$$\varphi_1 = \sqrt{\frac{2}{3}} \log(2)$$