

# QCD NLO corrections to $t\bar{t}Z$ production at the LHC including leptonic decays

Off-shell and parton-shower effects in  $t\bar{t}Z$  signatures



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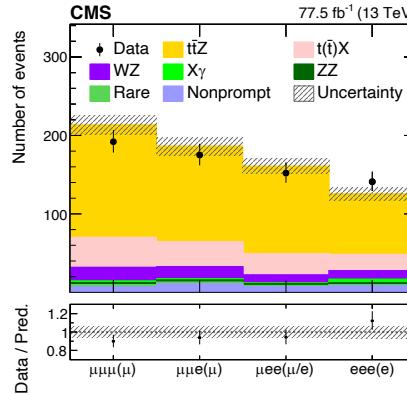
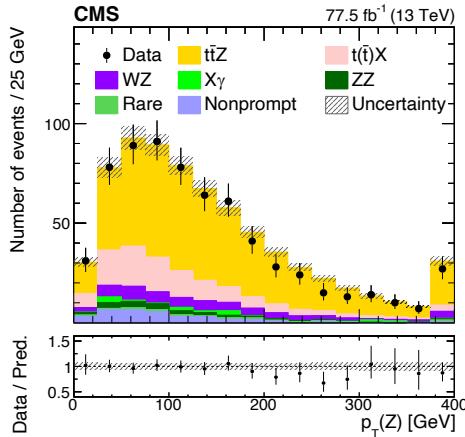
15th International Workshop on Top-Quark Physics (TOP 2022)  
Durham, UK - Sep 4-9, 2022

# $t\bar{t}Z$ at the LHC

- Crucial for a complete measurement of top-quark EW couplings  
(together with  $t\bar{t}W$ ,  $t\bar{t}\gamma$ ,  $t\bar{t}H$ , single-top processes, ...)
- Top-quark couplings @ (HL-)LHC as indirect probe of BSM physics
  - Top-quark, unique probe
  - (HL-)LHC: unprecedented number of top quarks
  - Unrivaled access to top-quark physics till future TeV-energy lepton collider
- Background to  $t\bar{t}H$ 
  - Need accurate modeling of both  $t\bar{t}Z$  and  $t\bar{t}W$  to measure  $t\bar{t}H$  ( $\rightarrow y t$ )
- Background to many searches of BSM physics
  - signatures with multi-leptons, b jets, and missing energy

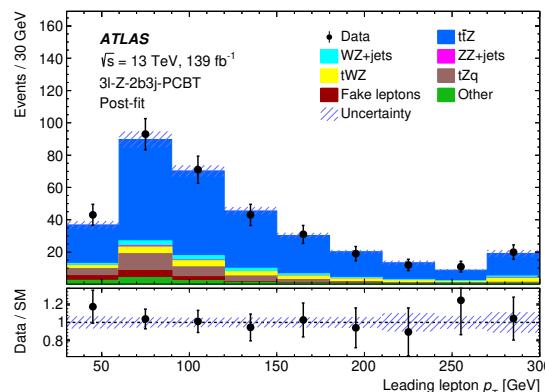
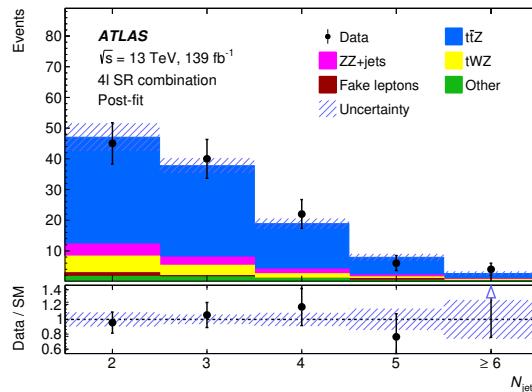
Received focused experimental and theoretical attention

# LHC Run2: access to event distributions



See talk by J. van der Linden

$t\bar{t}Z$  searches in 3l and 4l signatures



CMS [arXiv:1907.11270]

Interest in modelling  $t\bar{t}Z$  leptonic signatures

ATLAS [arXiv:2103.12603]

# Interpreting $t\bar{t}Z$ measurements ...

## Anomalous top couplings

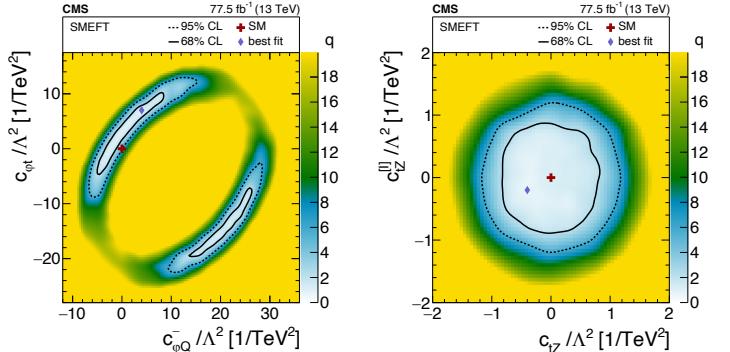
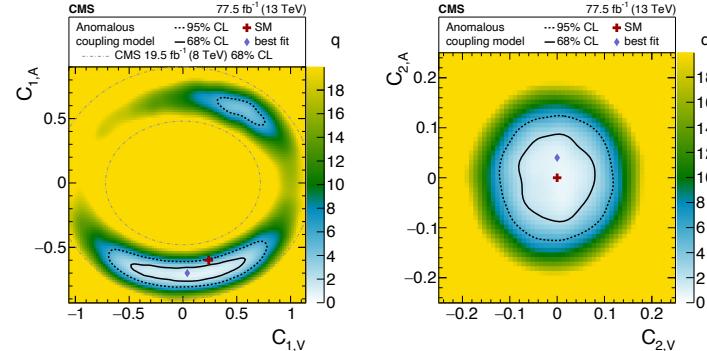
$$\mathcal{L} = e\bar{u}(p_t) \left[ \gamma^\mu (C_{1,V} + \gamma_5 C_{1,A}) + \frac{i\sigma^{\mu\nu} q_\nu}{M_Z} (C_{2,V} + i\gamma_5 C_{2,A}) \right] v(p_t) Z_\mu$$

## Effective operators

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \left( \frac{1}{\Lambda^2} \sum_i C_i O_i + \text{h.c.} \right) + O(\Lambda^{-4})$$

$$\begin{aligned} O_{uZ} &= -s_W O_{uB} + c_W O_{uW} \\ O_{uB} &= (\bar{q}\sigma^{\mu\nu} u)(\epsilon\varphi^* B_{\mu\nu}) \\ O_{uW} &= (\bar{q}\tau^I \sigma^{\mu\nu} u)(\epsilon\varphi^* W_{\mu\nu}^I) \\ O_{\varphi u} &= (\bar{u}\gamma^\mu u)(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi) \\ O_{\varphi q}^- &= O_{\varphi q}^1 - O_{\varphi q}^3 \\ O_{\varphi q}^1 &= (\bar{q}\gamma^\mu q)(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi) \\ O_{\varphi q}^3 &= (\bar{q}\tau^I \gamma^\mu q)(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi) \end{aligned}$$

...

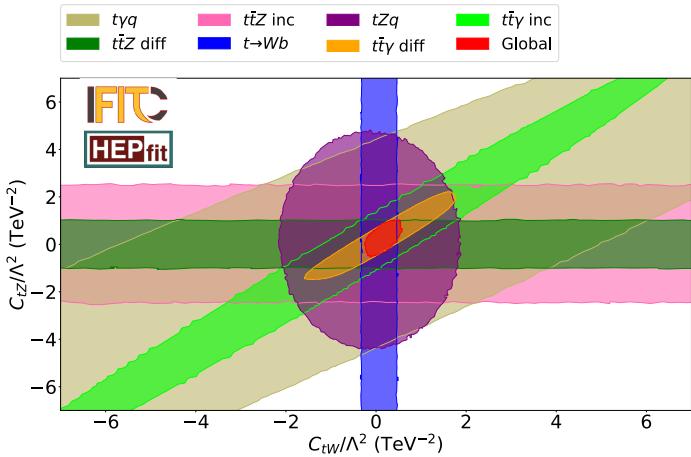
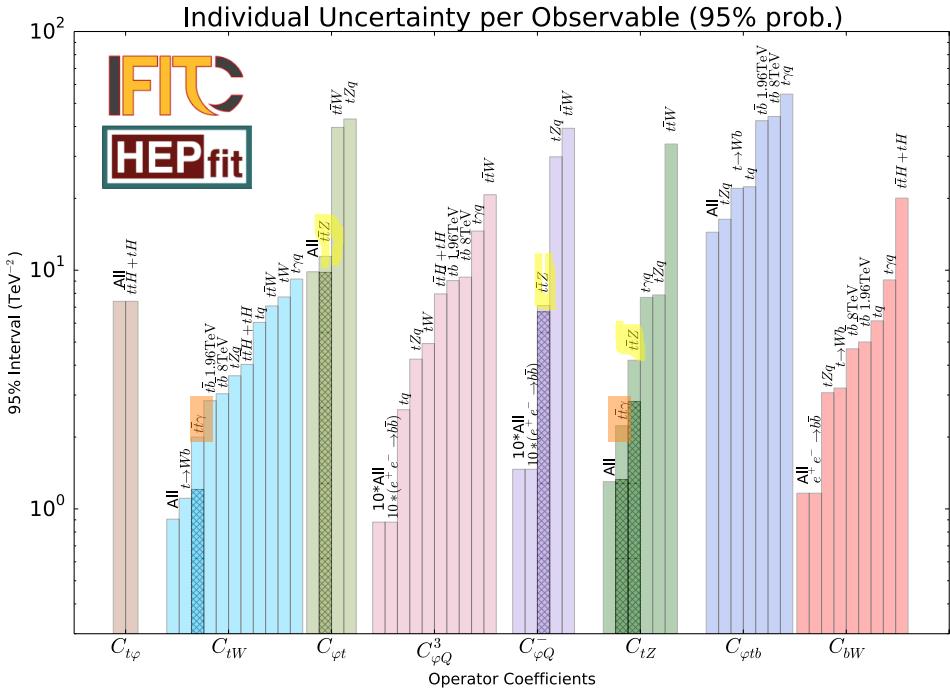


CMS [arXiv:1907.11270]

# ... through multiple and more sensitive probes

## Global fits of top observables

V Miralles, M. Miralles López, M. Moreno Llacer, A. Peñuelas, M. Perelló, M. Vos [arXiv:2107.13917]



Kinematic distributions add substantial constraining power

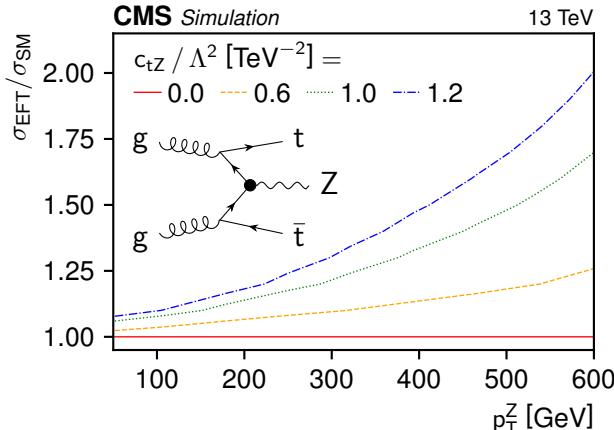
Accurate modelling of  $t\bar{t}Z$  differential cross sections and signatures is crucial

# ... and through new explorations



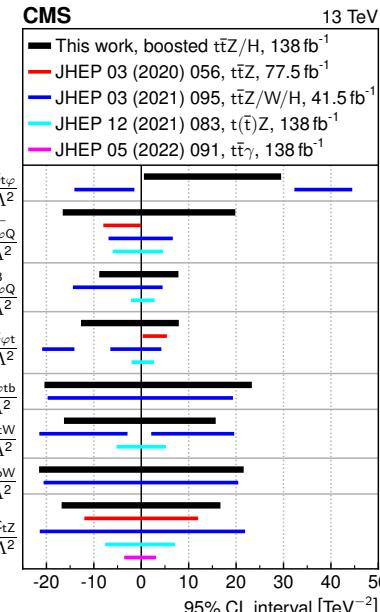
See talks by J. Wilson, M. Madigan, J. McFayden

## Top pair + boosted Z/H



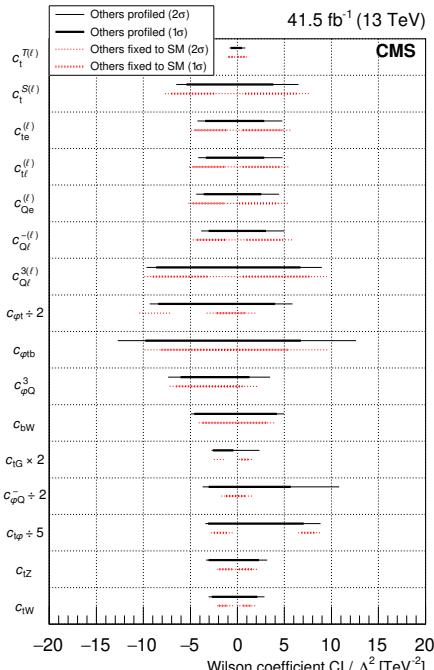
$$\delta\eta_{\text{SM}} \sim g_{\text{BSM}}^2 \frac{E^2}{M^2}$$

Effects in tails of distributions but also anomalous shapes



[CMS: arXiv:2208.12837]

## Top+additional leptons



[CMS: arXiv:2012.04120]

Pointing to the need for precision in modelling the complex signatures from  $t\bar{t}+X$  processes in regions where on-shell calculations may not be accurate enough

# $t\bar{t}Z$ hadronic production: theory overview

- On-shell  $t\bar{t}Z$ : NLO QCD and EW
  - Lazopoulos, McElmurry, Melnikov, Petriello, PLB 666 (2008) 62 [0804.2220]
  - Kardos, Trocsanyi, Papadopoulos, PRD 85 (2012) 054015 [1111.0610]
  - Maltoni, Pagani, Tsinikos, JHEP 02 (2016) 113 [1507.05640]
  - Frixione, Hirschi, Pagani, Zaro, JHEP 06 (2015) 184 [1504.03446]
- On-shell  $t\bar{t}Z$ : NNLL resummation
  - Broggio, Ferroglio, Ossola, Pecjak, Sameshima, JHEP 04 (2017) 105 [1702.00800]
  - Kulesza, Motyka, Schwartländer, Stebel, Theeuwes, Eur. Phys. J. C 79 (2019) 249 [1812.08622]
  - Broggio, Ferroglio, Frederix, Pagani, Pecjak, Tsinikos, JHEP 08 (2019) 039 [1907.04343]
  - Kulesza, Motyka, Schwartländer, Stebel, Theeuwes, Eur. Phys. J. C 80 (2020) 428 [2001.03031]
- On-shell  $t\bar{t}Z$ : NLO QCD+PS
  - Garzelli, Kardos, Papadopoulos, Trocsanyi, PRD 85 (2012) 074022 [1111.1444] (PowHel)
  - Garzelli, Kardos, Papadopoulos, Trocsanyi, JHEP 11 (2012) 056 [1208.2665] (PowHel)
  - Process available in MG5\_aMC@NLO, Sherpa, and Powheg-Box as well.

# On-shell $t\bar{t}Z$ : theory vs exp at a glance

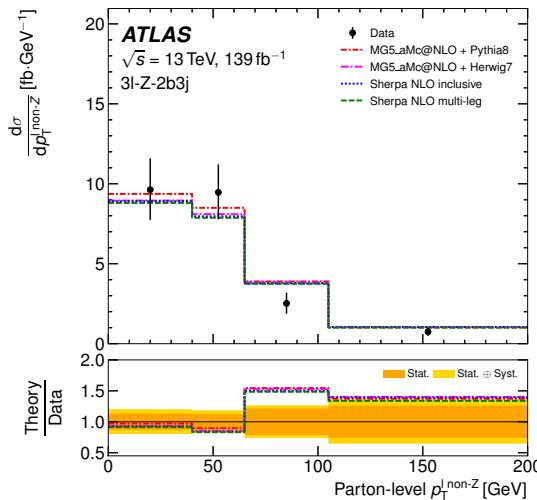
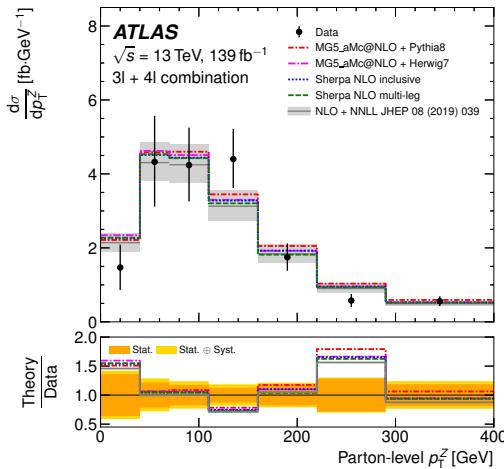
See talk by J. van der Linden

$$\left. \begin{array}{l} \text{NLO+NNLL: } 0.811^{+0.089(+11.0\%)}_{-0.078(-9.6\%)}{}^{+0.019(+2.4\%)}_{-0.019(-2.4\%)} \\ \text{ATLAS: } 0.99 \pm 0.05 \text{ (stat)} \pm 0.08 \text{ (syst)} \\ \text{CMS: } 0.95 \pm 0.05 \text{ (stat)} \pm 0.06 \text{ (syst)} \end{array} \right\}$$

[Broggio et al. arXiv:1907.04343]

[arXiv:2103.12603]

[arXiv:1907.11270]



Moving forward:

- Reduce theoretical systematics
- Describe full events more faithfully
  - Leptonic (and jet) observables
  - Z and tops off-shell

# $pp \rightarrow t\bar{t}Z$ : modeling events beyond on-shell production

- $pp \rightarrow t\bar{t}l^+l^-$  ( $l = \text{lepton}$ ): NLO QCD + PS

- On-shell top quarks with LO spin-correlations in decay ( $t \rightarrow b l \nu$ ) (using NWA)
- Include  $Zt\bar{t}$  off-shell effects and  $Zt\bar{t}/\gamma t\bar{t}$  interference
- Interfaced with PS in the Powheg-Box-V2 framework (including on-shell  $t\bar{t}Z$ )



M. Ghezzi, B. Jäger, S. Lopez, L. Reina, D. Wackerlo, [arXiv:2112.08892]]

- Fully off-shell  $pp \rightarrow e^+\nu_e\mu^-\bar{\nu}_\mu b\bar{b}\tau^+\tau^-$ : NLO QCD

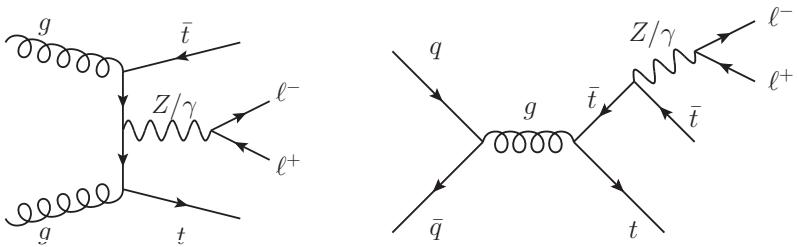
- Both double-, single-, and non resonant contributions, interferences, and off-shell effects of top, Z, W, and photon.
- All heavy resonances described by Breit-Wigner propagators.
- Comparison with NWA calculation.



See poster by J. Nasufi

G. Bevilacqua, H.B. Hartanto, M. Kraus, J. Nasufi, M. Worek [arXiv:2203.15688]

# pp $\rightarrow t\bar{t}l^+l^-$ matched to parton shower

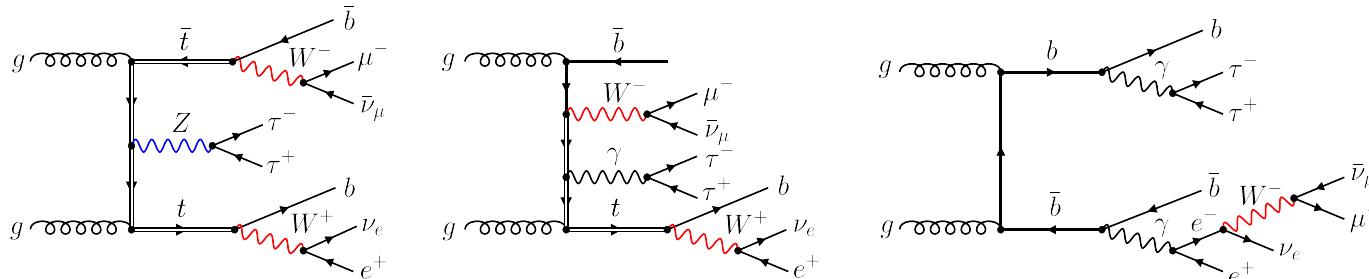


+ NLO QCD + PS

- One-loop matrix elements from NLOX [Honeywell, et al., arXiv:1812.11925]
- EW  $G_\mu$  input scheme ( $G_\mu, m_Z, m_W$ ). Other inputs:  $m_t, \Gamma_t, \Gamma_w, \Gamma_Z$
- Studied  $(\mu_R, \mu_F)$  scale dependence wrt to both a fixed and dynamical central scale (7-point variation)
 
$$\mu_0 = \frac{2m_t + m_Z}{2}$$

$$\mu_0 = \frac{M_T(e^+e^-) + M_T(t) + M_T(\bar{t})}{3}$$
- PDF: CT18NLO with  $\alpha_s(m_Z)=0.118$  ( $\alpha_s(\mu)$  in Msbar, 5FS)
- PS: Pythia8
- Specific signature studied:  $t\bar{t}e^+e^-$  with  $t \rightarrow b \mu v_\mu$  (with LO spin correlation)
  - $p_T^{e,\mu} > 10 \text{ GeV}, |\eta^{e,\mu}| < 2.5$
  - $|M_{ee} - m_Z| < 10 \text{ GeV}$  (to mimic exp. fiducial region)

# $pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \tau^+ \tau^-$ full off-shell description



+ NLO QCD

- NLO QCD corrections obtained in the HELAC-NLO framework [Bevilacqua et al., arXiv:110.1499]
  - One-loop matrix elements with HELAC-1LOOP. Real radiation with HELAC-DIPOLES.
- EW  $G_\mu$  input scheme ( $G_\mu, m_Z, m_W$ ). Other inputs:  $m_t, \Gamma_W, \Gamma_Z, \Gamma_t$  (LO, NLO, unstable-W and NWA)
- Unstable particles in complex mass scheme.
- Studied PDF dependence. Main results presented for NNPDF3.1
- Studied  $(\mu_R, \mu_F)$  scale dependence wrt to both a fixed and dynamical central scale (7-point variation)
- Specific signature studied:  $e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \tau^+ \tau^-$ 
  - $p_T^l > 20 \text{ GeV}, |y_l| < 2.5, \Delta R_{ll} > 0.4$
  - $p_T^b > 20 \text{ GeV}, |y_b| < 2.5, \Delta R_{bb} > 0.4$
  - $p_T^{\text{miss}} > 40 \text{ GeV}$

$$\mu_0 = \frac{2m_t + m_Z}{2} \quad \mu_0 = \frac{H_T}{3} \text{ for } H_T = \sum_i p_{T,i}$$

# Theoretical systematic: $pp \rightarrow t\bar{t}e^+e^-$

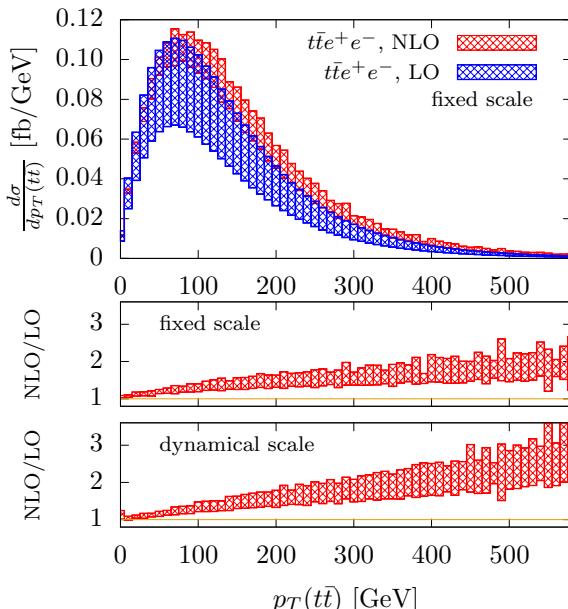
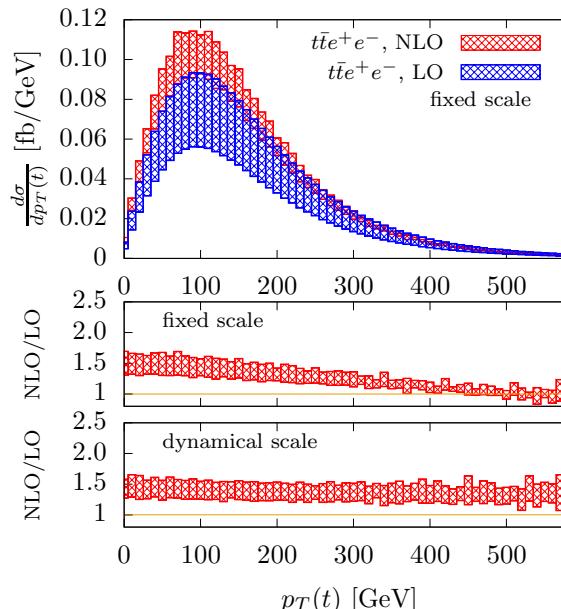
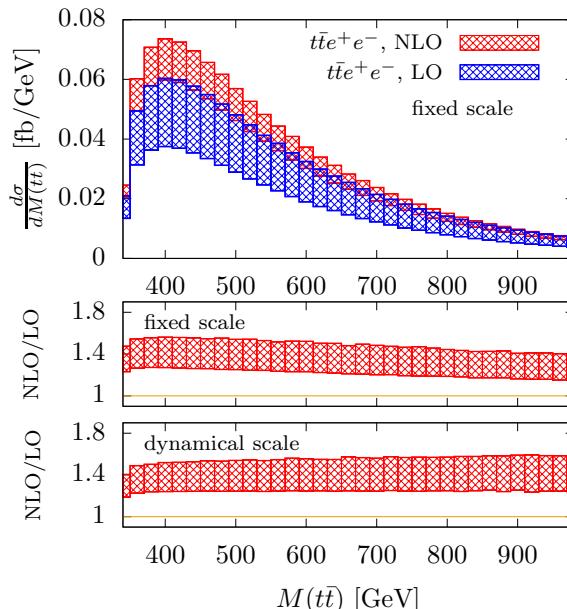
NLO QCD corrections are substantial and reduce the overall perturbative uncertainty

$$\sigma_{t\bar{t}e^+e^-}^{\text{LO}} = 15.9^{+5.1}_{-3.6} \text{ (} 15.8^{+5.0}_{-3.5} \text{)} \text{ fb}$$

$$\sigma_{t\bar{t}e^+e^-}^{\text{NLO}} = 21.9^{+2.0}_{-2.4} \text{ (} 22.1^{+2.2}_{-2.5} \text{)} \text{ fb}$$

Fixed and dynamic scales give very similar results (dyn. scale in parenthesis)

No uniform rescaling: different effects in different phase-space regions



# Theoretical systematics: $\text{pp} \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \tau^+ \tau^-$

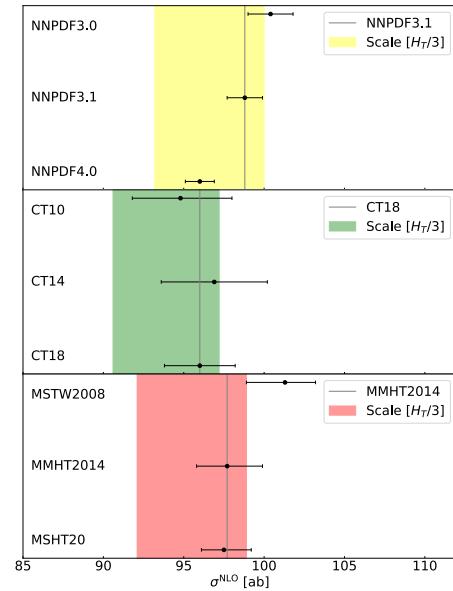
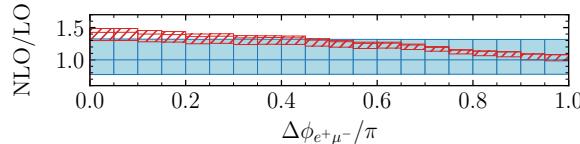
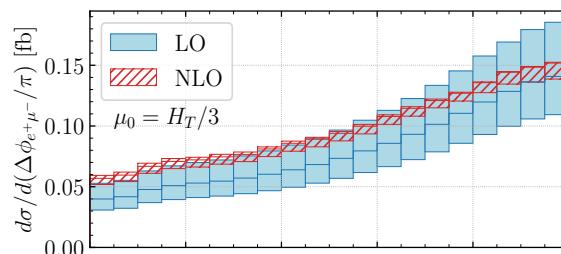
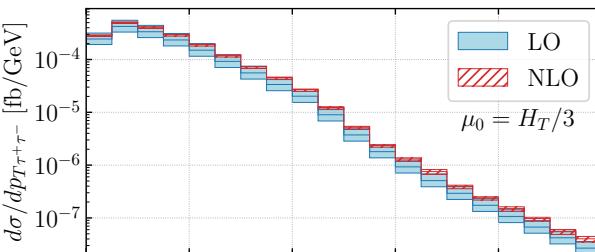
Very small residual systematic uncertainty at NLO QCD

$$\sigma_{\text{full off-shell}}^{\text{LO}} = 80.32^{+25.51(32\%)} \left( 76.98^{+24.30(32\%)} \right) \text{ ab}$$

$$\sigma_{\text{full off-shell}}^{\text{NLO}} = 98.88^{+1.22(1\%)} \left( 97.86^{+1.08(1\%)} \right) \text{ ab}$$

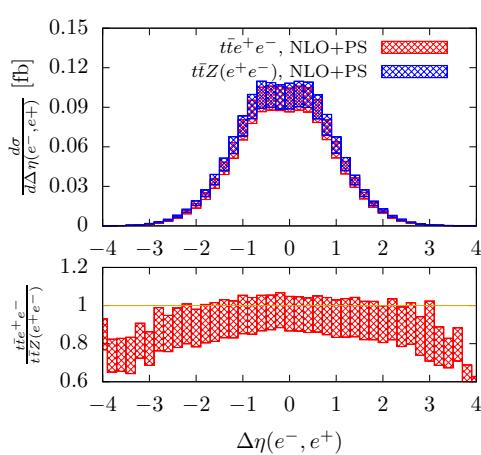
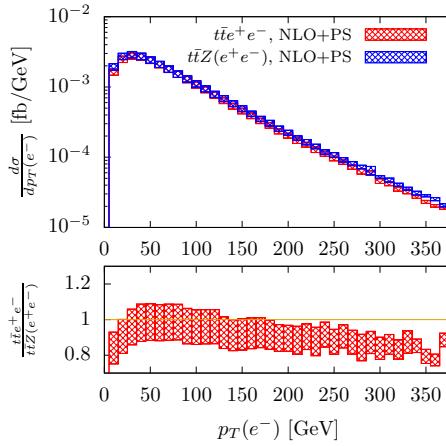
Dynamic scale preferred over full range of distributions.

Not a uniform rescaling.



Small dependence  
on PDF

# $pp \rightarrow t\bar{t}e^+e^-$ : partial off-shell and spin-correlation effects + PS



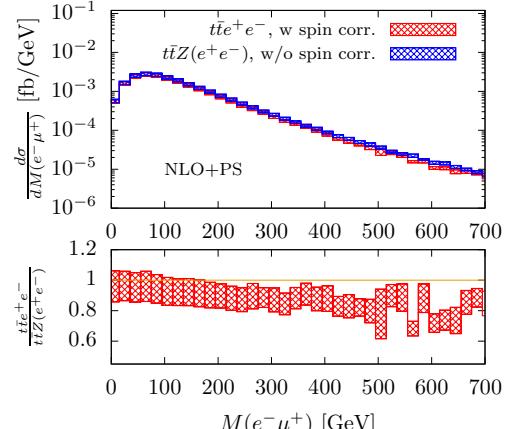
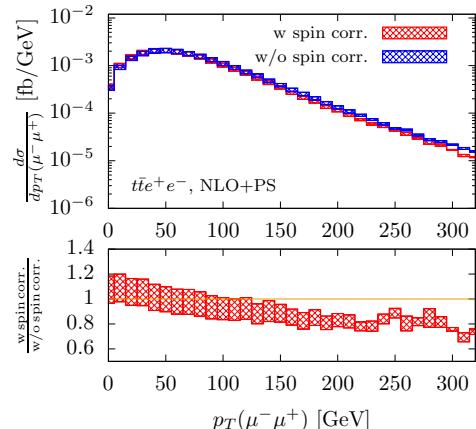
Compare  $t\bar{t}Z$  and  $t\bar{t}e^+e^-$   
keeping stable top quarks:

- Effects of off-shell Z
- Effects of  $e^+e^-$  spin correlations

10-20% effect in high  $p_T$  region and in  
the large absolute-value pseudorapidity  
difference region

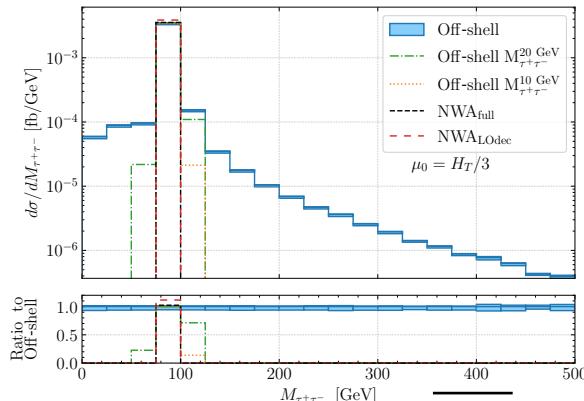
Compare  $t\bar{t}e^+e^-$  with and without  
modeling of top decays (NWA with  
LO spin correlations).

10-20% visible effects in the tails of  
distributions

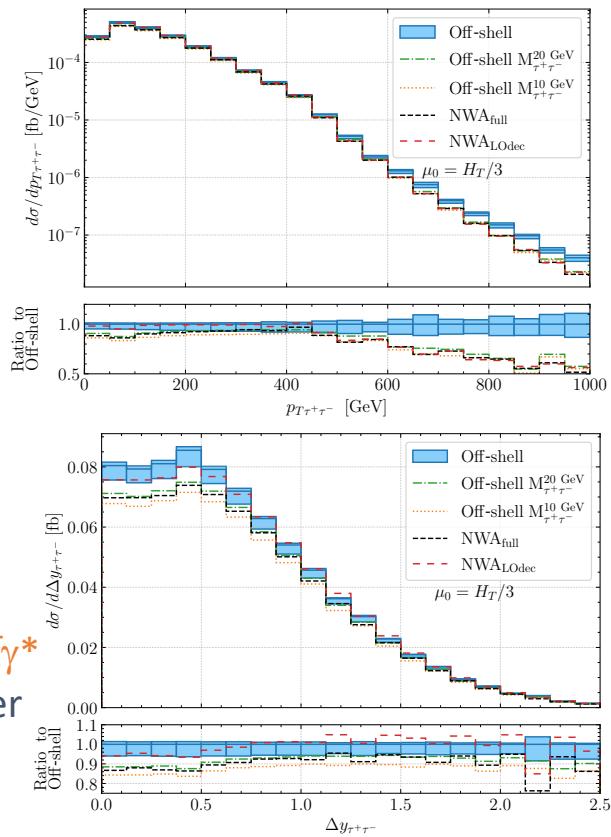


# $pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \tau^+ \tau^-$ : fully off-shell vs NWA

Very thorough study of modelling effects



MODELLING	$\sigma_i^{\text{NLO}} [\text{fb}]$	$\sigma_i^{\text{NLO}} / \sigma_{\text{NWAfull}}^{\text{NLO}} - 1$
Off-shell	98.88	+11.4 %
Off-shell $M_{\tau^+\tau^-}^{25 \text{ GeV}}$	91.00	+2.5 %
Off-shell $M_{\tau^+\tau^-}^{20 \text{ GeV}}$	89.96	+1.4 %
Off-shell $M_{\tau^+\tau^-}^{15 \text{ GeV}}$	88.44	-0.3 %
Off-shell $M_{\tau^+\tau^-}^{10 \text{ GeV}}$	85.74	-3.4 %
NWA <sub>full</sub>	88.75	-
NWA <sub>Lodec</sub>	96.74	+9.0 %



- Large off-shell effects on total cross section (11%) originating from  $t\bar{t}\gamma^*$  contribution (including  $Z/\gamma^*$  interference): studied imposing narrower  $|M_{\tau\tau} - m_Z| < X$  ( $X=25, 20, 15, 10 \text{ GeV}$ ) cut.  
Less evident in  $t\bar{t}l^+l^-$  study because it used  $X=10 \text{ GeV}$ .
- Large effect from including NLO QCD corrections to top-quark decay (9%)
- Sizable off-shell effects in specific fiducial regions of differential distributions even with narrow window cut around the  $Z$  peak.

# Conclusions

- Enabling the top-physics precision program of the (HL)-LHC is a priority since no other collider will reach the necessary energy to explore it for at least a few decades
- $t\bar{t}+X$  ( $X=W, Z, \gamma, H$ ) processes are challenging but uniquely capable of testing the presence of new physics (NP) effects in top-quark interactions.
  - They are interconnected and may need to be approached as a whole  
Aim for **global fits of classes of signatures**
  - NP that modifies top-quark interactions is most likely heavy → EFT approach  
**Effects most likely in tails or endpoint of kinematic distributions**
  - Off-shell and parton-shower effects can be large in this kinematic regions and need to be included.
- This talk has reviewed progress made with **two studies of off-shell effects** for the particular case of  $t\bar{t}Z$  production, including leptonic decays, PS, and partial or full off-shell effects, and confirmed the importance of **extending the modelling** of  $t\bar{t}Z$  events to include them.