$$\text{with} \qquad \delta_{ii} = -\Delta_i \sum_i \delta_{ij} = 0$$