	$L \otimes A$	+0.71	$[+0.58, +0.84]$	5.7σ
$C_{10}^{'bs\mu\mu}$	$R \otimes A$	-0.20	$[-0.29, -0.08]$	1.7 σ
$C_9^{bs\mu\mu} = C_{10}^{bs\mu\mu}$	$L \otimes R$	+0.15	$[+0.02, +0.29]$	1.2 σ
$C_9^{bs\mu\mu} = -C_{10}^{bs\mu\mu}$	$L \otimes L$	-0.53	$[-0.61, -0.46]$	6.9σ

Only small pull for

- ▶ Coefficients with $\ell = e$ (cannot explain $b \rightarrow s\mu\mu$ anomaly)
- ▶ Scalar coefficients (can only reduce tension in $B_s \rightarrow \mu\mu$)

see also similar fits by other groups:

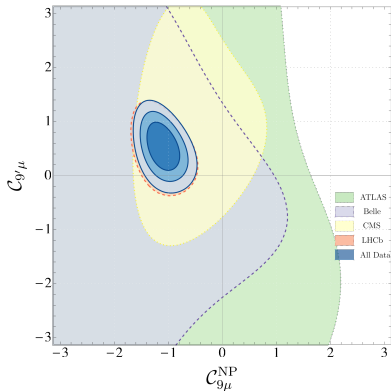
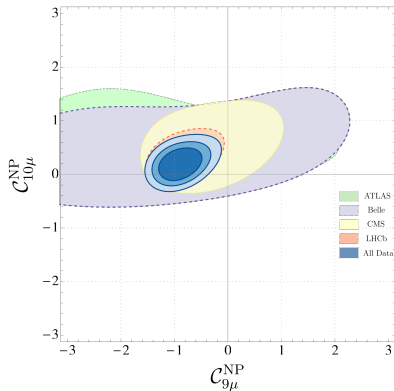
Ciuchini et al., arXiv:1903.09632

Datta et al., arXiv:1903.10086

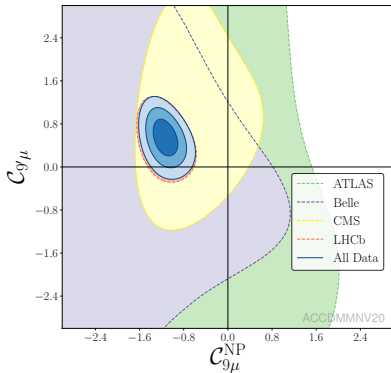
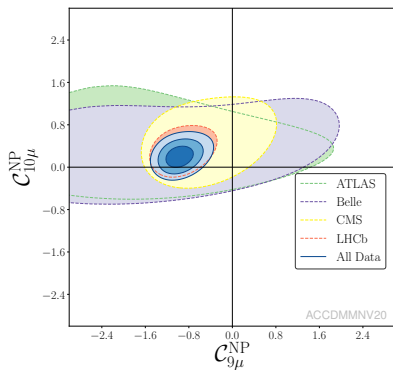
Kowalska et al., arXiv:1903.10932

Arbey et al., arXiv:1904.08399

2D Scenarios for $C_{i\mu}$ [2019]



2D Scenarios for $C_{i\mu}$ [2020]



2D and 6D Scenarios for $C_{i\mu}$ [2020]

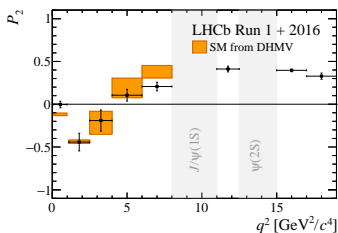
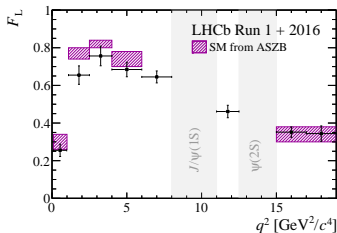
2D Hyp.	All			LFUV		
	Best fit	Pull _{SM}	p-value	Best fit	Pull _{SM}	p-value
$(C_{9\mu}^{\text{NP}}, C_{10\mu}^{\text{NP}})$	(-0.98, 0.19)	6.2	39.8 %	(-0.31, 0.44)	3.2	70.0 %
$(C_{9\mu}^{\text{NP}}, C_{9'\mu})$	(-1.14, 0.55)	6.5	47.4 %	(-1.86, 1.20)	3.5	81.2 %
$(C_{9\mu}^{\text{NP}}, C_{10'\mu})$	(-1.17, -0.33)	6.6	50.3 %	(-1.87, -0.59)	3.7	89.6 %
$(C_{9\mu}^{\text{NP}} = -C_{9'\mu}, C_{10\mu}^{\text{NP}} = C_{10'\mu})$	(-1.10, 0.28)	6.5	48.9 %	(-1.69, 0.29)	3.5	82.4 %
$(C_{9\mu}^{\text{NP}}, C_{9'\mu} = -C_{10'\mu})$	(-1.17, 0.23)	6.6	51.1 %	(-2.05, 0.50)	3.8	91.9 %

- ▶ Right-handed currents appear quite naturally
- ▶ No change in the hierarchy of scenarios

	C_7^{NP}	$C_{9\mu}^{\text{NP}}$	$C_{10\mu}^{\text{NP}}$	$C_{7'}$	$C_{9'\mu}$	$C_{10'\mu}$
Bfp	+0.00	-1.13	+0.20	+0.00	+0.49	-0.10
1 σ	[-0.02, +0.02]	[-1.30, -0.96]	[+0.05, +0.37]	[-0.01, +0.02]	[+0.04, +0.95]	[-0.33, +0.14]
2 σ	[-0.03, +0.04]	[-1.46, -0.78]	[-0.09, +0.57]	[-0.03, +0.04]	[-0.39, +1.45]	[-0.55, +0.41]

- ▶ Pull_{SM}: 5.1 [2019] \rightarrow 5.8 σ [2020]
- ▶ p -value: 81.6% [2019] \rightarrow 46.8% [2020]

Comments on the $B \rightarrow K^* \mu\mu$ data



New data from LHCb

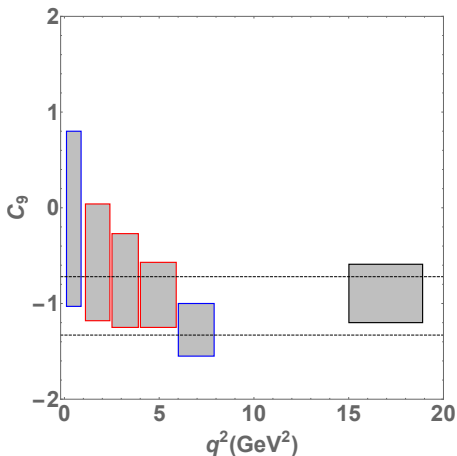
- uncertainty reduced by 30 – 50% (in particular $[1.1, 2.5]$ and $[2.5, 4]$)
- new average value for F_L in the bin $[2.5, 4]$ more than 4σ below 1, helping the discussion in terms of optimised observables P_i

Excellent consistency

- new tensions with respect to the SM in $\langle P_3 \rangle_{[1.1, 2.5]}$, $\langle P'_6 \rangle_{[6, 8]}$ and $\langle P'_8 \rangle_{[1.1, 2.5]}$
- enhanced tension for other observables such as the first bin of $P_{1,2}$
- tension in first bin of P'_5 decreased, in better agreement with theory (see later)

Solve earlier tensions of the fit discussed in [\[Algueró, Capdevila, SDG, Masjuan Matias\]](#)

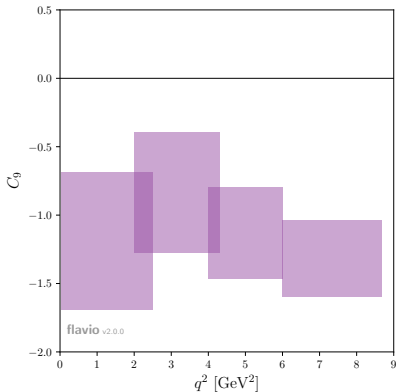
Consistency of the results over the q^2 range



Sanity check possible for the $C_{9\mu}^{\text{NP}}$ hypothesis

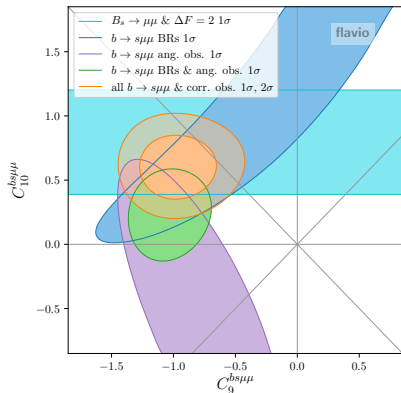
- ▶ $B \rightarrow K^* \mu\mu$ Br + ang obs +
 $B_s \rightarrow \mu\mu$ + $B \rightarrow X_s \mu\mu$ +
 $b \rightarrow s\gamma$
- ▶ $C_{9\mu}^{\text{NP}}$ fitted separately for each bin
- ▶ Good agreement with global fit (2σ range)
- ▶ No indication of a q^2 variation
- ▶ In particular, agreement between low and large recoils with very different theoretical approaches and systematics

Consistency of the results over the q^2 range



- Finding also **good agreement with q^2 -independent C_9** considering data on $B \rightarrow K^* \mu\mu$ from LHCb, ATLAS, CMS, CDF (different binning)

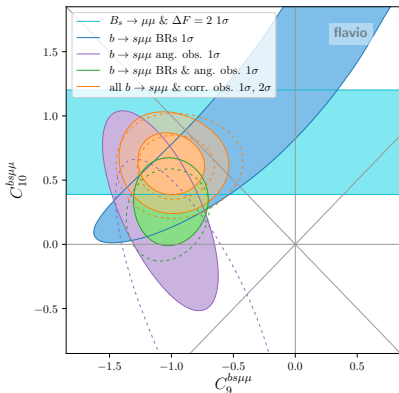
Scenarios with two Wilson coefficients



WET at 4.8 GeV

- **[2019]:**
Angular obs. slightly disfavour positive $C_{10}^{bs\mu\mu}$, but overall good agreement between different sectors

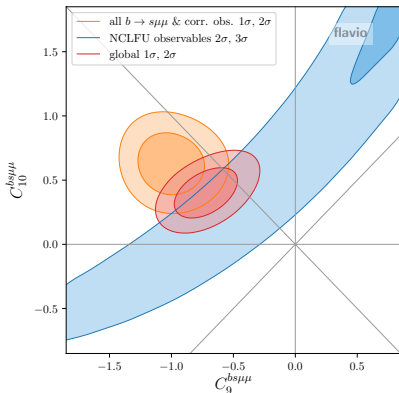
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- ▶ **[2019]:**
Angular obs. slightly disfavour positive $C_{10}^{bs\mu\mu}$, but overall good agreement between different sectors
- ▶ **[2020]:**
Angular obs. slightly favour positive $C_{10}^{bs\mu\mu}$, agreement increased

Scenarios with two Wilson coefficients



WET at 4.8 GeV

- ▶ **[2019]:**
Angular obs. slightly disfavour positive $C_{10}^{bs\mu\mu}$, but overall good agreement between different sectors
- ▶ **[2020]:**
Angular obs. slightly favour positive $C_{10}^{bs\mu\mu}$, agreement increased
- ▶ **Global likelihood:**
 - ▶ Tension between fits to R_K & R_{K^*} and $b \rightarrow s\mu\mu$ observables in C_9 direction \Rightarrow **LFU C_9 ?**
 - ▶ Purely left-handed $C_9^{bs\mu\mu} = -C_{10}^{bs\mu\mu}$ yields very good fit to experimental data

Scenarios with two Wilson coefficients

- ▶ **LFU contribution** only affects $b \rightarrow s\mu\mu$ observables
- ▶ Tension between fits to $b \rightarrow s\mu\mu$ observables and R_K & R_{K^*} could be reduced by **LFU** contribution to C_9
- ▶ Perform two-parameter fit in space of $C_9^{\text{univ.}}$ and $\Delta C_9^{bs\mu\mu} = -C_{10}^{bs\mu\mu}$:

$$C_9^{bsee} = C_9^{\text{univ.}}$$

$$C_9^{bs\mu\mu} = C_9^{\text{univ.}} + \Delta C_9^{bs\mu\mu}$$

$$C_9^{bs\tau\tau} = C_9^{\text{univ.}}$$

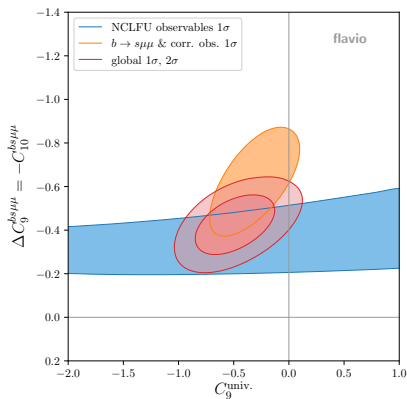
$$C_{10}^{bsee} = 0$$

$$C_{10}^{bs\mu\mu} = -\Delta C_9^{bs\mu\mu}$$

$$C_{10}^{bs\tau\tau} = 0$$

scenario first considered in
Algueró et al., arXiv:1809.08447

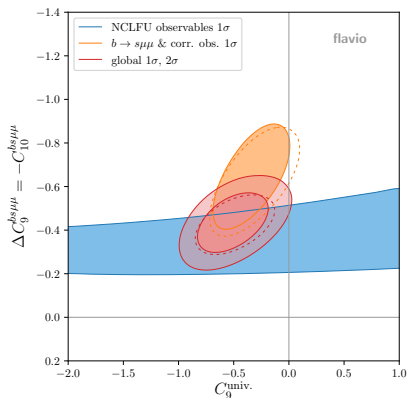
Scenarios with two Wilson coefficients



- [2019]: Preference for **non-zero** $C_9^{\text{univ.}}$

WET at 4.8 GeV

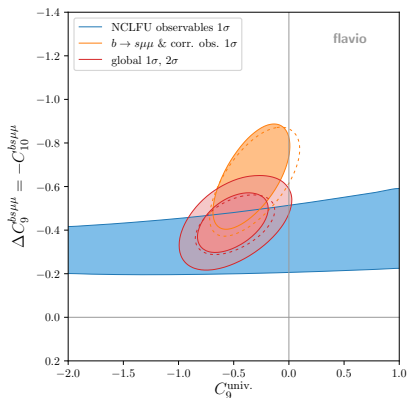
Scenarios with two Wilson coefficients



WET at 4.8 GeV

- ▶ [2019]: Preference for **non-zero** $C_9^{\text{univ.}}$
- ▶ [2020]: Preference for **non-zero** $C_9^{\text{univ.}}$ slightly increased

Scenarios with two Wilson coefficients

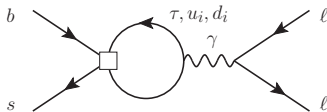


WET at 4.8 GeV

► [2019]:
Preference for **non-zero** $C_9^{\text{univ.}}$

► [2020]:
Preference for **non-zero** $C_9^{\text{univ.}}$
slightly increased

► $C_9^{\text{univ.}}$ can arise from RG effects:

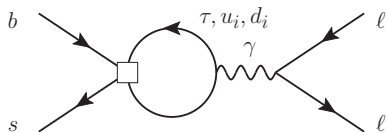


Bobeth, Haisch, arXiv:1109.1826
Crivellin, Greub, Müller, Saturnino, arXiv:1807.02068

The global picture in the SMEFT

RG effects require scale separation

- ▶ Consider **SMEFT at 2 TeV**



Possible operators:

- ▶ $[O_{lq}^{(3)}]_{3323} = (\bar{l}_3 \gamma_\mu \tau^a l_3)(\bar{q}_2 \gamma^\mu \tau^a q_3)$:

Can also **explain $R_{D^{(*)}}$ anomalies!**

- ▶ $[O_{lq}^{(1)}]_{3323} = (\bar{l}_3 \gamma_\mu l_3)(\bar{q}_2 \gamma^\mu q_3)$:

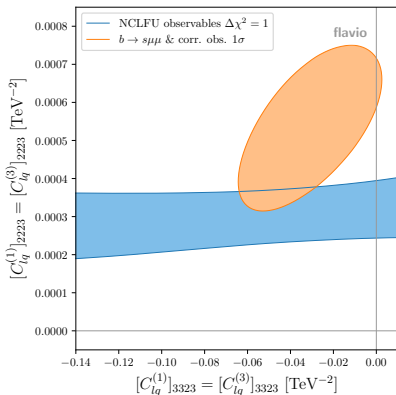
Strong constraints from $B \rightarrow K \nu \nu$ require $[C_{lq}^{(1)}]_{3323} \approx [C_{lq}^{(3)}]_{3323}$

Buras et al., arXiv:1409.4557

- ▶ $[O_{qe}]_{2333} = (\bar{q}_2 \gamma_\mu q_3)(\bar{e}_3 \gamma^\mu e_3)$ cannot explain $R_{D^{(*)}}$

- ▶ Four-quark operators cannot explain $R_{D^{(*)}}$, models yielding large enough contributions already in tension with data

The global picture in the SMEFT

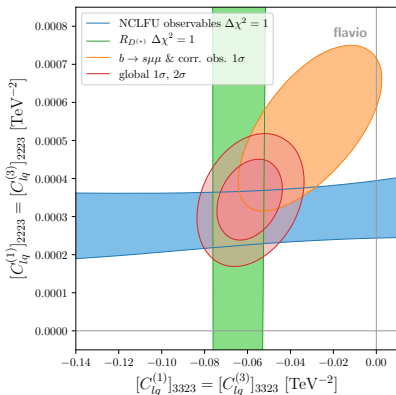


- [2019]:
Clear preference for
non-zero $[C_{lq}^{(1)}]_{3323} = [C_{lq}^{(3)}]_{3323}$

$$[C_{lq}^{(1)}]_{3323} = [C_{lq}^{(3)}]_{3323} \Rightarrow C_9^{\text{univ.}} \quad (\text{RG effect})$$

$$[C_{lq}^{(1)}]_{2223} = [C_{lq}^{(3)}]_{2223} \Rightarrow \Delta C_9^{bs\mu\mu} = -C_{10}^{bs\mu\mu}$$

The global picture in the SMEFT

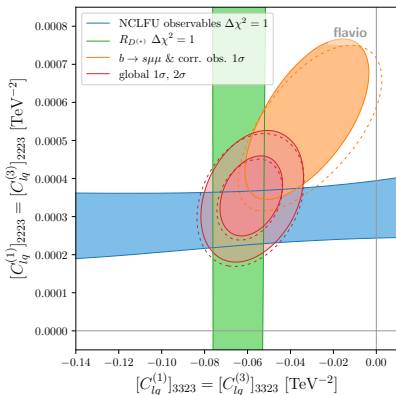


- ▶ **[2019]:**
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- ▶ **$R_{D^{(*)}}$ explanation:**
Agreement with combined $R_{K^{(*)}}$ and
 $b \rightarrow s\mu\mu$ explanation has improved

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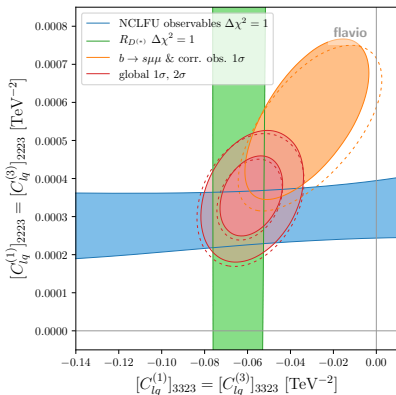


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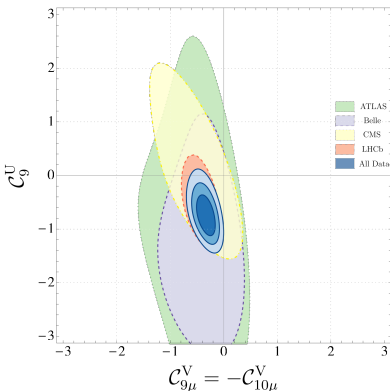
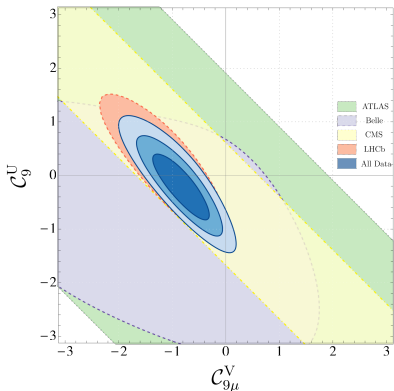
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Preference for
non-zero $[C_{lq}^{(1)}]_{3323} = [C_{lq}^{(3)}]_{3323}$
slightly increased
- ▶ **Only a simple SMEFT scenario**
⇒ Consider explicit models that yield
this coefficients
⇒ Good candidate: **U_1 Leptoquark**

Scenarios for LFU and LFUV C_i [2019]

R_K and R_{K^*} support LFUV NP, but there could also be a LFU piece

$$C_{ie} = C_i^U \quad C_{i\mu} = C_i^U + C_{i\mu}^V$$

[Algueró, Capdevila, SDG, Masjuan, Matias]

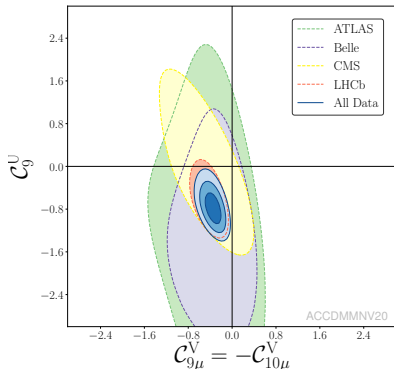
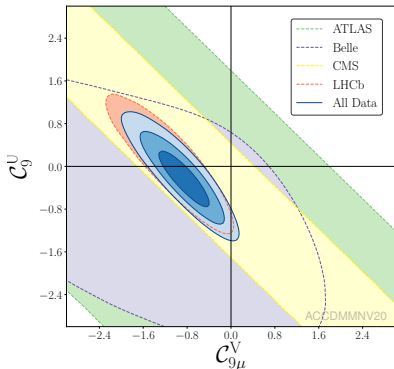


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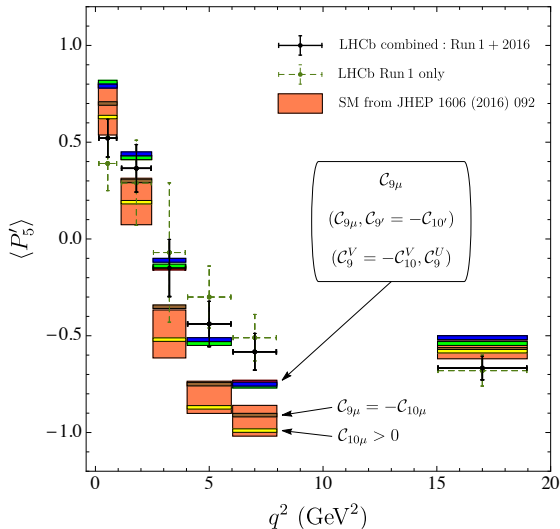
Scenarios for LFU and LFUV C_i [2020]

Scenario	Best-fit point	1σ	2σ	Pull _{SM}	p-value	
Sc. 5	$C_{9\mu}^V$	-0.54	[-1.06, -0.06]	[-1.68, +0.39]	6.0	39.4 %
	$C_{10\mu}^V$	+0.58	[+0.13, +0.97]	[-0.48, +1.33]		
	$C_9^U = C_{10}^U$	-0.43	[-0.85, +0.05]	[-1.23, +0.67]		
Sc. 6	$C_{9\mu}^V = -C_{10\mu}^V$	-0.56	[-0.65, -0.47]	[-0.75, -0.38]	6.2	41.4 %
	$C_9^U = C_{10}^U$	-0.41	[-0.53, -0.29]	[-0.64, -0.16]		
Sc. 7	$C_{9\mu}^V$	-0.84	[-1.15, -0.54]	[-1.48, -0.26]	6.0	36.5 %
	C_9^U	-0.25	[-0.59, +0.10]	[-0.92, +0.47]		
Sc. 8	$C_{9\mu}^V = -C_{10\mu}^V$	-0.34	[-0.44, -0.25]	[-0.54, -0.16]	6.5	48.4 %
	C_9^U	-0.80	[-0.98, -0.60]	[-1.16, -0.39]		
Sc. 9	$C_{9\mu}^V = -C_{10\mu}^V$	-0.66	[-0.79, -0.52]	[-0.93, -0.40]	5.7	28.4 %
	C_{10}^U	-0.40	[-0.63, -0.17]	[-0.86, +0.07]		
Sc. 10	$C_{9\mu}^V$	-1.03	[-1.18, -0.87]	[-1.33, -0.71]	6.2	41.5 %
	C_{10}^U	+0.28	[+0.12, +0.45]	[-0.04, +0.62]		
Sc. 11	$C_{9\mu}^V$	-1.11	[-1.26, -0.95]	[-1.40, -0.78]	6.3	43.9 %
	$C_{10'}^U$	-0.29	[-0.44, -0.15]	[-0.58, -0.01]		
Sc. 12	$C_{9'\mu}^V$	-0.06	[-0.21, +0.10]	[-0.37, +0.26]	2.1	2.2 %
	C_{10}^U	+0.44	[+0.26, +0.62]	[+0.09, +0.81]		
Sc. 13	$C_{9\mu}^V$	-1.16	[-1.31, -1.00]	[-1.46, -0.83]	6.2	49.2 %
	$C_{9'\mu}^V$	+0.56	[+0.27, +0.83]	[-0.02, +1.10]		
	C_{10}^U	+0.28	[+0.08, +0.49]	[-0.11, +0.70]		
	$C_{10'}^U$	+0.01	[-0.19, +0.22]	[-0.40, +0.42]		

Consistency of scenarios with $B \rightarrow K^* \mu\mu$ data

- ▶ Increase of significance for some scenarios (up to 0.8σ), but same hierarchies

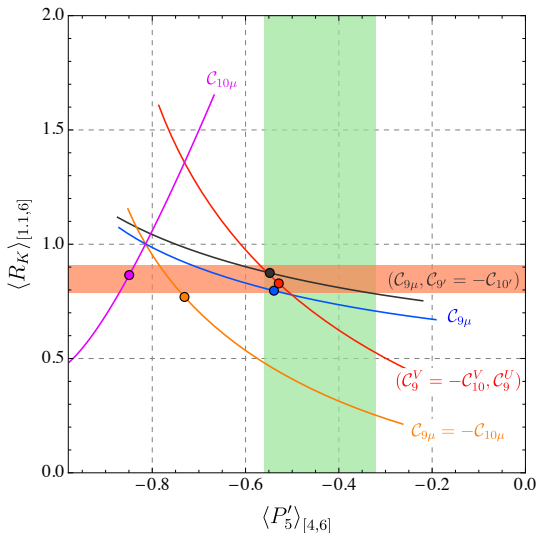
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- ▶ Reduction of the internal inconsistencies of the fit
 - ▶ for P'_5

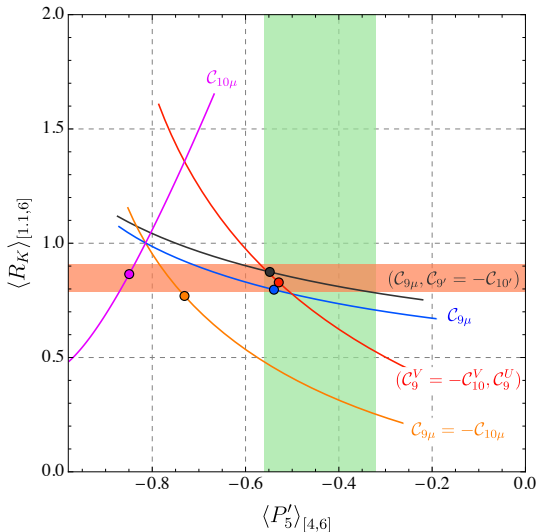
for some of the scenarios

Consistency of scenarios with $B \rightarrow K^* \mu \mu$ data



- ▶ Increase of significance for some scenarios (up to 0.8σ), but same hierarchies
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 - ▶ for P'_5
 - ▶ between P'_5 and R_K
- for some of the scenarios

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- ▶ Reduction of the internal inconsistencies of the fit
 - ▶ for P'_5
 - ▶ between P'_5 and R_K
- for some of the scenarios
- ▶ p -value of SM decreased to 1.4%

An EFT interpretation: SMEFT

Connect $b \rightarrow sll$ and $b \rightarrow cl\nu$ anomalies within SMEFT ($\Lambda_{NP} \gg m_{t,W,Z}$)

$$\mathcal{L}_{SMEFT} = \mathcal{L}_{SM} + \mathcal{L}_{d>4}$$

with higher-dim ops involving only SM fields

[Grzadkowski, Iskrzynski, Misiak, Rosiek ; Alonso, Grinstein, Camalich]

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- ▶ Two ops. with left-handed doublets

$$\mathcal{O}_{ijkl}^{(1)} = [\bar{Q}_i \gamma_\mu Q_j][\bar{L}_k \gamma^\mu L_l] \quad \mathcal{O}_{ijkl}^{(3)} = [\bar{Q}_i \gamma_\mu \vec{\sigma} Q_j][\bar{L}_k \gamma^\mu \vec{\sigma} L_l]$$

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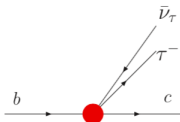
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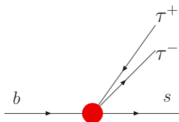
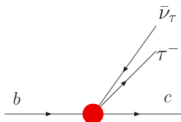
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- ▶ FCNC part of $\mathcal{O}_{2333}^{(1,3)}$ with $\mathcal{C}_{2333}^{(1)} = \mathcal{C}_{2333}^{(3)}$ [Capdevila, Crivellin, SDG, Hofer, Matias]

- ▶ Large NP contribution $b \rightarrow s\tau\tau$ through $\mathcal{C}_{9\tau}^V = -\mathcal{C}_{10\tau}^V$
- ▶ Avoids bounds from $B \rightarrow K^{(*)}\nu\nu$, Z decays, direct production in $\tau\tau$



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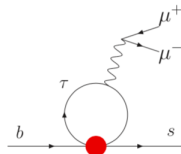
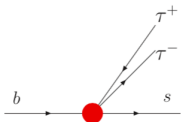
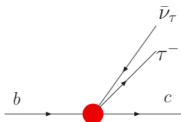
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- ▶ Avoids bounds from $B \rightarrow K^{(*)}\nu\nu$, Z decays, direct production in $\tau\tau$
- ▶ Through radiative effects. (small) NP contribution to \mathcal{C}_a^U



An EFT interpretation: B anomalies

Scenario LFU + LFUV NP (Sc 8)

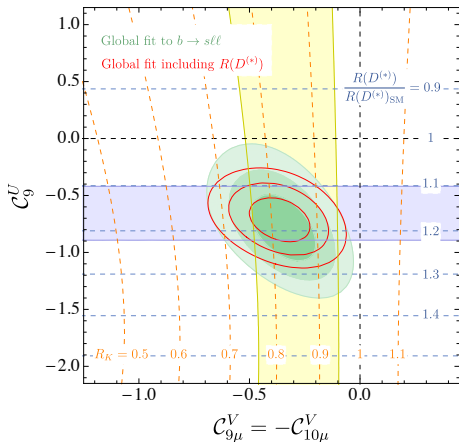
- ▶ $C_{9\mu}^V = -C_{10\mu}^V$ from small \mathcal{O}_{2322}
[$b \rightarrow s\mu\mu$]
- ▶ C_9^U from radiative corr from large \mathcal{O}_{2333}
[$b \rightarrow c\tau\nu$ and $b \rightarrow s\mu\mu$]

Generic flavour struct and NP at scale Λ

$$C_9^U \approx 7.5 \left(1 - \sqrt{\frac{R_{D^{(*)}}}{R_{D^{(*)},SM}}} \right) \times \left(1 + \frac{\log(\Lambda^2/(1\text{TeV}^2))}{10.5} \right)$$

- ▶ Agreement with (R_D, R_{D^*}) for $\Lambda = 1 - 10$ TeV
- ▶ Scenario 8 has Pull_{rmSM} of 7.4σ once R_{D^*} included
- ▶ Huge enhancement of $b \rightarrow s\tau\tau$ modes $O(10^{-4})$ [Capdevila, Crivellin, SDG, Hofer, Matias]

$$\text{Br}(B_s \rightarrow \tau^+\tau^-)_{\text{LHCb}} \leq 6.8 \times 10^{-3}, \quad \text{Br}(B \rightarrow K\tau^+\tau^-)_{\text{Babar}} \leq 2.25 \times 10^{-3}$$



Conclusions

Conclusions

New $B \rightarrow K^* \mu\mu$ data a very reassuring confirmation of the situation in $b \rightarrow sll$

- ▶ Increased consistency between $B \rightarrow K^* \mu\mu$ data and the rest of the global fit, in particular between R_K and P'_5
- ▶ Increase in the pull_{SM} of the favoured scenarios, no change in hierarchy of scenarios
- ▶ Possibility of right-handed currents in several favoured scenarios
- ▶ Possibility of LFU contributions, in good agreement with simple EFT interpretations combining $b \rightarrow cl\nu$ and $b \rightarrow sll$ anomalies
- ▶ Significant decrease of the p -value of the SM

Backup slides

Simplified U_1 -leptoquark model

- ▶ U_1 vector leptoquark $(\mathbf{3}, 1)_{2/3}$ couples quarks and leptons

$$\mathcal{L}_{U_1} \supset g_{lq}^{ij} (\bar{q}^j \gamma^\mu l^i) U_\mu + \text{h.c.}$$

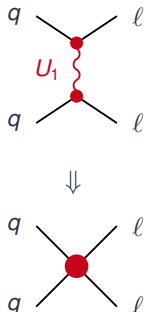
- ▶ Generates **semi-leptonic operators at tree-level**

$$[C_{lq}^{(1)}]_{ijkl} = [C_{lq}^{(3)}]_{ijkl} = -\frac{g_{lq}^{jk} g_{lq}^{il*}}{2M_U^2}$$

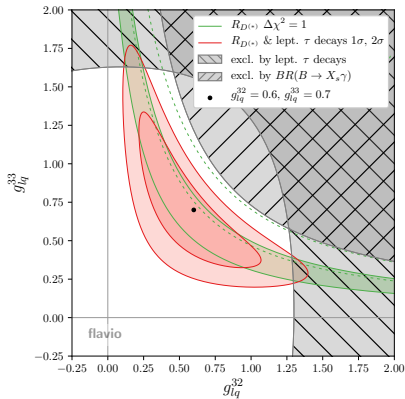
- ▶ And **dipole operators at one-loop**, e.g.

$$[O_{dV}]_{ij} = (\bar{q}_i \sigma^{\mu\nu} V_{\mu\nu} d_j) \varphi, \quad V \in \{W, B, G\}:$$

$$[C_{dV}]_{23} = \kappa_V \frac{Y_b}{16\pi^2} \sum_i \frac{g_{lq}^{i2} g_{lq}^{i3*}}{M_U^2}, \quad \kappa_W = \frac{g}{6}, \quad \kappa_B = \frac{-4g'}{9}, \quad \kappa_V = \frac{-5g_s}{12}$$



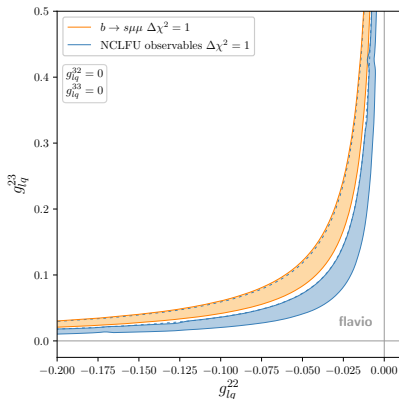
Simplified U_1 -leptoquark model



- ▶ $R_{D^{(*)}}$ mostly depends on **tauonic couplings** g_{lq}^{32}, g_{lq}^{33}
- ▶ Dipole operators contribute to **$BR(B \rightarrow X_s \gamma)$**
- ▶ RG running contributes to **leptonic τ decays**
- ▶ Well defined allowed region for explaining $R_{D^{(*)}}$, select **benchmark point**

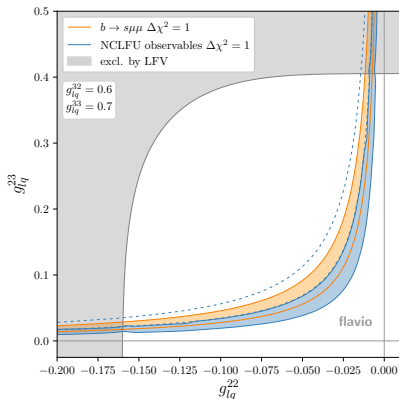
$$g_{lq}^{32} = 0.6, \quad g_{lq}^{33} = 0.7$$

Simplified U_1 -leptoquark model



- ▶ $R_{K^{(*)}}$ can be explained by **muonic couplings** g_{lq}^{22}, g_{lq}^{23}
- ▶ **Vanishing tauonic couplings:**
Tension between fits to $R_{K^{(*)}}$ and $b \rightarrow s\mu\mu$ observables after Moriond 2019

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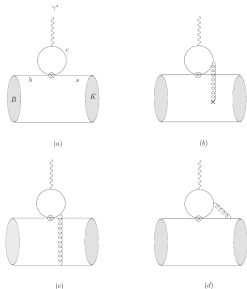
- ▶ $R_{K^{(*)}}$ can be explained by **muonic couplings** g_{lq}^{22}, g_{lq}^{23}
- ▶ **Vanishing tauonic couplings:**
Tension between fits to $R_{K^{(*)}}$ and $b \rightarrow s\mu\mu$ observables after Moriond 2019
- ▶ Benchmark point explaining $R_{D^{(*)}}$,

$$g_{lq}^{32} = 0.6, \quad g_{lq}^{33} = 0.7,$$

implies non-zero $C_9^{\text{univ.}}$, $R_{K^{(*)}}$ and $b \rightarrow s\mu\mu$ in good agreement after Moriond 2019

- ▶ Constraint from **LFV observables**

Pending questions



► Estimate of **soft-gluon $c\bar{c}$ contribution** from Light-Cone Sum Rules

- Several $c\bar{c}$ contributions, with hard and soft gluons (hard to estimate)
- Soft-gluon correction from LCSR smaller than thought ? [Gubernari, Van Dyk]
- Impact on contribution to be worked out (not used at face value in fits)

► **Narrow-width approx** for form factors

- Not problem for K or ϕ , but for K^* ?
- Lattice QCD : other collaborations ?
- K^* -meson LCSR: not able to catch the effect (need to use $K\pi$ DAs)
- B -meson LCSR: universal 10% effect, increasing SM discrepancy

[Khodjamirian, SDG, Virto]

