



# Studies of top quark spin and polarization in CMS

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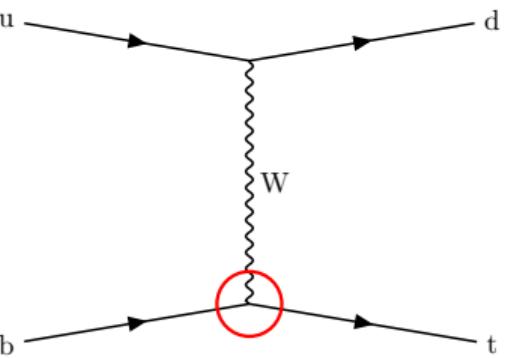
15th International workshop on top quark physics  
Durham (UK), September 6th, 2022



Institute of High Energy Physics  
Chinese Academy of Sciences

# Introduction

- Top quark is the heaviest fermion in the SM
  - Mean lifetime ( $\approx 10^{-25}$  s) much shorter than typical QCD timescales
- **Top quark decays before QCD can randomize its spin**
- **Pure EW decay** (plus V–A kind of interaction) preserves strong **angular correlations among decay products**
- $t\bar{t}$ : largest cross section but no single spin configuration in any basis
  - Process initiated by QCD ( $gg \rightarrow t\bar{t}$ )



- ***t*-channel single-top:** production through  $Wtb$  vertex (V–A interaction)
  - **Strongly polarized top quarks**

Spin and polarization

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Introduction

Spin asymmetry in single top

Spin asymmetry in  $t\bar{t}$

Spin coefficients in  $t\bar{t}$

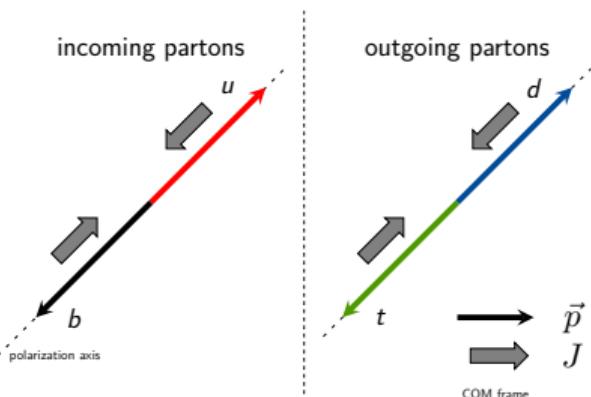
Projections at the HL-LHC

Summary

# Introduction

- Incoming partons ( $ub$ ) back-to-back in center-of-momentum (COM) frame
- **V-A interaction** at Wub vertex  $\implies u,b$  have **LH chirality**
- **Ultra-relativistic regime** at LHC  $\implies$  helicity == chirality  $\implies u,b$  have **LH helicity**
  - Spin projection is 0
- $d$  is ultra-relativistic  $\implies d$  is LH
- **Conservation of angular momentum**  $\implies t$  is LH **in this frame**
  - Polarization is frame-dependent

<sup>1</sup>See e.g., Phys. Lett. B 476 (2000) 323



- Experimental and theoretical arguments<sup>1</sup>  $\implies$  use **top quark rest frame; project along spectator quark direction**

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- Study **top quark** polarization via its **decay products**
- **Powerful observable:** top quark polarization angle  $\cos \theta_{\text{pol}}^*$ :

$$\cos \theta_{\text{pol}}^* = \frac{\vec{p}_{q'}^* \cdot \vec{p}_\ell^*}{|\vec{p}_{q'}^*| |\vec{p}_\ell^*|}$$

where  $\ell \equiv$  lepton from t decay;  $q' \equiv$  spectator quark;  $* \equiv$  t quark rest frame

- It also holds that:

$$\frac{1}{\sigma} \frac{d\sigma}{d \cos \theta_{\text{pol}}^*} = \frac{1}{2} \left( 1 + 2A_\ell \cos \theta_{\text{pol}}^* \right)$$

where the top quark spin asymmetry is connected to the polarization  $P$  via

$$A_\ell = \frac{1}{2} P \alpha_\ell, \quad \alpha_\ell \approx 1, \text{ lepton spin analyzing power}$$

Spin and polarization

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Spin asymmetry in tZq

Spin coefficients in tt

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# Spin asymmetry from t-channel single top,

Eur. Phys. J. C 80 (2020) 370



- **t-channel single top quark**

- $L \simeq 36 \text{ fb}^{-1}$

- Target: **leptonic ( $\mu, e$ ) top quark decay**

- Select events with exactly one isolated lepton

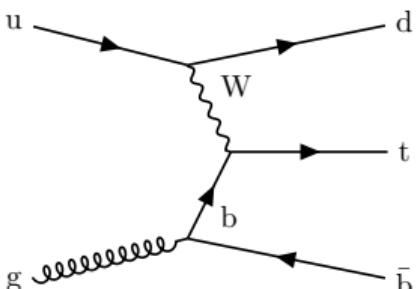
- **Main background:**  $t\bar{t}$ ; other backgrounds:  $tW$ ,  $V+jets$ , QCD

- Events split into **NjMb categories**

- 2j1b, signal enriched
  - 3j2b, to constrain  $t\bar{t}$  background
  - 2j0b, for validation purposes (not used in final fit)

- **Top quark candidate** is reconstructed in 2j1b:

- Get  $p_{z,\nu_\ell}$  by constraining  $\vec{p}_T^{\text{miss}}$  and  $\ell$  to  $m_W$
  - Build candidate from 4 momenta of  $\ell$ ,  $\nu_\ell$  and b jet



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Spin asymmetry in single top

Spin asymmetry in  $tZq$

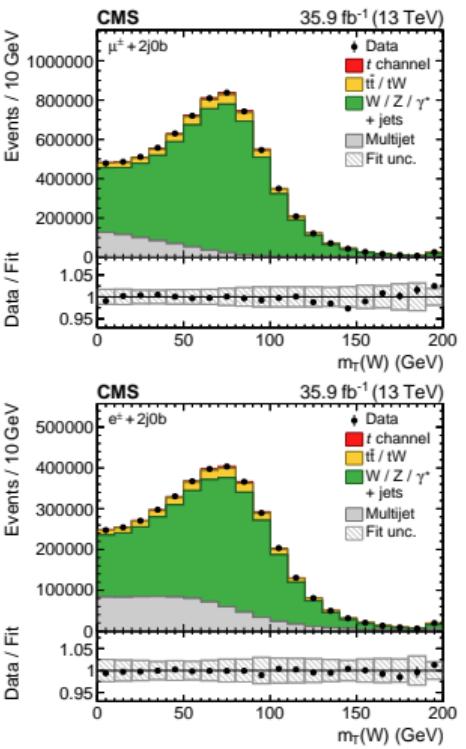
Spin coefficients in  $t\bar{t}$

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Summary

# Multijet background estimation

- Multijet background estimated with **two-step procedure**:
  - ① Distributions from multijet events estimated from **sideband region in data**
  - ② Normalization estimated through a **maximum-likelihood (ML) fit** to the data
- Definition of **sideband region**:
  - Muon channel: invert relative isolation requirement
  - Electron channel: fail loose ID criteria
- **Validate the background estimation in 2j0b category**
  - Has similar background composition of signal enriched 2j1b category
  - Not used in the final fit



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Spin asymmetry in single top

Spin asymmetry in tZq

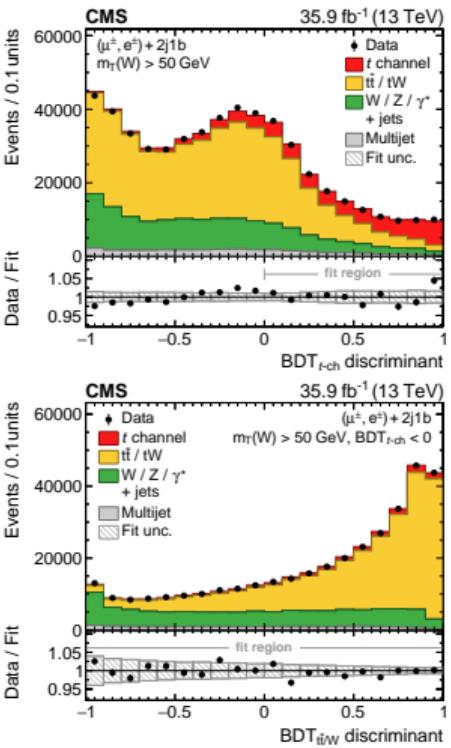
Spin coefficients in tt

Projections at the HL-LHC

Summary

# Signal extraction

- Train a  $BDT_{t\text{-ch}}$  to separate signal from  $t\bar{t}$ ,  $W+\text{jets}$  and QCD
  - Good separation power, but **similar shapes for  $t\bar{t}$  and  $W+\text{jets}$**
- Train a  $BDT_{t\bar{t}/W}$  to separate  $t\bar{t}$  from  $W+\text{jets}$
- ML fit performed using:
  - $BDT_{t\text{-ch}}$ ,  $BDT_{t\bar{t}/W}$ ,  $m_T(W)$  in 2j1b
  - $m_T(W)$  in 3j2b
- For each differential cross section measurement, observable is divided in intervals and **independent fit is performed in each interval**
- **Unfold** the resulting spectra **at parton level**



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Spin asymmetry in single top

Spin asymmetry in  $t\bar{Z}q$

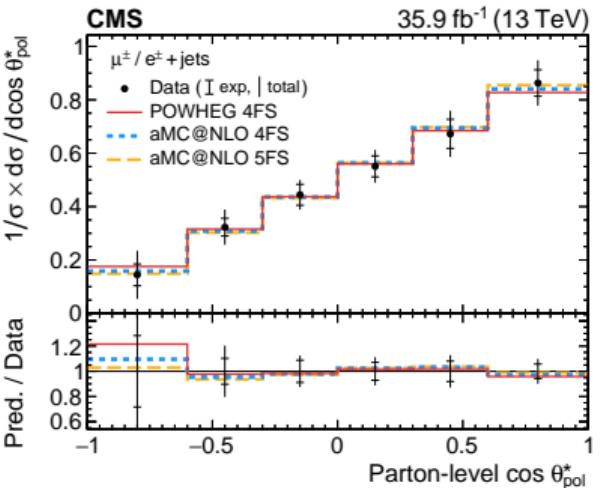
Spin coefficients in  $t\bar{t}$

Projections at the HL-LHC

Summary

# Results

- Spin asymmetry determined from parton-level  $\frac{1}{\sigma} \frac{d\sigma}{d \cos \theta_{\text{pol}}^*}$
- **Linear  $\chi^2$  fit** based on previously discussed functional dependence
- $A_\ell = 0.440 \pm 0.031(\text{stat+exp}) \pm 0.062(\text{theo})$
- **Good agreement with SM prediction** of 0.436 (POWHEG at NLO with negligible uncertainty)
- **Rules out a previous<sup>2</sup>  $2.0\sigma$  tension** found by CMS at  $\sqrt{s} = 8$  TeV



- Dominant uncertainties
  - Top quark mass
  - $t\bar{t}$  parton shower

<sup>2</sup>JHEP 04 (2016) 073

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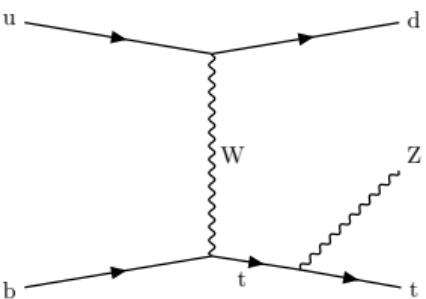
Spin coefficients in  $t\bar{t}$

Projections at the HL-LHC

Summary

# Spin asymmetry from tZq events, JHEP 02 (2022) 107

- **t-channel single top quark plus a Z boson**
  - $L \simeq 138 \text{ fb}^{-1}$
- Target: **leptonic ( $\mu, e$ ) top quark and Z decays**
  - Select events with exactly three isolated leptons (with an opposite-sign-same-flavor pair)
- **Main backgrounds:**
  - **Prompt leptons:** WZ+jets,  $t\bar{t}Z$ , ZZ
  - **Non-prompt leptons:**  $t\bar{t}$  dileptonic, DY
- Events split into NjMb categories
  - $1 < j < 4; \geq 1b$
  - $\geq 4j; \geq 1b$  ( $t\bar{t}Z$  control region)
- Several validation regions defined to validate background modeling



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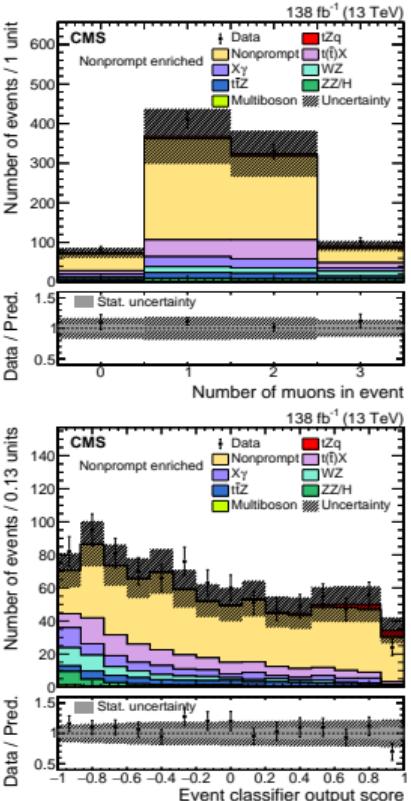
Spin coefficients in  $t\bar{t}$

Projections at the HL-LHC

Summary

# Non-prompt background estimation

- Non-prompt background estimated with **fake rate method**
- Estimate **probability (fake rate) for a non-prompt lepton to pass analysis cuts**
  - Measured in a QCD enriched data sample
- Define two **lepton** selections: **loose and tight**
- Define a region identical to signal region but with at least one loose-non-tight lepton
- **Apply fake rate** there to get non-prompt yield in signal region
- **Validate method** in dedicated non-prompt lepton validation region



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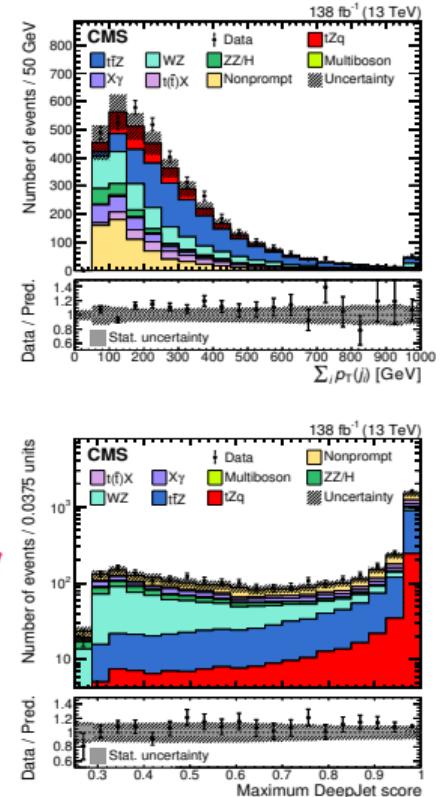
Spin coefficients in tt

Projections at the HL-LHC

Summary

# Signal extraction

- Train a multiclass neural network (NN)
  - 22 input features
- 5 output nodes:
  - 1 tZq
  - 2 ttZ
  - 3 WZ
  - 4 ttX
  - 5 Others
- ML fit performed using:
  - tZq NN node in signal region
  - ttZ NN node in ttZ control region
  - $m_T^W$  in WZ control region
  - $n_e$  in  $Z\gamma$  control region
  - Counting in ZZ and non-prompt control regions



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Spin asymmetry in tZq

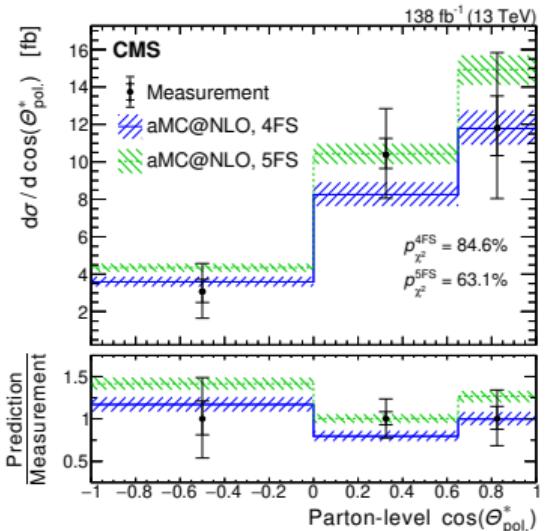
Spin coefficients in tt

Projections at the HL-LHC

Summary

# Results

- Spin asymmetry determined from parton-level  $\frac{1}{\sigma} \frac{d\sigma}{d \cos \theta_{\text{pol}}^*}$
- $A_\ell$  parametrized based on previously discussed functional dependence and fitted
- $A_\ell = 0.54 \pm 0.16(\text{stat}) \pm 0.06(\text{syst})$
- **Good agreement with SM prediction** of 0.44 (0.45) by MADGRAPH5\_aMC@NLO in the 4FS (5FS)
- Measurement is **statistically dominated** in tZq channel



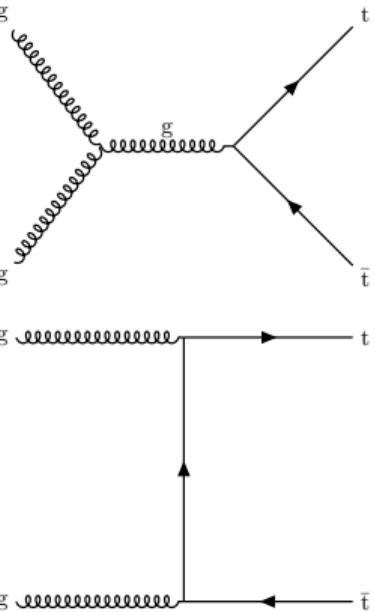
- Dominant uncertainties
  - Background modeling
  - b tagging efficiency
  - Jet energy scale

# Polarization and spin coefficients in $t\bar{t}$ , Phys. Rev. D 100, 072002 (2019)



- Top quarks mainly produced in pairs at the LHC
- $t\bar{t}$  pairs are **unpolarized at tree level**
  - Parity conserving and time invariant QCD production
- Small **sources of polarization** come from
  - EW corrections
  - Absorptive terms at one loop
- Measure all the independent coefficients of the spin-dependent part of the  **$t\bar{t}$  production density matrix,  $R$**
- Due to very narrow top quark width we can factorize production ( $R$ ) and decay ( $\rho$ ) processes

$$\mathcal{M}(gg/\text{qq} \rightarrow t\bar{t} \rightarrow \ell^+ \nu b \ell^- \bar{\nu} b) \propto \rho R \bar{\rho}$$



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Spin  
asymmetry in  
single top

Spin  
asymmetry in  
 $tZq$

Spin  
coefficients in  
 $t\bar{t}$

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# Introduction

- The production spin density matrix  $R$  can be decomposed like

$$R \propto \tilde{A} \mathbb{1} \otimes \mathbb{1} + \tilde{B}_i^+ \sigma^i \otimes \mathbb{1} + \tilde{B}_i^- \mathbb{1} \otimes \sigma^i + \tilde{C}_{ij} \sigma^i \otimes \sigma^j$$

with

- $\tilde{B}^\pm \equiv$  3-D vector of  $t$  and  $\bar{t}$  polarization in each direction
- $\tilde{C} \equiv$  3x3 matrix of coefficients for spin correlations between  $t$  and  $\bar{t}$
- Total: 15 coefficients**, measured wrt a convenient set of 3 orthonormal axes
- It also holds true that

$$\frac{1}{\sigma} \frac{d^2\sigma}{d \cos \theta_1^i d \cos \theta_2^j} = \frac{1}{4} \left( 1 + B_1^i \cos \theta_1^i + B_2^j \cos \theta_2^j - C_{ij} \cos \theta_1^i \cos \theta_2^j \right)$$

with  $\theta_1^i$  ( $\theta_2^j$ )  $\equiv$  angle of + (-) charged lepton wrt axis i (j) in rest frame of  $t$  ( $\bar{t}$ )

- Integrating one angle out we get **15 single-differential distributions to measure**

Spin and polarization

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Spin asymmetry in  $t\bar{Z}q$

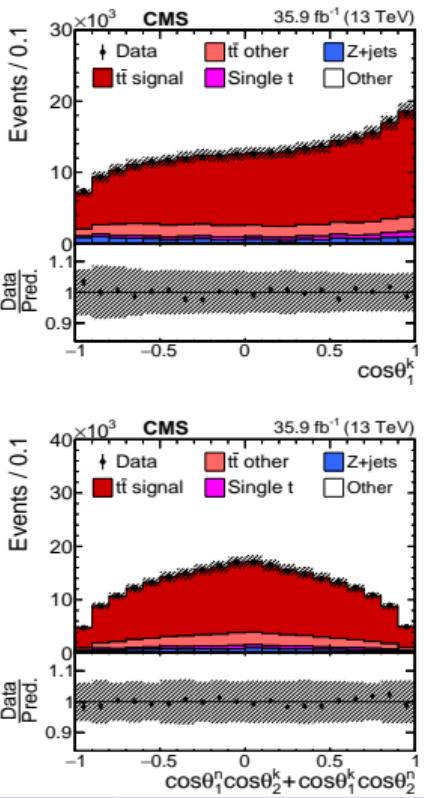
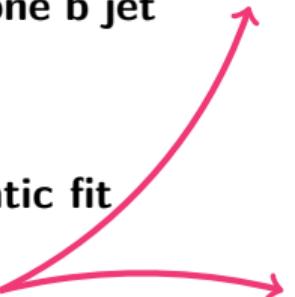
Spin coefficients in  $t\bar{t}$

Projections at the HL-LHC

Summary

# Signal selection

- **$t\bar{t}$  production**
  - $L \simeq 36 \text{ fb}^{-1}$
- Target: **dileptonic** ( $\mu^+\mu^-$ ,  $e^+e^-$ ,  $e^\pm\mu^\mp$ ) decays
- Ask for **exactly two leptons** with opposite charge, **at least two jets**, **at least one b jet**
- **Main backgrounds:** other  $t\bar{t}$  decay channels,  $tW$  and  $Z+jets$
- Reconstruct top quarks with **kinematic fit** constrained to  $W$  and  $t$  masses
- Build angular observable of interest
- Compute differential spectra and unfold and parton level



Spin and polarization

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Spin asymmetry in single top

Spin asymmetry in  $tZ$

Spin coefficients in  $t\bar{t}$

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# Results

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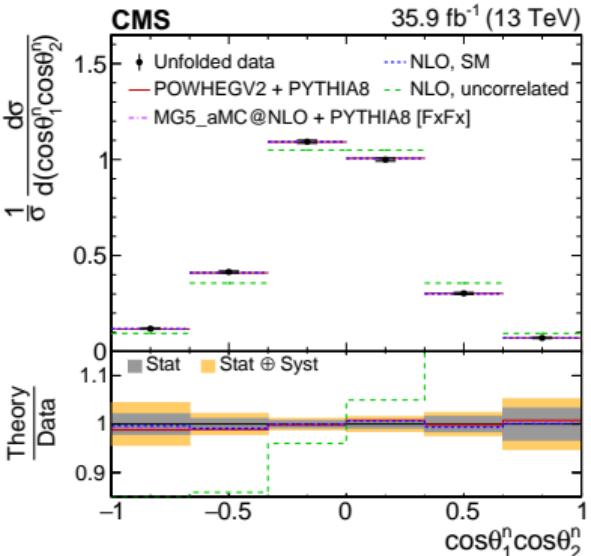
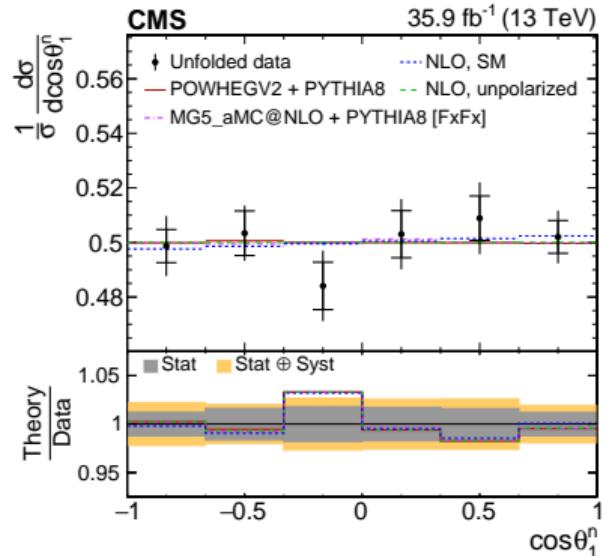
Spin asymmetry in single top

Spin asymmetry in tZq

Spin coefficients in tt

Projections at the HL-LHC

Summary



- Left: measurement is not sensitive to tiny polarization effects in the SM
- Right:** measurement is **sensitive to spin correlation effects**

# Results

Spin and polarization

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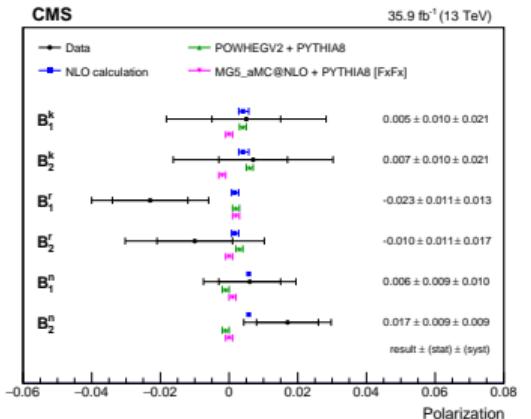
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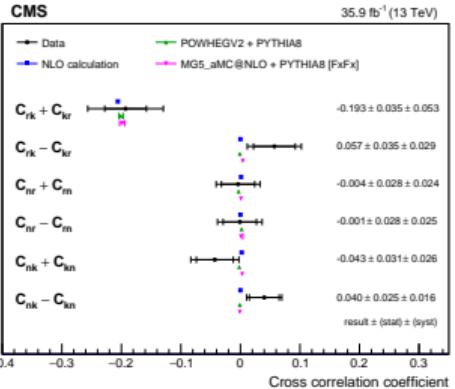
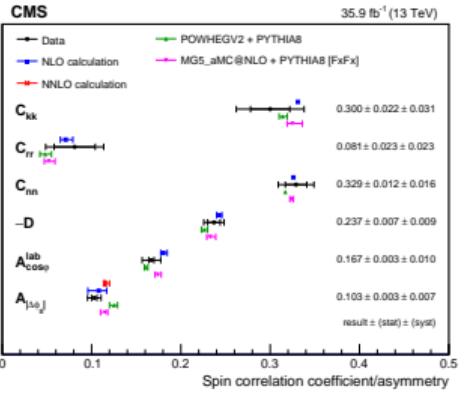
Spin coefficients in tt

Projections at the HL-LHC

Summary



- Good agreement between measured and predicted values for all the coefficients
- Statistical and systematic uncertainties are in general comparable

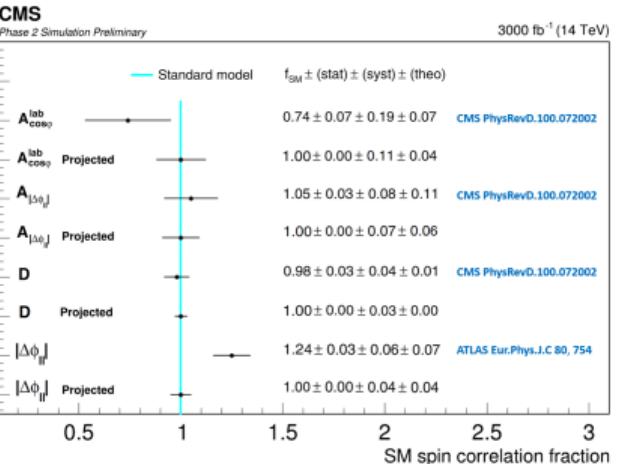


# Projection of spin correlation measurements at the HL-LHC

## CMS-PAS-FTR-18-034



- Same mathematical framework of previous result
- Similar selection in terms of objects
  - Only use  $e\mu$  channel
- Assume trigger and detector performance similar to Run2
- Assume better control of theory and experimental uncertainties
- Unprecedented precision in spin correlation observables is expected



- Can solve the  $|\Delta\phi_{ee}|$  puzzle
- $2.2\sigma$  tension seen by ATLAS<sup>3</sup>...
  - ...but not by CMS

<sup>3</sup>Eur. Phys. J. C 80 754

# Summary

- CMS has measured top quark spin and polarization properties using different processes
- Measured the **spin asymmetry using t-channel** single top quark events
  - Measurement is systematics dominated
- Measured the **spin asymmetry in** rarer **tZq** events
  - Measurement is statistics dominated
- Measured the **polarization and spin coefficients of the  $t\bar{t}$**  production matrix
  - Also projected to HL-LHC scenario
- **All results are in agreement with the SM** predictions within uncertainties
  - Previous moderate tensions in spin asymmetry ruled out by these results
- Not the end of the story!
  - Extend results to full Run2
  - Profit from Run3 data

**Stay tuned!**

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Spin  
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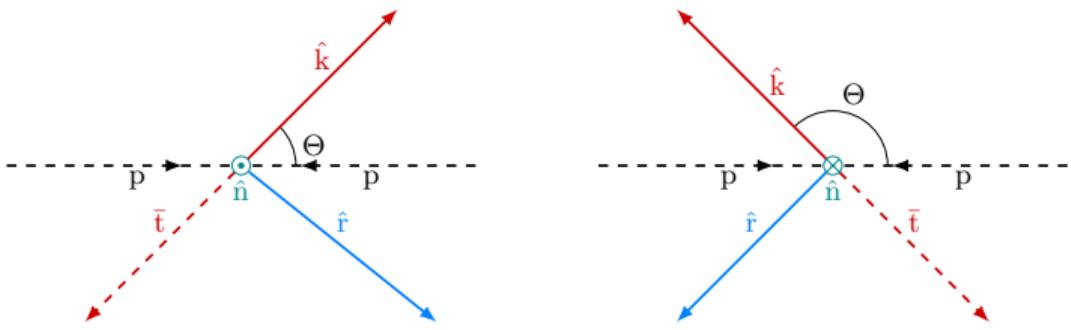
# Backup slides

# Orthonormal axes

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Spin coefficients in  $t\bar{t}$



- $\hat{k} \equiv$  top quark direction
- $\hat{n} = (\hat{p} \times \hat{k}) / \sin \Theta$        $\hat{p} \equiv$  incoming parton direction
- $\hat{r} = (\hat{p} - \hat{r} \cos \Theta) / \sin \Theta$

# Coefficients

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Spin coefficients in  $t\bar{t}$

Coefficient	Measured	PowhegV2	MG5	NLO
$B_1^k$	$0.005 \pm 0.023$	$0.004^{+0.001}_{-0.001}$	$0.000^{+0.001}_{-0.001}$	$4.0^{+1.7}_{-1.2} \times 10^{-3}$
$B_2^k$	$0.007 \pm 0.023$	$0.006^{+0.001}_{-0.001}$	$-0.002^{+0.001}_{-0.001}$	$4.0^{+1.7}_{-1.2} \times 10^{-3}$
$B_1^r$	$-0.023 \pm 0.017$	$0.006^{+0.001}_{-0.001}$	$0.002^{+0.001}_{-0.001}$	$1.6^{+1.2}_{-0.9} \times 10^{-3}$
$B_2^r$	$-0.010 \pm 0.020$	$0.003^{+0.001}_{-0.001}$	$0.000^{+0.001}_{-0.001}$	$1.6^{+1.2}_{-0.9} \times 10^{-3}$
$B_1^n$	$-0.006 \pm 0.013$	$-0.001^{+0.001}_{-0.001}$	$0.001^{+0.001}_{-0.001}$	$5.7^{+0.5}_{-0.4} \times 10^{-3}$
$B_2^n$	$0.017 \pm 0.013$	$-0.001^{+0.001}_{-0.001}$	$0.000^{+0.001}_{-0.001}$	$5.7^{+0.5}_{-0.4} \times 10^{-3}$
$C_{kk}$	$0.300 \pm 0.038$	$0.314^{+0.005}_{-0.004}$	$0.325^{+0.011}_{-0.006}$	$0.331^{+0.002}_{-0.002}$
$C_{rr}$	$0.081 \pm 0.032$	$0.048^{+0.007}_{-0.006}$	$0.052^{+0.007}_{-0.006}$	$0.071^{+0.008}_{-0.006}$
$C_{nn}$	$0.329 \pm 0.020$	$0.317^{+0.001}_{-0.001}$	$0.324^{+0.002}_{-0.002}$	$0.326^{+0.002}_{-0.002}$
$C_{rk} + C_{kr}$	$-0.193 \pm 0.064$	$-0.201^{+0.004}_{-0.003}$	$-0.198^{+0.004}_{-0.005}$	$-0.206^{+0.002}_{-0.002}$
$C_{rk} - C_{kr}$	$0.057 \pm 0.046$	$-0.001^{+0.002}_{-0.002}$	$0.004^{+0.002}_{-0.002}$	$0$
$C_{nr} + C_{rn}$	$-0.004 \pm 0.037$	$-0.003^{+0.002}_{-0.002}$	$0.001^{+0.002}_{-0.002}$	$1.6^{+0.01}_{-0.01} \times 10^{-3}$
$C_{nr} - C_{rn}$	$-0.001 \pm 0.038$	$0.002^{+0.002}_{-0.002}$	$0.001^{+0.003}_{-0.002}$	$0$
$C_{nk} - C_{kn}$	$-0.043 \pm 0.041$	$-0.002^{+0.002}_{-0.002}$	$0.003^{+0.002}_{-0.002}$	$2.15^{+0.04}_{-0.07} \times 10^{-3}$
$C_{nk} + C_{kn}$	$0.040 \pm 0.029$	$-0.001^{+0.002}_{-0.002}$	$-0.001^{+0.002}_{-0.002}$	$0$