# Form Factors For Bottom and Charm $\rightarrow$ Strange Semileptonic Decays

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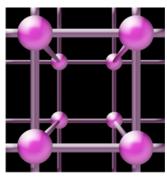


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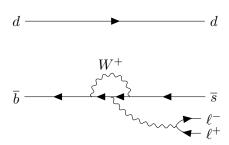
#### Overview

- ► Motivation
- ▶ Hadronic form factors for meson decays
- ► A brief introduction to Lattice QCD and heavy-HISQ
- ▶  $B \to K\ell^+\ell^-$  form factor calculation
- ▶ Preliminary  $B \to K\ell^+\ell^-$  and  $D \to K\ell\nu$  results





#### Motivation



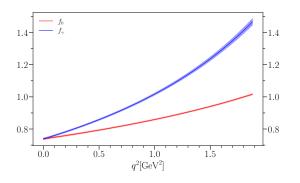
- ▶ Flavour changing weak decays of heavy mesons can test the SM
- ▶  $D \to K\ell\nu$  depends on CKM element:  $V_{cs}$
- ▶  $B \to K\ell^+\ell^-$  is a FCNC, proceeds via loop diagrams
- ▶ Both good places to look for new physics



#### Form factors

$$\frac{d\Gamma^{D o K}}{dq^2} = \frac{G_F^2 |V_{cs}|^2}{24\pi^3} |\vec{p}_K|^3 |f_+(q^2)|^2$$

- ▶ Parameterise the 'QCD bit' in decays rates etc.
- ▶ Describe the shape in  $q^2 = (p_{\text{parent}} p_{\text{daughter}})^2$  space





# Intro to LQCD

- ▶ Problem: QCD non-perturbative at low energies.
- Need to solve path integral. Discretise Euclidean action on a 4D lattice of space-time points with spacing a.
- ▶ Many discretisations of the action exist. We use a highly improved (HISQ) action which removes effects associated with the naive discretisation process through order  $a^2$ .
- ► For QCD we must integrate over quark and gluon fields.
- ▶ Calculate correlation functions by inserting operators and performing Monte Carlo integration. Repeat for many a values and extrapolate to continuum (a = 0).

$$\int \mathcal{D}\bar{\psi}\mathcal{D}\psi\mathcal{D}\overline{Ae^{-S[\bar{\psi},\psi,A]}}$$



# Intro to LQCD

We can calculate two and three point functions to study meson masses and decays from first principles, but with some limitations:

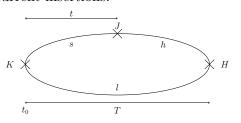
- ► The computational cost of calculations is very large. This grows quickly with lighter masses and finer lattices.
- ▶ Errors grow large with masses where  $am \gtrsim 0.8$ . This means to reach the b mass we must use very fine lattices where a is very small.

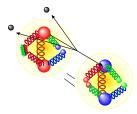
The solution is to study heavy mass behaviour. Work with several heavy masses  $m_c \leq m_h \leq m_b$  and then evaluate the result at the b mass: heavy-HISQ.



# Form Factors in heavy-HISQ

- $\triangleright$  Calculate meson form factors over the full range of  $q^2$  values.
- ▶ Interested in  $f_+(q^2)$ ,  $f_0(q^2)$  and  $f_T(q^2)$  form factors for pseudoscalar to pseudoscalar decays.
- ► Require three-point correlators with scalar, vector and tensor current insertions.







# Example: $B \to K$

- ▶ MILC HISQ 2+1+1 ensembles. All valence quarks HISQ
- ▶ 5 lattice spacings in range 0.15-0.045fm. Some with physical light quarks.
- ▶ Physical b is  $am_b \approx 0.9$  on finest lattice
- ► Choose several heavy masses and daughter momenta for each ensemble
- ► Combine heavy mass fit with continuum extrapolation
- ightharpoonup D o K comes 'for free'
- ▶ Cover whole physical  $q^2$  range



Perform standard z space fit:

standard 
$$z$$
 space fit:
$$f_{0}(q^{2}) = \frac{\log s}{1 - \frac{q^{2}}{M_{H_{s}^{0}}^{2}}} \sum_{n=0}^{N-1} a_{n}^{0} z^{n},$$

$$f_{+,T}(q^{2}) = \frac{\log s}{1 - \frac{q^{2}}{M_{H_{s}^{*}}^{2}}} \sum_{n=0}^{N-1} a_{n}^{+,T} \left(z^{n} - \frac{n}{N}(-1)^{n-N} z^{N}\right),$$

$$a_{n}^{0,+} = \left(1 + \rho_{n}^{0,+} \log\left(\frac{M_{H}}{M_{D}}\right)\right) \times$$

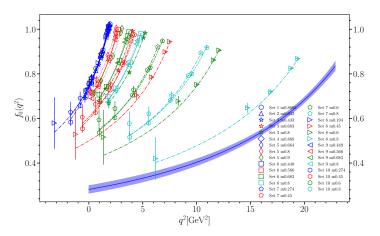
$$\sum_{i,j,k=0}^{N_{ijk}-1} d_{ijkn}^{0,+} \left(\frac{\Lambda_{QCD}}{M_{H}}\right)^{i} \left(\frac{am_{h}^{val}}{\pi}\right)^{2j} \left(\frac{a\Lambda_{QCD}}{\pi}\right)^{2k}$$

$$\times (1 + \mathcal{N}_{n}^{0,+}).$$

$$(1)$$

$$A_{QCD} = 0.5 \text{GeV}$$

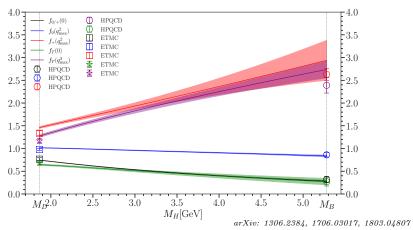
### $B \to K$ preliminary results



Continuum result at the b mass in blue. Heavy-HISQ allows us to evaluate at any mass from c to b.



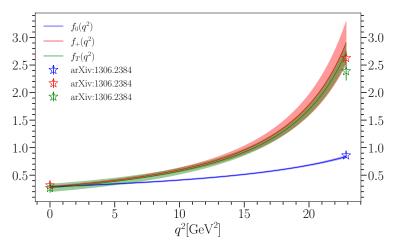
# $B \to K$ preliminary results



We can study behaviour with heavy mass.



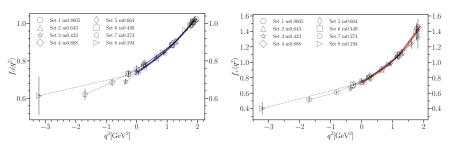
# $B \to K$ preliminary results



Tensor important for SM  $B \to K$  due to  $b \to s$  transition Normalisation with  $\mu = 2 \text{GeV}$ , matched to  $\overline{\text{MS}}$  at 3 loop at b mass



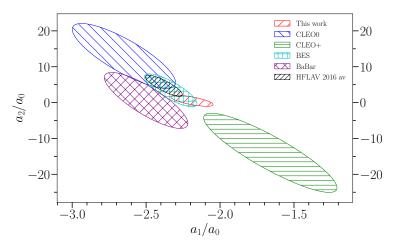
#### D o K preliminary results (B. Chakraborty,C. T. H. Davies)



- ▶ Charm mass easy to reach on ensembles
- ► Full  $q^2$  range  $\implies$  can compare bin by bin with exp. partial decay rate data
- ▶ Lots of good exp. data available, can compare shape

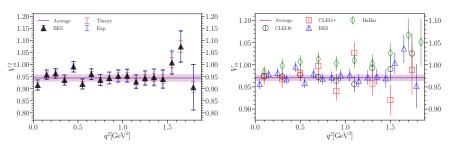


#### D o K preliminary results (B. Chakraborty,C. T. H. Davies)



One  $\sigma$  error ellipses. Ratios of  $f_+$  z expansion coefficients  $a_n$ , directly comparable with experiment.

#### $D \to K$ preliminary results (B. Chakraborty, C. T. H. Davies)



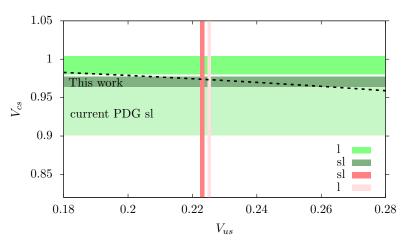
► Experimental error dominates each bin.

$$\Delta_i \Gamma = \int_{q_i^2}^{q_{i+1}^2} \frac{d\Gamma}{dq^2} dq^2 = \frac{G_F^2 |V_{cs}|^2}{24\pi^3} \int_{q_i^2}^{q_{i+1}^2} |\vec{p}_K|^3 |f_+(q^2)|^2 dq^2$$
 (3)



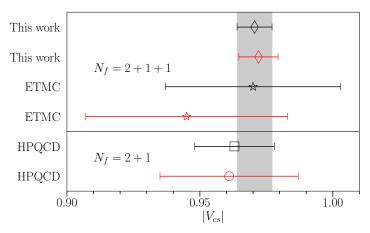
#### D o K preliminary results (B. Chakraborty, C. T. H. Davies)

Preliminary  $V_{cs} = 0.9706(66)[(54)_{th}(37)_{ex}]$ , big improvement on current PDG sl value of 0.939(38)





#### $D \to K$ preliminary results (B. Chakraborty, C. T. H. Davies)



 $f_{+}(0)|V_{cs}| = 0.7180(33)$ (HFLAV, arXiv:1612.07233)

arXiv: 1706.03657, 1305.1462, 1008.4562



#### Conclusions

- ▶ Heavy HISQ an effective method for studying heavy to strange decays and form factors
- ▶ Can improve upon  $B \to K\ell^+\ell^-$  and  $D \to K\ell\nu$  results
- ▶ Improvement on  $V_{cs}$  determination from  $D \to K \ell \nu$  using bin by bin comparisons with experiment

Thanks for listening. Any questions?



#### Extra Slides

$$Z_{V} \langle K | V^{0} | \hat{H} \rangle =$$

$$f_{+}(q^{2}) \left( p_{H}^{0} + p_{K}^{0} - \frac{M_{H}^{2} - M_{K}^{2}}{q^{2}} q^{0} \right)$$

$$+ f_{0}(q^{2}) \frac{M_{H}^{2} - M_{K}^{2}}{q^{2}} q^{0},$$

$$(4)$$

$$\langle K|S|H\rangle = \frac{M_H^2 - M_K^2}{m_h - m_s} f_0(q^2),$$
 (5)

$$Z_T \langle \hat{K} | T^{i0} | \hat{H} \rangle = \frac{2iM_H p_K^i}{M_H + M_K} f_T(q^2), \tag{6}$$



#### Extra Slides

$$z(q^2) = \frac{\sqrt{t_+ - q^2} - \sqrt{t_+ - t_0}}{\sqrt{t_+ - q^2} + \sqrt{t_+ - t_0}}$$
 (7)

$$\frac{m_l}{m_s} \approx \frac{M_\pi^2}{M_{\eta_s}^2} \tag{8}$$

