

Closing in on t -channel simplified dark matter models

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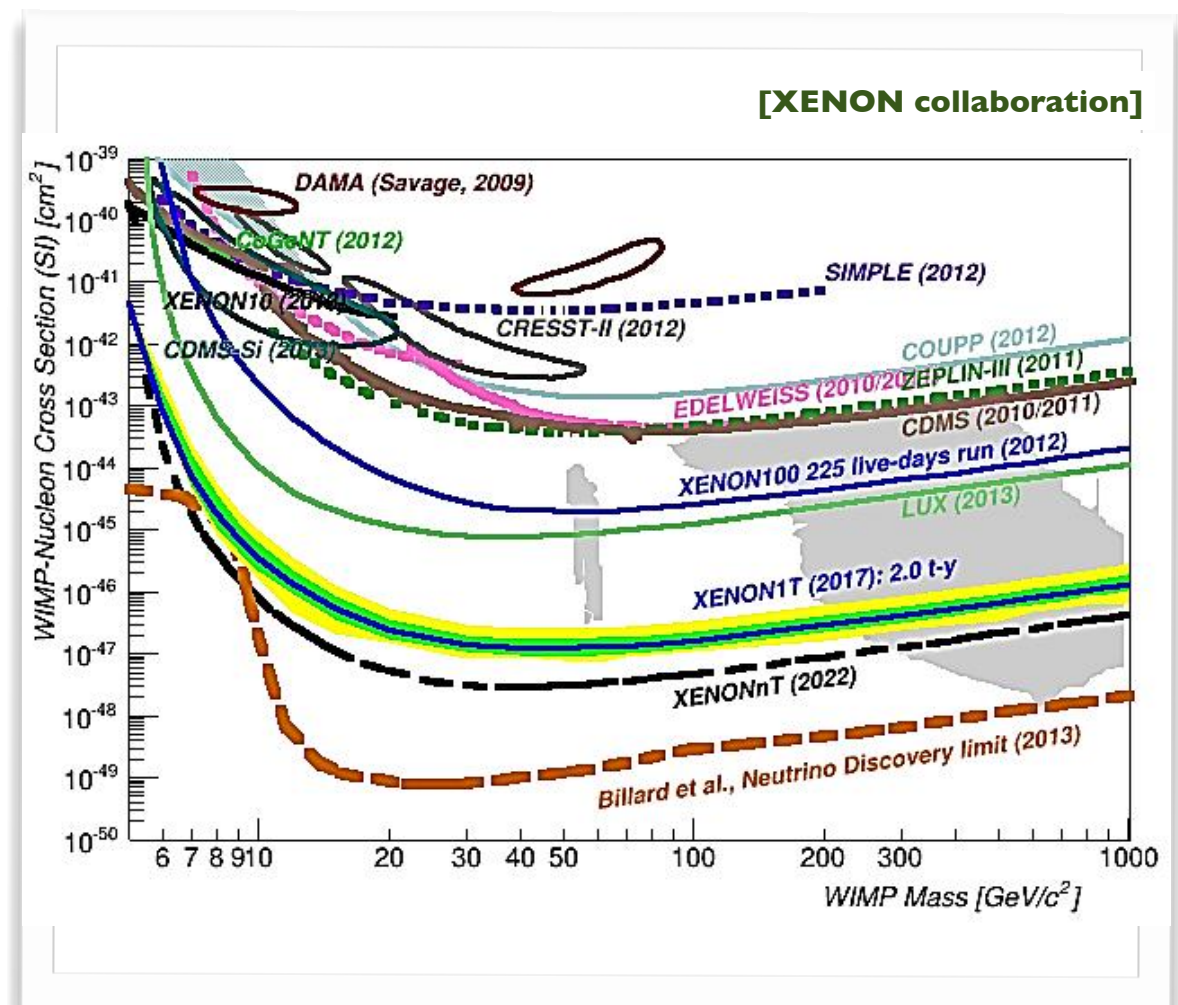
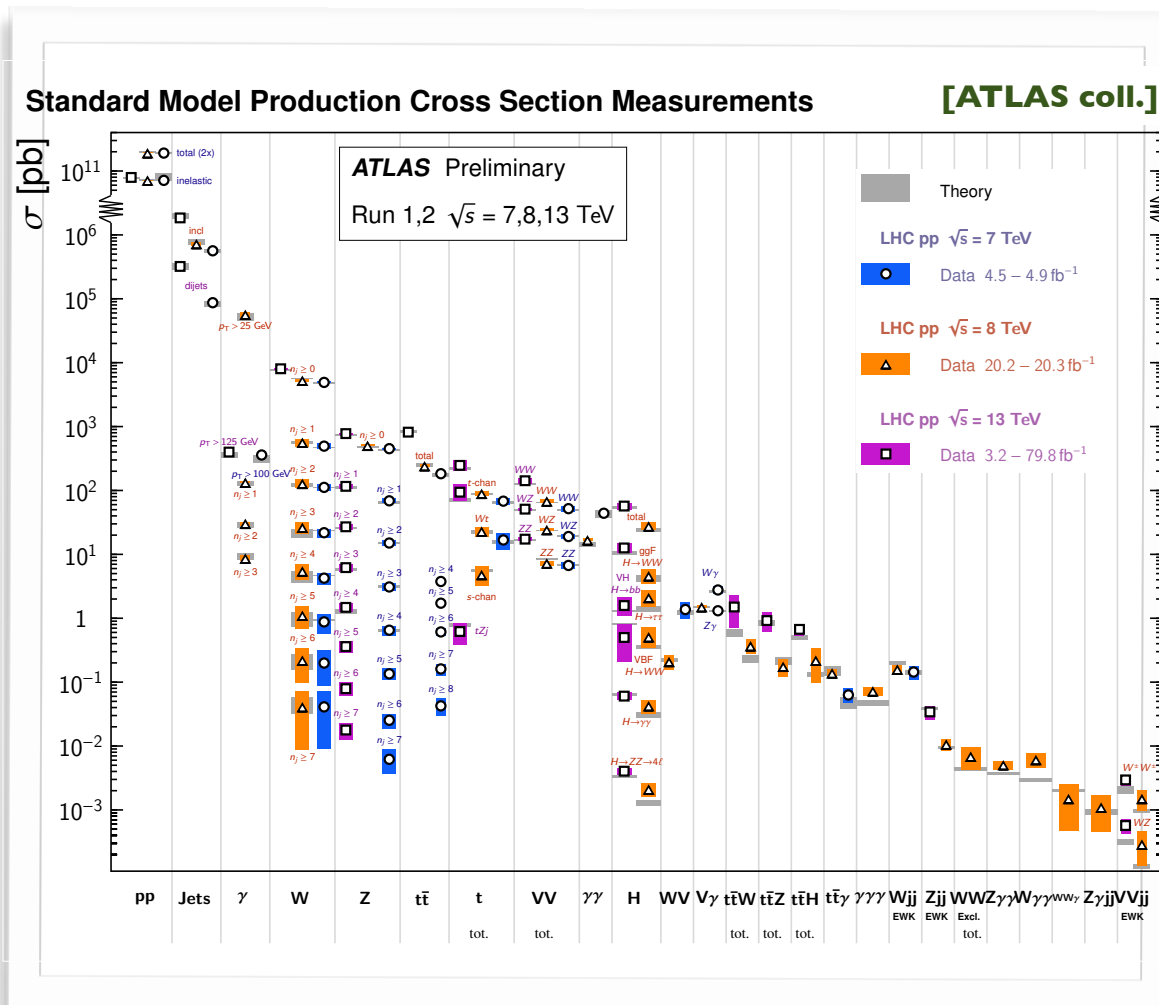
Outline

1. Introduction
2. A simplified model for t -channel dark matter
3. Dark matter at colliders: generalities, signals and re-interpretations
4. Cosmological constraints and their complementarity
5. Summary - conclusions

New physics searches in 2020

◆ Theoretically, we are in the dark

- ♣ No sign of new physics, measurements compatible with the SM
 - intriguing features need confirmation
- ♣ No leading new physics candidate theory
 - crucial: no loophole in new physics explorations

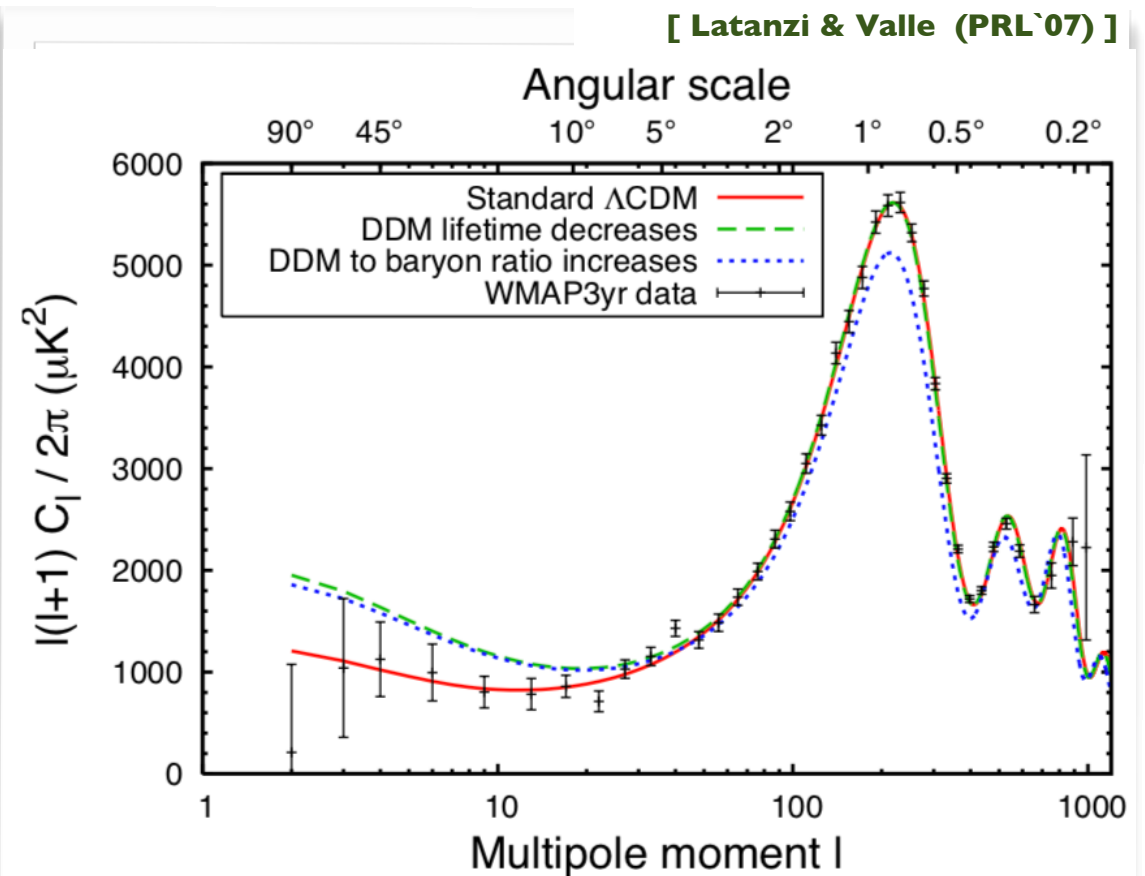
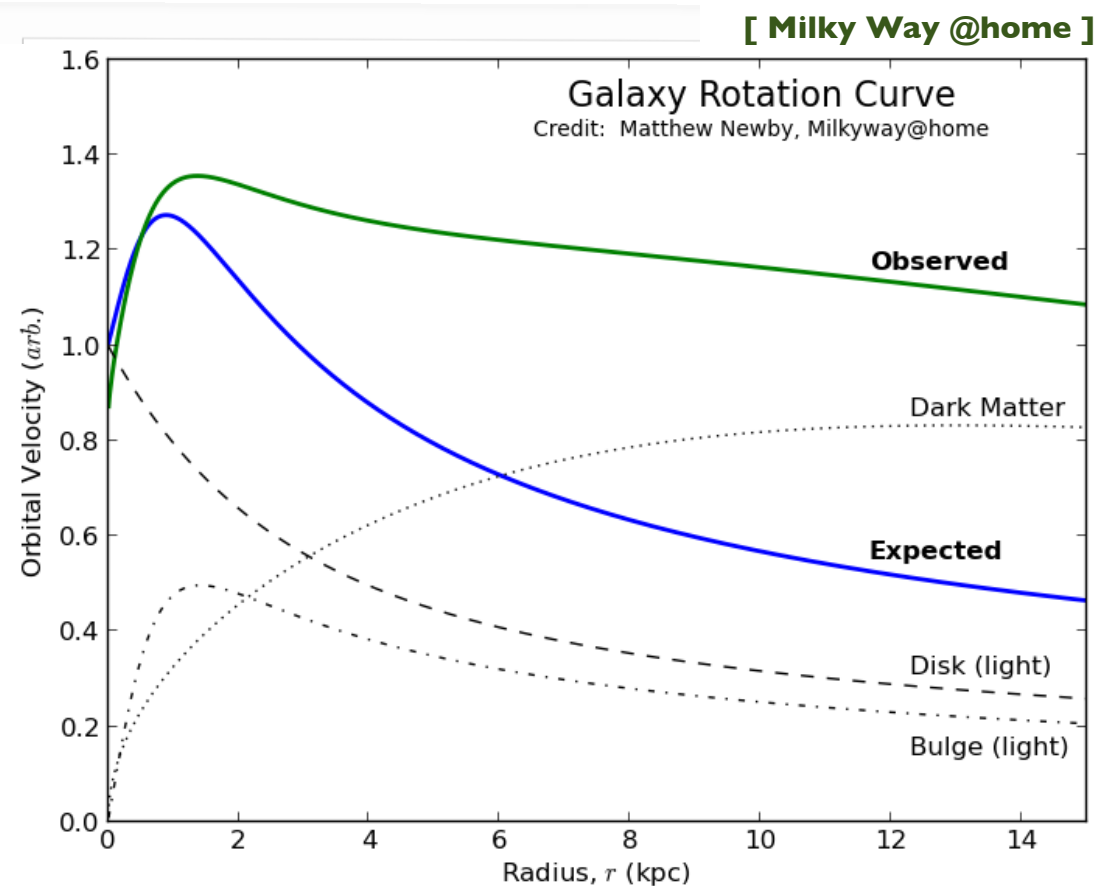


New physics and dark matter

♦ Dark matter is an important motivation for new physics

- ♣ Flattening of the galaxy rotation curves
- ♣ Gravitational lensing
- ♣ Cosmic microwave background
- ♣ Structure formation

Enormous endeavour to detect dark matter



Dark matter in cosmology and at colliders

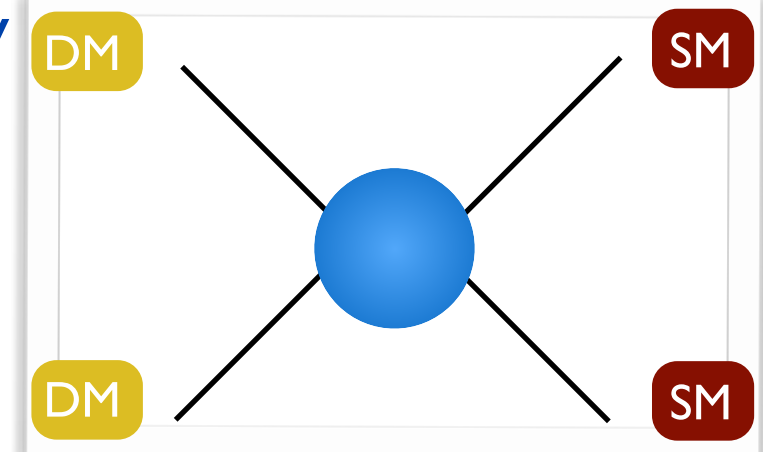
- ♦ Dark matter is searched for directly, indirectly and at colliders
 - ♣ This huge experimental effort offers a **strategy to constrain models**

- ♦ **Complementary between colliders and cosmology**

- ♣ Dark matter relic abundance must be reproduced
- ♣ Dark matter direct/indirect detection constraints
- ♣ Direct production at colliders

- ♦ **One important issue: precision**

- ♣ Do QCD corrections matter?
- ♣ Can QCD corrections change conclusions?
- ♣ Especially relevant if DM interacts with quarks and gluons



Dark matter simplified models

[Arina, BF & Mantani (EPJC'20)]

Simplified dark matter models @ LHC

♦ Generic simplified models for dark matter @ LHC

♣ Minimality: SM + 1 DM candidate + 1 mediator (coupling to quarks and gluons)

- ★ Representative of different theoretically-motivated new physics scenarios
- ★ Lack non-minimal features (multiple mediators, multi-component DM, etc.)
- ★ Can change the picture presented in this talk

♦ Properties

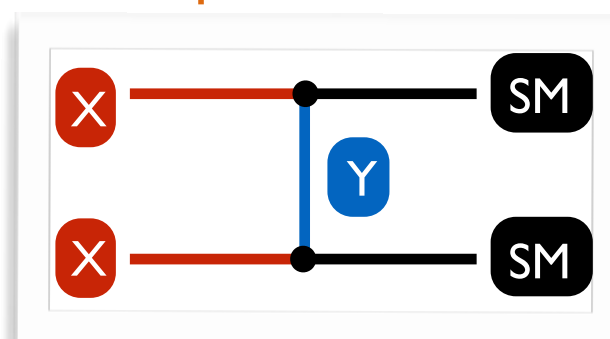
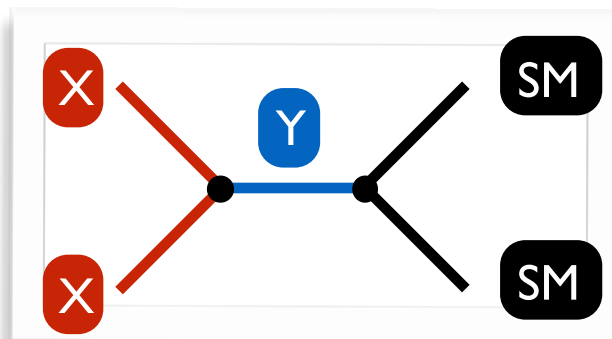
♣ DM (X) is stable

- Odd under some $\mathbb{Z}_2$ discrete symmetry
- SM states even

♣ The mediator (Y) connects DM and quarks/gluons

- ★ $\mathbb{Z}_2$ -even: s-channel models → colour singlet and electrically neutral
- ★ $\mathbb{Z}_2$ -odd: t-channel models → colour triplet and electrically charged

Topic of this talk



A comprehensive approach to new physics simulations

[Christensen, de Aquino, Degrande, Duhr, BF, Herquet, Maltoni & Schumann (EPJC'11)]

Idea / Lagrangian



FEYNRULES / UFO



Matrix
Elements



Observables



Phenomenology

◆ Model building: from Lagrangian to tools

- ❖ FEYNRULES $\oplus$ MoGRE $\oplus$ NLOCT $\rightarrow$ UFO @ NLO
- ❖ General on-shell renormalisation scheme

[Alloul, Christensen, Degrande, Duhr & BF (CPC'14) ; Degrande (CPC'15)]

[Degrande, Duhr, BF, Mattelaer & Reither (CPC'12)]

[Frixione, BF, Hirschi, Mawatari, Shao, Sunder & Zaro (JHEP'19)]

◆ Hard scattering

- ❖ LO/NLO Feynman diagram, matrix elements
- ❖ MG5aMC/MadDM $\rightarrow$ cosmology/colliders at LO/NLO

[Alwall et al. (JHEP'14)]

[Ambrogi et al. (PDU'19)]

◆ BSM phenomenology @ colliders with MG5_aMC

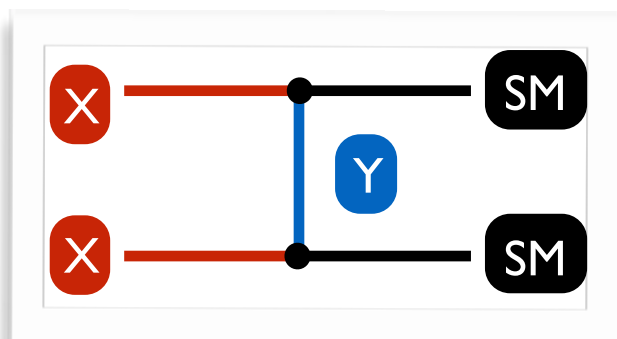
- ❖ Matching matrix elements with parton showers
- ❖ Simplified treatment of the resonances (MADSTR)

[Alwall et al. (JHEP'14)]

[Frixione, BF, Hirschi, Mawatari, Shao, Sunder & Zaro (JHEP'19)]

A generic t -channel DM

♦ A generic t -channel DM model



Many parameters / spin combination
 $\rightarrow$ simplifications/restrictions

♣ 2 spins: J_X, J_Y

♣ 13 masses:

★ 1 DM mass: m_X

★ 12 mediator masses ($SM = u_L, d_L, u_R, d_R$)

♣ 9 couplings (with $SU(2)_L \times U(1)_Y$ invariance)

★ 3 vectors in flavour space

★ $SM = Q_L, u_R, d_R$

♦ Spin options

X (DM)	Spin	Self-conj.	Y (med.)	Spin
$\tilde{S}$	0	yes	ψ_Q, ψ_u, ψ_d	1/2
S	0	no		
$\tilde{\chi}$	1/2	yes	$\varphi_Q, \varphi_u, \varphi_d$	0
χ	1/2	no		
$\tilde{V}_\mu$	1	yes	ψ_Q, ψ_u, ψ_d	1/2
V_μ	1	no		

♣ Dark matter

★ Spin 0, 1/2 and 1

★ Majorana or not

♣ 12 mediators

★ Spin 0 or 1/2 (no spin 1)

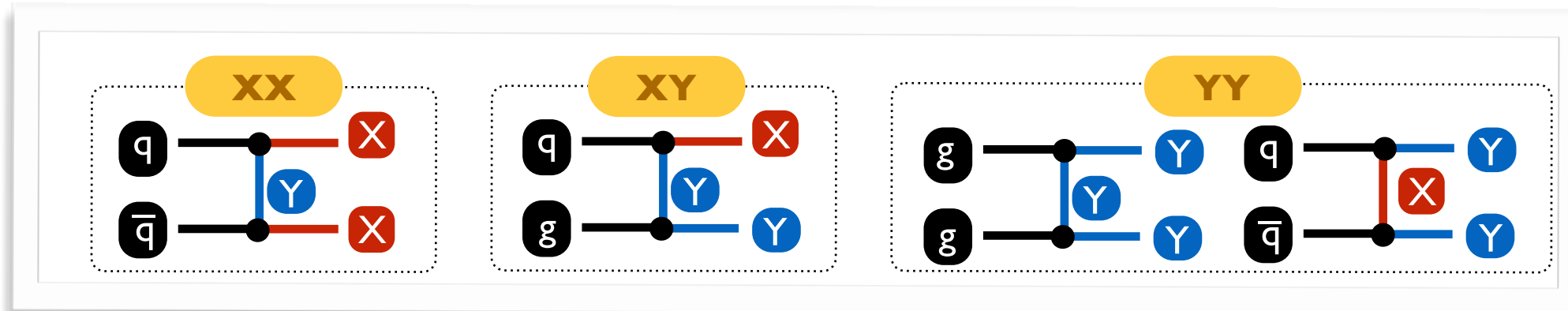
★ Independent couplings to all gauge eigenstates

Dark matter at colliders

Generalities (no top)

DM @ colliders: light generation mediators

♦ Three classes of processes $\rightarrow$ jets generated from radiation or mediator decays



❖ **Signal less naive than considering XX production only**

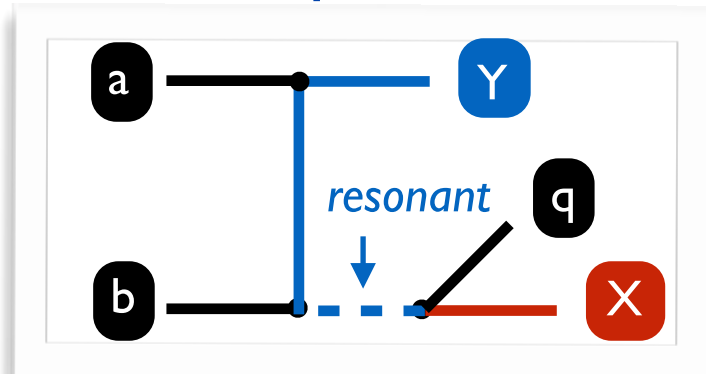
- ★ DM pair production
- ★ DM/mediator associated production (with mediator decays into DM+jet)
- ★ Mediator pair production (with mediator decays into DM+jet)

❖ **Mediator pair-production: t -channel and QCD contributions**

- ★ Model-dependent relative dominance $\rightarrow$ couplings, masses
- ★ Mixed order situation $\rightarrow$ to be simulated separately with MG5_aMC
- ★ Interference issue $\rightarrow$ re-weighted LO simulations

Resonance subtraction: generalities

◆ NLO computations are not trivial



♣ Overlap

- ★ $YY @ LO \otimes Y \rightarrow Xq$ decay
- ★ $YX @ NLO$ (real emission)

♣ Possible (huge) enhancement w.r.t. LO (if YY dominates over XY)

- ★ **Spoiling the perturbative expansion for the original process**

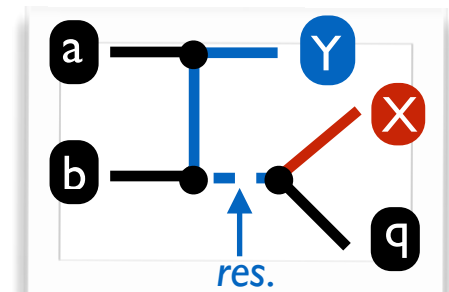
♣ All three subprocesses need to be considered separately to avoid double counting

- ★ **Resonances must be subtracted**

Resonance treatment in practice

[Frixione, BF, Hirschi, Mawatari, Shao, Sunder & Zaro (JHEP`19)]

Matrix element: resonant and non-resonant pieces



$$|\mathcal{A}|^2 = |\mathcal{A}^{(\text{non-res.})}|^2 + 2\Re\left(\mathcal{A}^{(\text{non-res.})}\mathcal{A}^{(\text{res.})\dagger}\right) + |\mathcal{A}^{(\text{res.})}|^2$$

Diagram removal

$$|\mathcal{A}|^2 = |\mathcal{A}^{(\text{non-res.})}|^2 + \cancel{2\Re\left(\mathcal{A}^{(\text{non-res.})}\mathcal{A}^{(\text{res.})\dagger}\right)} + \cancel{|\mathcal{A}^{(\text{res.})}|^2}$$

- ❖ DR: removal of the resonant diagrams
- ❖ DR+I: interferences are kept [our choice]

Projection of the kinematics on the resonance

$$|\mathcal{A}^{(\text{res.})}|^2 d\Phi \Rightarrow |\mathcal{A}^{(\text{res.})}|^2 d\Phi - f(m^2) \mathbb{P}\left(|\mathcal{A}^{(\text{res.})}|^2 d\Phi\right) \quad \star t\text{-channel example: } m = m_{Xq} \sim m_Y$$

❖ The projector operator $\mathbb{P}$

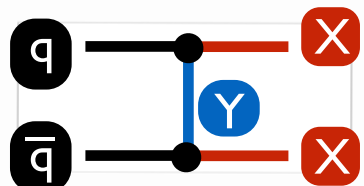
★ From an n -body kinematics to an $(n-1) \otimes (1 \rightarrow 2)$ kinematics

$$|\mathcal{A}^{(\text{res.})}(ab \rightarrow XYq)|^2 = |\mathcal{A}(ab \rightarrow YY)|^2 \otimes |\mathcal{A}(Y \rightarrow Xq)|^2$$

- ❖ The pre-factor f is arbitrary (tends to 1 in the resonant limit)
- ❖ DS: Initial-state or final-state reshuffling

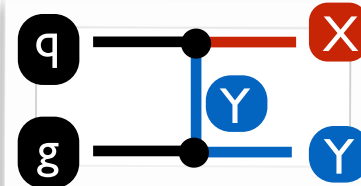
A fivefold signal event generation procedure

XX @ NLO



- ★ Jet activity $\rightarrow$ QCD radiation
- ★ Resonance: XY prod. + decay

XY @ NLO



- ★ Jet activity $\rightarrow$ QCD radiation
 $\rightarrow$ mediator decay
- ★ Resonances: YY/XX prod. + decay (benchmark dependent)

YY @ NLO



- ★ Jet activity $\rightarrow$ QCD radiation and mediator decay
- ★ Resonance: YX production + (off-shell) decay
- ★ 2 interfering channels (from qqbar initial states)

Dark matter at colliders

NLO vs LO simulations

[Arina, BF & Mantani (EPJC'20)]

1st gen. mediator & Dirac DM

◆ Dirac DM coupling to the right-handed up quark

X (DM)	Spin	Self-conj.	Y (med.)	Spin
χ	1/2	no	φ_{u_1}	0

$$\mathcal{L}_{X-uR}(X) = \left[\lambda_\varphi \bar{X} u_1 \varphi_{u_1}^\dagger + \text{h.c.} \right]$$

- ♣ Benchmark BM1: $m_\chi = 150 \text{ GeV}$, $m_Y = 500 \text{ GeV}$, $\lambda=1$
- ♣ Benchmark BM2: $m_\chi = 150 \text{ GeV}$, $m_Y = 1000 \text{ GeV}$, $\lambda=1$
- ♣ Largish DM-mediator coupling

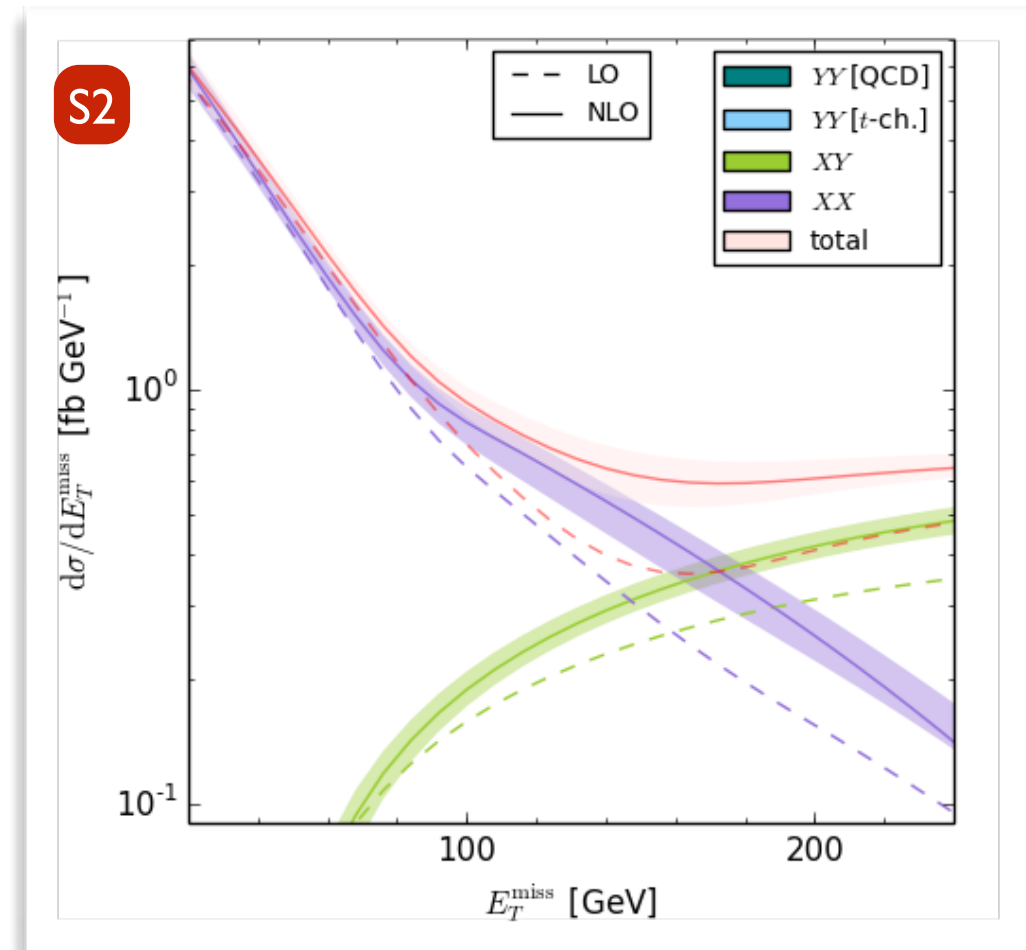
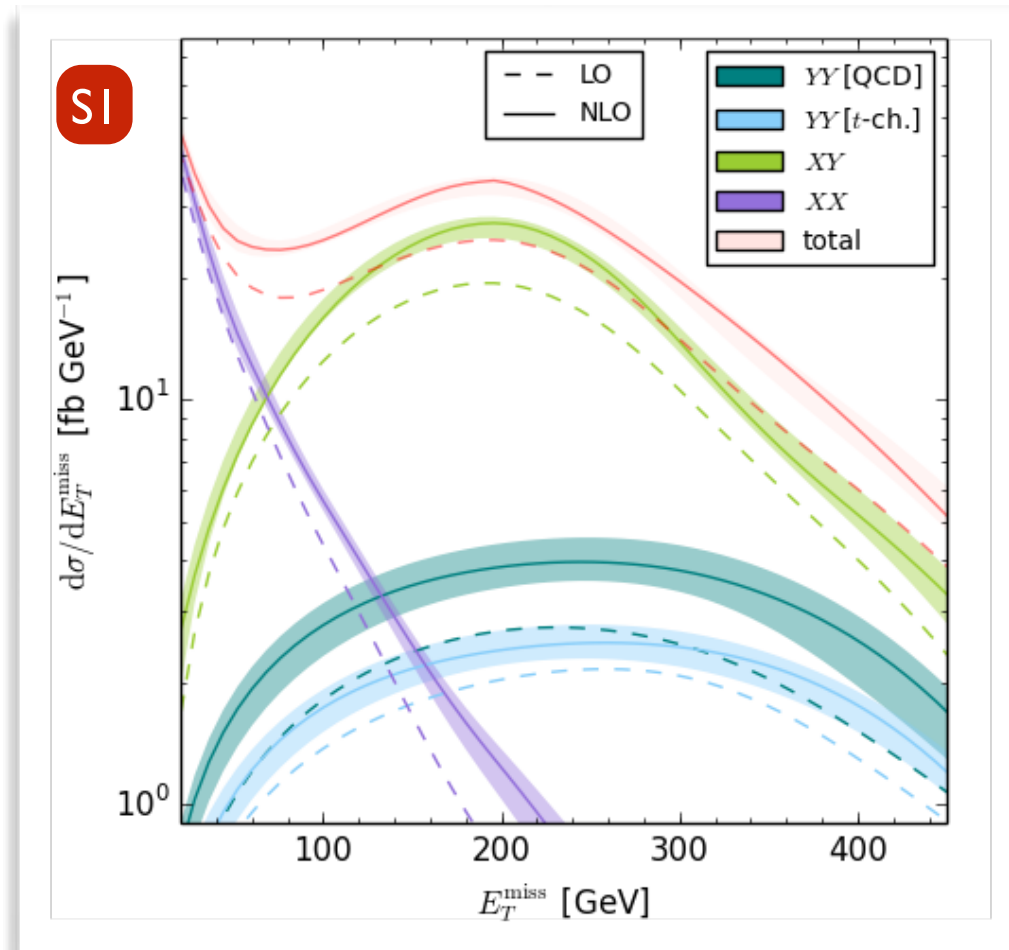
◆ Total rates

Scen.	XX [fb]	XY [fb]	YY (total) [fb]	YY (QCD) [fb]	YY (t-channel) [fb]
LO S1	$775.3^{+0.4\%}_{-0.8\%} \pm 1.9\%$	$1617^{+16.5\%}_{-13.4\%} \pm 1.0\%$	$473.5^{+23.6\%}_{-16.9\%} \pm 3.0\%$	$324.2^{+34.2\%}_{-23.8\%} \pm 3.4\%$	$261.5^{+7.1\%}_{-6.3\%} \pm 2.5\%$
S2	$122.0^{+1.8\%}_{-2.0\%} \pm 1.9\%$	$74.1^{+20.3\%}_{-15.8\%} \pm 1.2\%$	$7.452^{+19.8\%}_{-14.5\%} \pm 5.6\%$	$3.545^{+37.3\%}_{-25.4\%} \pm 7.2\%$	$6.939^{+11.1\%}_{-9.4\%} \pm 5.0\%$
NLO S1	$929.8^{+1.9\%}_{-1.3\%} \pm 1.9\%$	$2212^{+5.9\%}_{-6.3\%} \pm 1.0\%$	$648.4^{+8.0\%}_{-9.2\%} \pm 3.1\%$	$484.7^{+10.7\%}_{-12.4\%} \pm 3.4\%$	$314.1^{+2.6\%}_{-2.6\%} \pm 2.5\%$
S2	$139.1^{+1.3\%}_{-1.1\%} \pm 2.0\%$	$101.8^{+6.0\%}_{-7.1\%} \pm 1.2\%$	$9.888^{+6.5\%}_{-7.6\%} \pm 5.8\%$	$5.303^{+11.2\%}_{-13.3\%} \pm 7.4\%$	$8.749^{+3.6\%}_{-3.9\%} \pm 4.9\%$

- ♣ Large XX and XY contributions
 - could be a significant component of the signal
- ♣ YY is smaller
 - ★ QCD and t-channel diagrams both important
 - ★ Large destructive interferences
- ♣ Large K-factors
 - NLO rates matter
- ♣ Reduction of the TH errors
 - to a few percents
- ♣ Smaller λ
 - YY-QCD always remains

Differential distributions: missing energy

◆ Properties of the signal at the LHC



- ❖ XX: large cross section and only contributes for small MET
→ irrelevant for the signal (preselection requires large MET)
- ❖ XY dominates in the intermediate MET regime
- ❖ YY kicks in at intermediate MET (sub-dominant)
★ QCD and t -channel diagrams both important (different shapes)

Recasting ATLAS SUSY 2016-27 (monojet; 36/fb)

◆ CLs exclusion from the best region

S2	Process	CL _s [LO]	E_T^{miss} constraint	CL _s [NLO]	E_T^{miss} constraint
	Total	$75.6^{+10.1}_{-10.5} \%$	$\in [700, 800] \text{ GeV}$	$97.8^{+0.9}_{-1.4} \%$	$\geq 700 \text{ GeV}$
	XX	$0.7^{+0.6}_{-0.6} \%$	$\in [250, 300] \text{ GeV}$	$3.6^{+0.3}_{-0.6} \%$	$\geq 900 \text{ GeV}$
	XY	$62.7^{+12.3}_{-10.4} \%$	$\in [500, 600] \text{ GeV}$	$83.9^{+2.9}_{-4.3} \%$	$\in [700, 800] \text{ GeV}$
	YY [total]	$24.0^{+3.1}_{-3.1} \%$	$\geq 900 \text{ GeV}$	$58.1^{+2.2}_{-3.1} \%$	$\geq 900 \text{ GeV}$
	YY [QCD]	$10.7^{+4.4}_{-2.6} \%$	$\geq 900 \text{ GeV}$	$17.0^{+2.1}_{-2.1} \%$	$\geq 900 \text{ GeV}$
	YY [<i>t</i> -channel]	$29.6^{+3.3}_{-2.6} \%$	$\geq 900 \text{ GeV}$	$38.9^{+1.2}_{-1.8} \%$	$\geq 900 \text{ GeV}$

[MADANALYSIS 5]

- ❖ **NLO** simulations are crucial
 - ★ Modification of the rates (larger yields) and shapes (different best region)
 - ★ Better control of the theory errors
- ❖ Considering **all signal components** is crucial
 - ★ One component alone is not sufficient to exclude the scenario

◆ SI (lighter mediator) is excluded (from YX, YY and the total)

Benchmarking
Fixing λ or Γ_Y

[Arina, BF, Mantani, Mies, Panizzi & Salko (2020)]

1st gen. mediator & Majorana DM

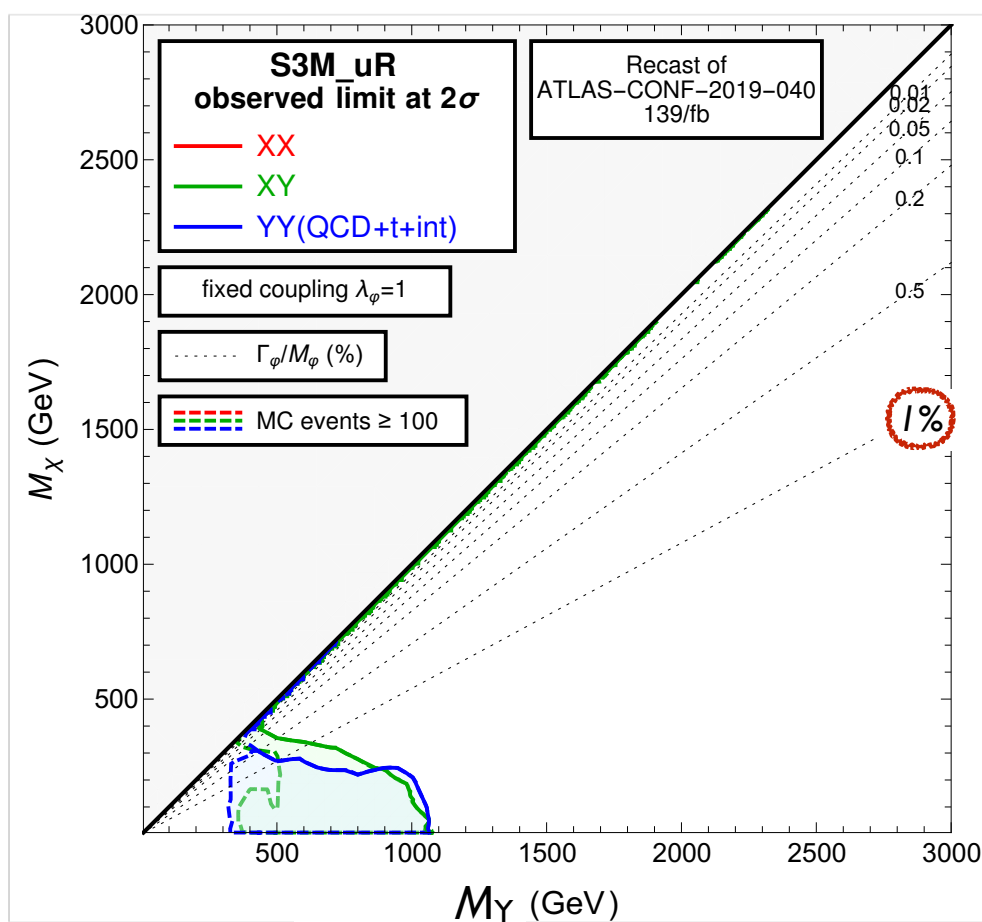
♦ Majorana DM coupling to the right-handed up quark

X (DM)	Spin	Self-conj.	Y (med.)	Spin
$\tilde{\chi}$	1/2	yes	φ_{u_1}	0

$$\mathcal{L}_{X-uR}(X) = \left[\lambda_{\varphi} \bar{X} u_1 \varphi_{u_1}^{\dagger} + \text{h.c.} \right]$$

♣ Masses free

♣ Still a fixed $\lambda = 1$ coupling (typical of s-channel DM literature)



♦ Recast: ATLAS multijet + MET search

♣ 139/fb

♣ Monojet-like and multijet + MET regions

♦ Signal component complementarity

♣ DM production is irrelevant

♣ YY and XY production: comparable reach

→ M_Y below 1 TeV

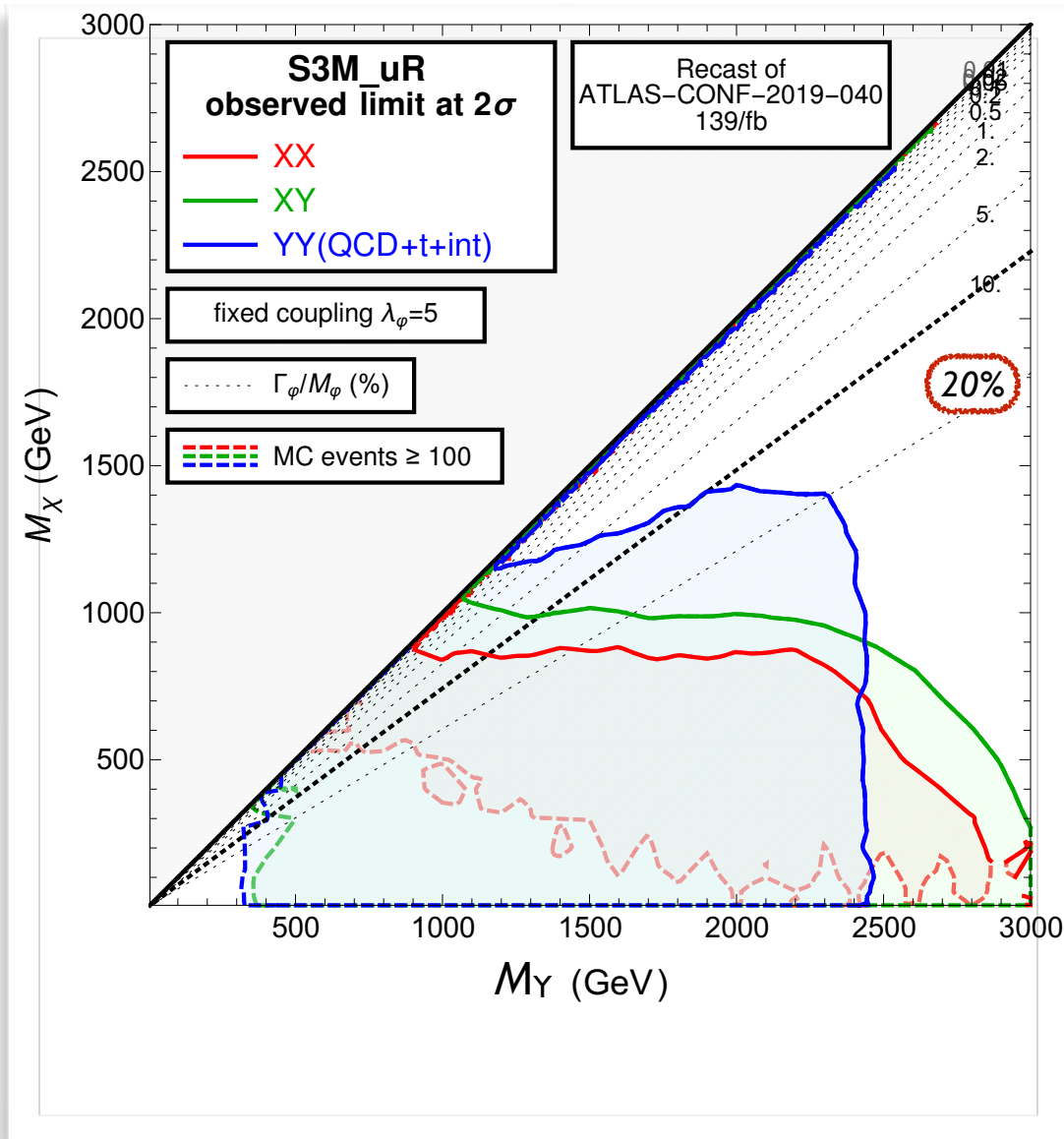
→ M_X below few hundred GeV

→ Mild coverage of the parameter space

♣ The width of the mediator can play a role

→ especially for larger λ values

More strongly coupled dark matter



◆ $\lambda = 5$

♣ All channels contribute (larger rates)

★ $XX \sim \lambda^4$

★ $XY \sim \lambda^2$

★ $YY \sim \lambda^4 + \lambda^2 + \lambda^0$

♣ Simulations unreliable

★ The NWA breaks down

★ $\Gamma_Y/M_Y > 10\%$ or compressed spectrum

★ Most 'excluded' points inconclusive

♣ Γ_Y plays a role for large λ values

◆ Sensitivity to all channels

♣ Different jetty properties

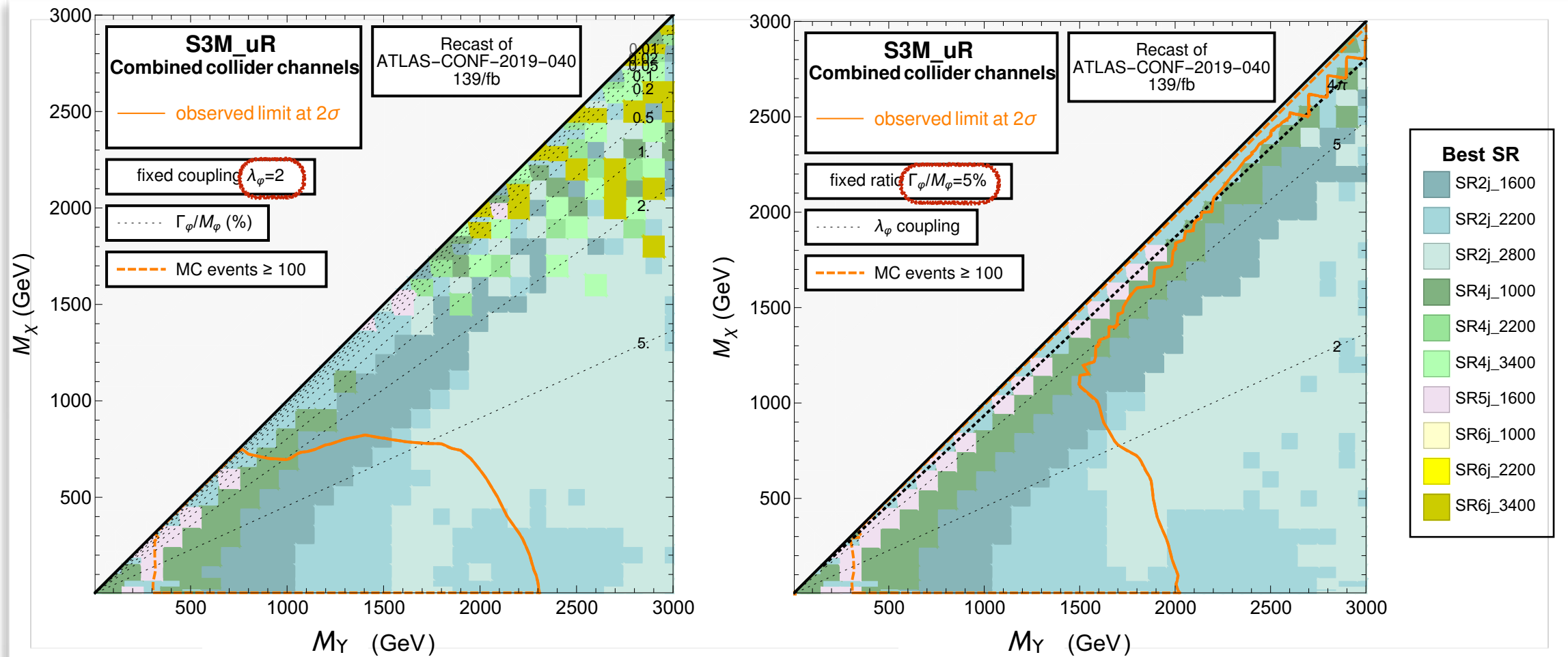
→ XX: small N_j , mostly soft jets

→ XY: medium N_j , hard and softer jets

→ YY: large N_j , hard jets

♣ Dedicated regions for all cases

Fixed coupling vs fixed width



◆ $\lambda = 2$ vs $\Gamma_Y/M_Y = 5\%$

♣ Signal $\equiv XX + XY + YY$

♣ Regions with 2 very hard jets (SR2j) $\rightarrow YY$ production and decay

♣ Regions with more not so hard jets (SR4j, SR5j, SR6j) $\rightarrow$ compressed regime

♣ **Reliability of the simulations**

★ Fixed Γ_Y/M_Y : compressed spectrum $\equiv$ non-perturbative regime

★ Fixed λ : split spectrum $\equiv$ broad mediator

Cosmological constraints

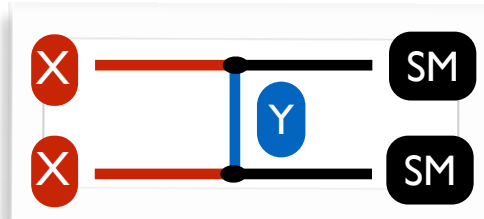
LO vs NLO

[Colucci, BF, Giacchino, Lopez Honorez, Tytgat & Vandecasteele (PRD`18)]

t -channel DM annihilations @ NLO

◆ Many competing channels opening up at NLO

♣ Tree-level annihilations



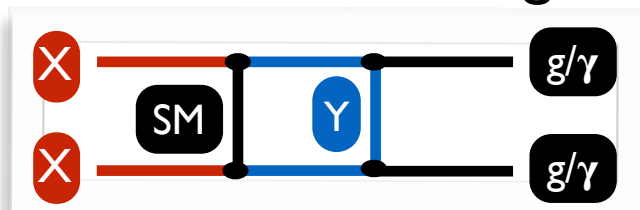
★ Scalar DM: d -wave suppressed

★ Majorana DM: p -wave suppressed

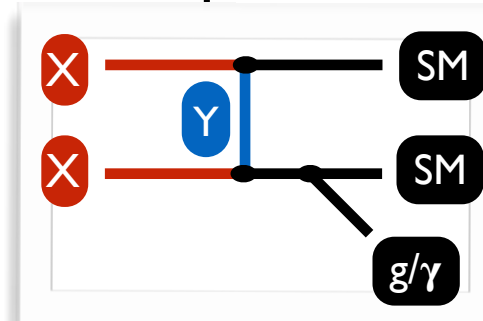
→ NLO corrections can be crucial

♣ At $O(\alpha_s)$

★ Annihilations into gluons/photons



★ Gluon/photon emission



→ Role of VIB

♣ Co-annihilations may matter (XY and YY)

◆ Scalar DM coupling to the right-handed top quark

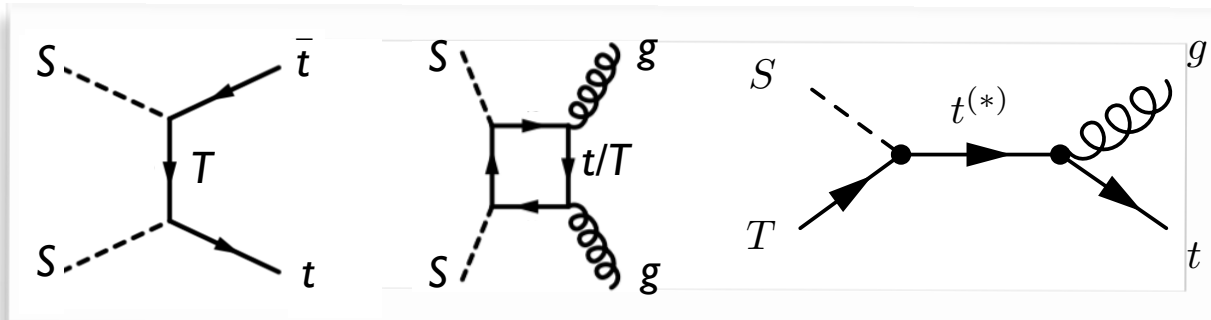
X (DM)	Spin	Self-conj.	Y (med.)	Spin	$\mathcal{L} = \left[\tilde{y}_t S \bar{T} P_R t + \text{h.c.} \right]$
S	0	yes	T	1/2	

♣ Masses and coupling free

Relic abundance: generalities

◆ Several competing annihilation channels

- ★ Into (potentially virtual) tops
- ★ Into gluons (loop-induced)
- ★ $ST \rightarrow t^{(*)}$ co-annihilations (potentially resonant)



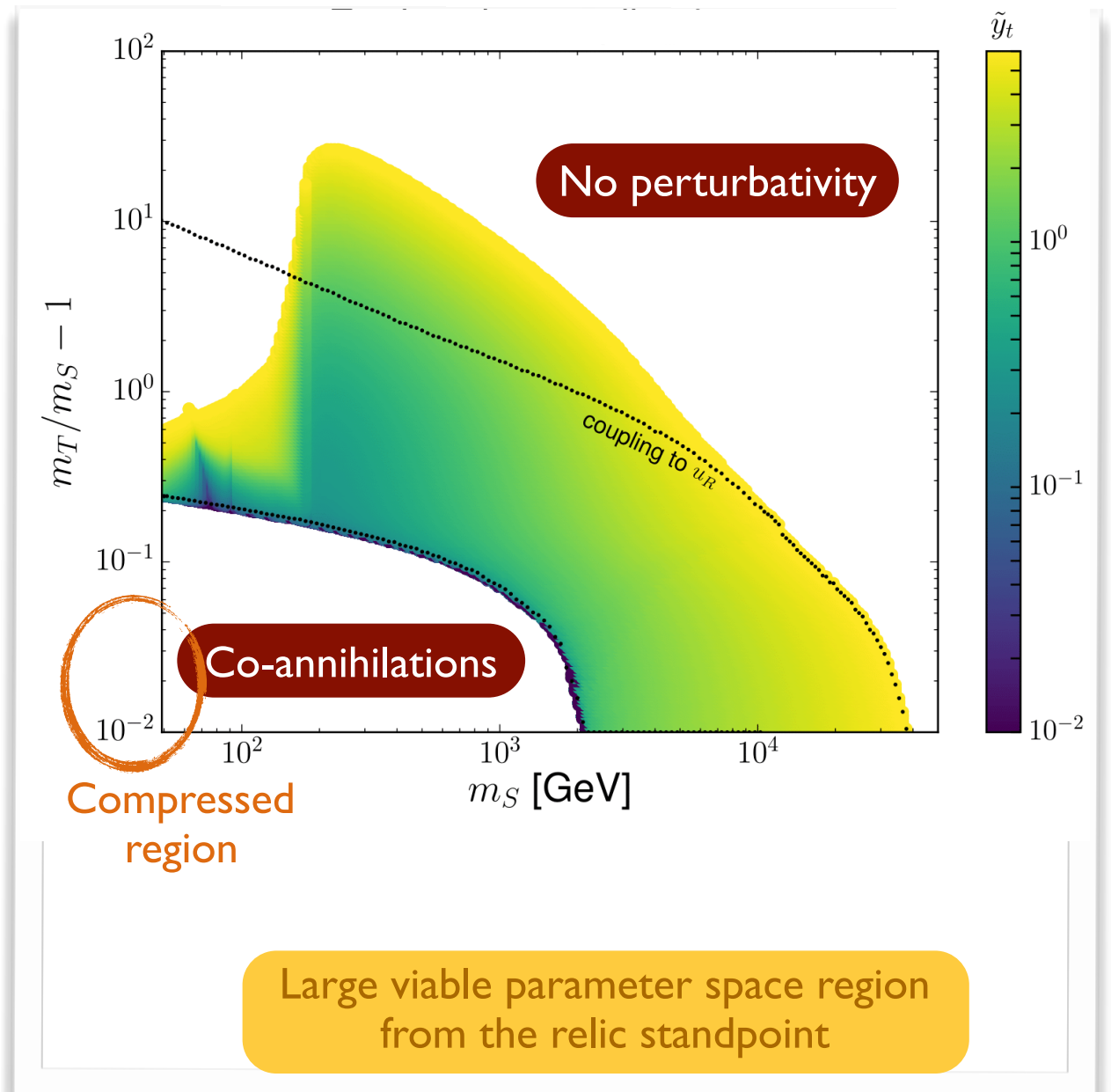
❖ Coloured point $\equiv$ viable scenario

$$\Omega_{\text{DM}} h^2 = 0.12 \quad [\text{Planck Collaboration (AA'20)}]$$

- ★ NLO QCD corrections included

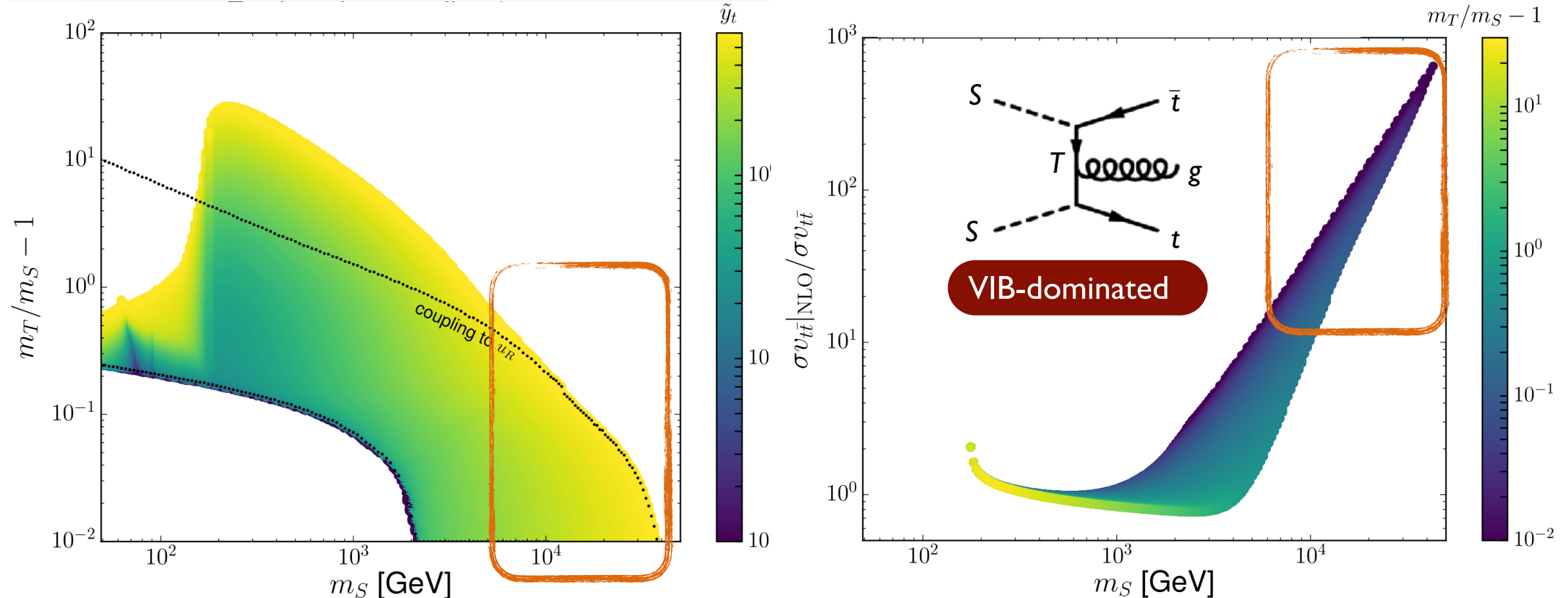
❖ Right relic abundance $\rightarrow \tilde{y}_t$

- ★ Min: 0.001 (co-annihilations)
- ★ Max: 6 (perturbativity)



Multi-TeV dark matter

◆ Regime with a heavy scalar ($m_S > 5 \text{ TeV}$)



❖ Annihilations into tops dominate

$$(\sigma v)_{\text{NLO}} \approx (\sigma v)_{\text{LO}} \left[1 + \frac{\alpha_s C_F}{\pi} \left(\frac{9}{4} - \frac{3}{2} \log \frac{M_S^2}{m_t^2} \right) \right]$$

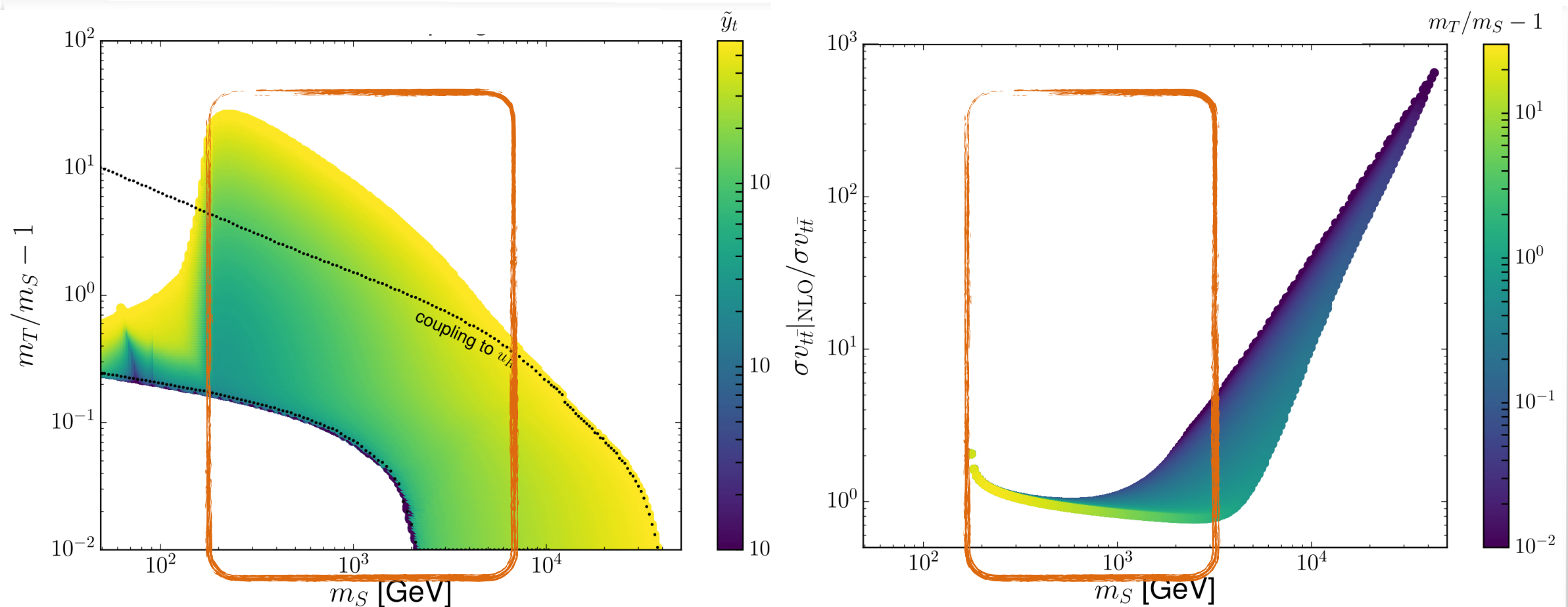
- ★ Top-mass effects negligible
- ★ Velocity-independent (~ 1)

❖ Huge QCD K -factors

- ★ Virtual internal bremsstrahlung (VIB)
($\propto (m_T/m_S)^{-4}$)

Moderately heavy dark matter

◆ Regime with ($m_t < m_S < 5 \text{ TeV}$)



♣ Annihilations into tops dominate

- ★ Important top-mass effects
- ★ Opens up a new region ($\neq$ light quarks)
 - annihilations into quarks negligible
- ★ Mild K -factors

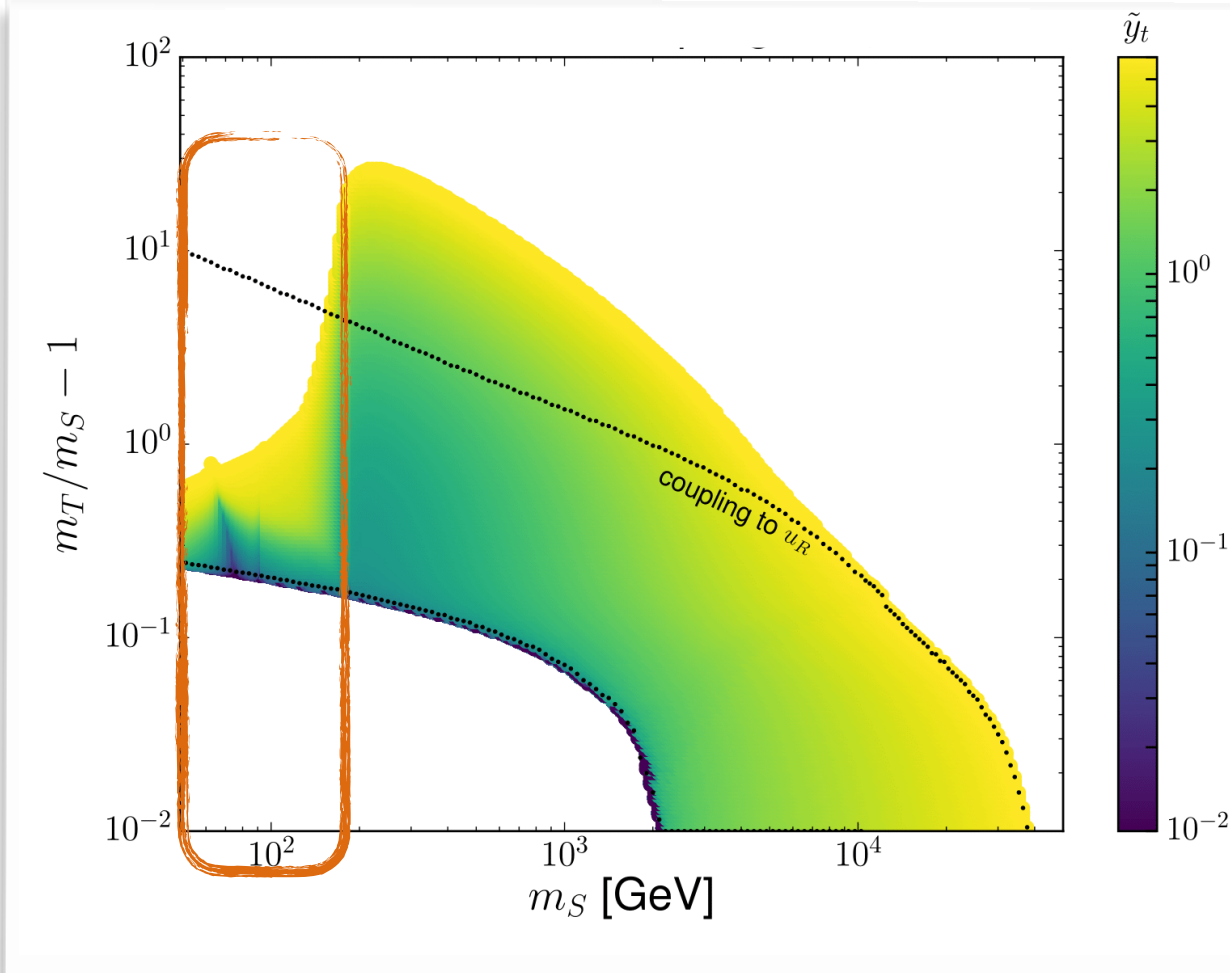
♣ Close to threshold

$$(\sigma v)_{\text{NLO}} \approx (\sigma v)_{\text{LO}} \left[1 + \frac{\alpha_s C_F}{\pi} \left(\frac{\pi^2}{2\beta_0} - 1 \right) \right]$$

- ★ Velocity small
- ★ Spurious results at threshold

Light dark matter

◆ Regime with ($m_S < m_t$)



✿ Annihilations into tops is closed

★ 3-body annihilations (into tWb)

$$m_S \in \left[\frac{m_t + m_W}{2}, m_t \right]$$

★ $SS \rightarrow gg$ important for $m_S < (m_t + m_W)/2$

➤ loop-induced

★ Co-annihilations crucial near $m_T + m_S \sim m_t$
➤ resonant enhancement ($m_S \sim 75$ GeV)

Direct and indirect detection

[Arina, BF, Mantani, Mies, Panizzi & Salko (2020)]

Direct and indirect detection

◆ Higher-order contributions impact indirect/direct detection

- ❖ g/γ radiation $\leadsto$ features in gamma and cosmic ray spectra
- ❖ Loop-induced g -DM scattering $\leadsto$ DM/nucleon scattering
- ❖ More accurate estimations of the scattering cross sections

◆ Constraints

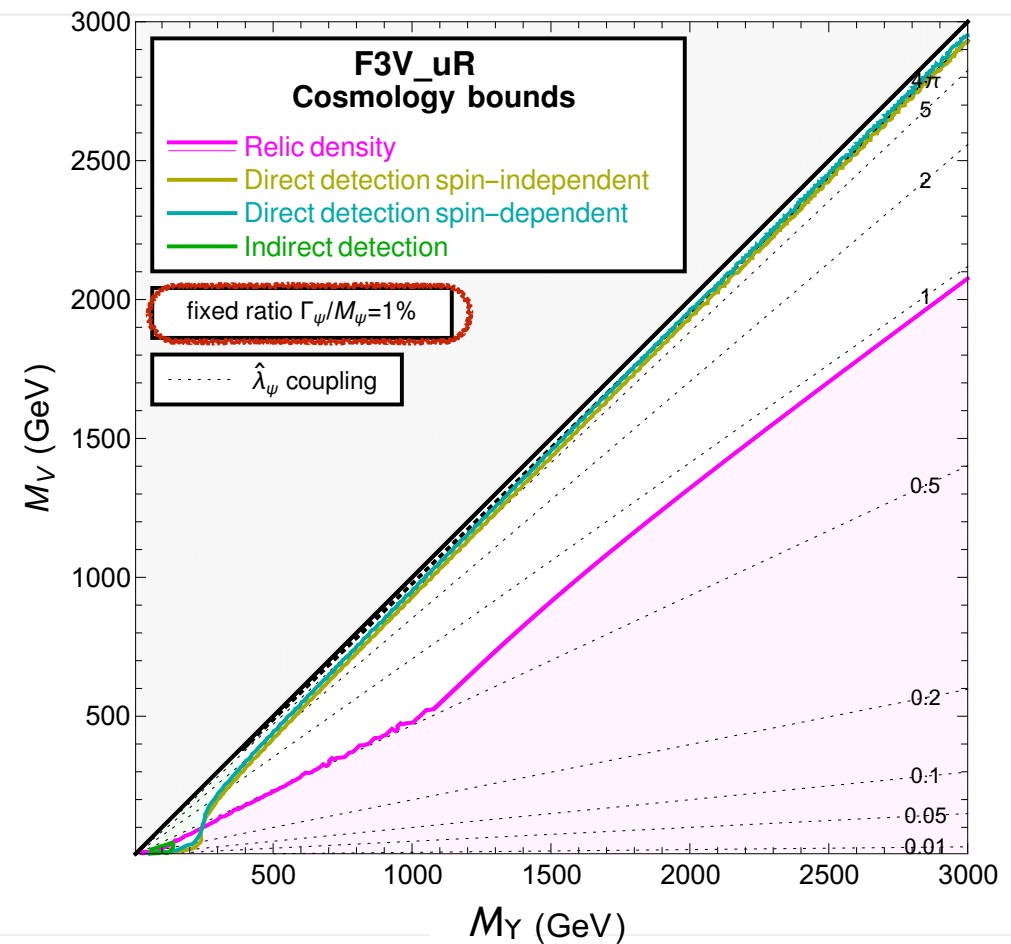
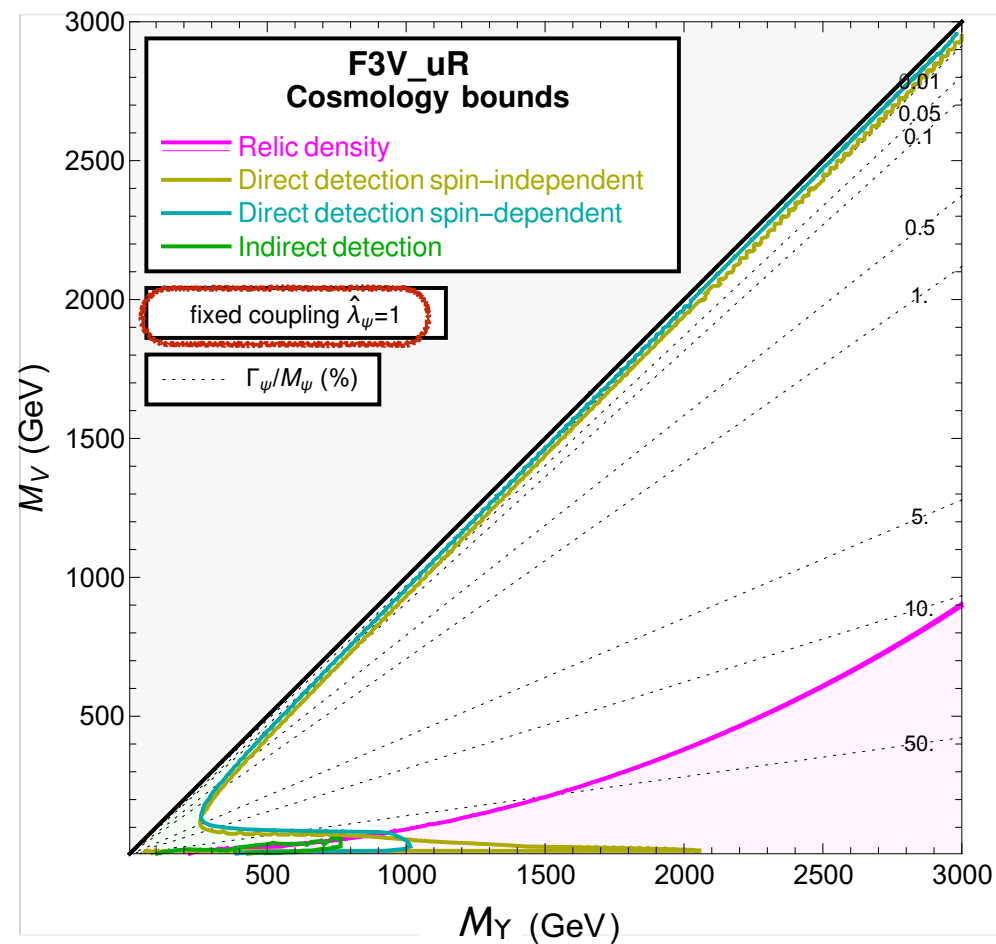
- ❖ PICO: spin-dependent direct detection [PICO Collaboration (PRL`17)]
- ❖ XENONIT: spin-independent direct detection [XENON Collaboration (PRL`18)]
- ❖ FERMI-LAT & HESS: gamma ray spectra [FERMI-LAT Collaboration (PRD`15); HESS Collaboration (PRL`18)]
- ❖ Dwarf spheroidal galaxies: annihilations into gg [DES, FERMI-LAT Collaboration (AJ`17)]

◆ Vector DM coupling to the right-handed up quark

X (DM)	Spin	Self-conj.	Y (med.)	Spin	$\mathcal{L}_{F3V_{uR}} = \left[\hat{\lambda}_u \bar{\psi} \not{V} u_R + \text{h.c.} \right]$
V	1	yes	ψ	1/2	

- ❖ Masses and coupling free

Fixed coupling / fixed width

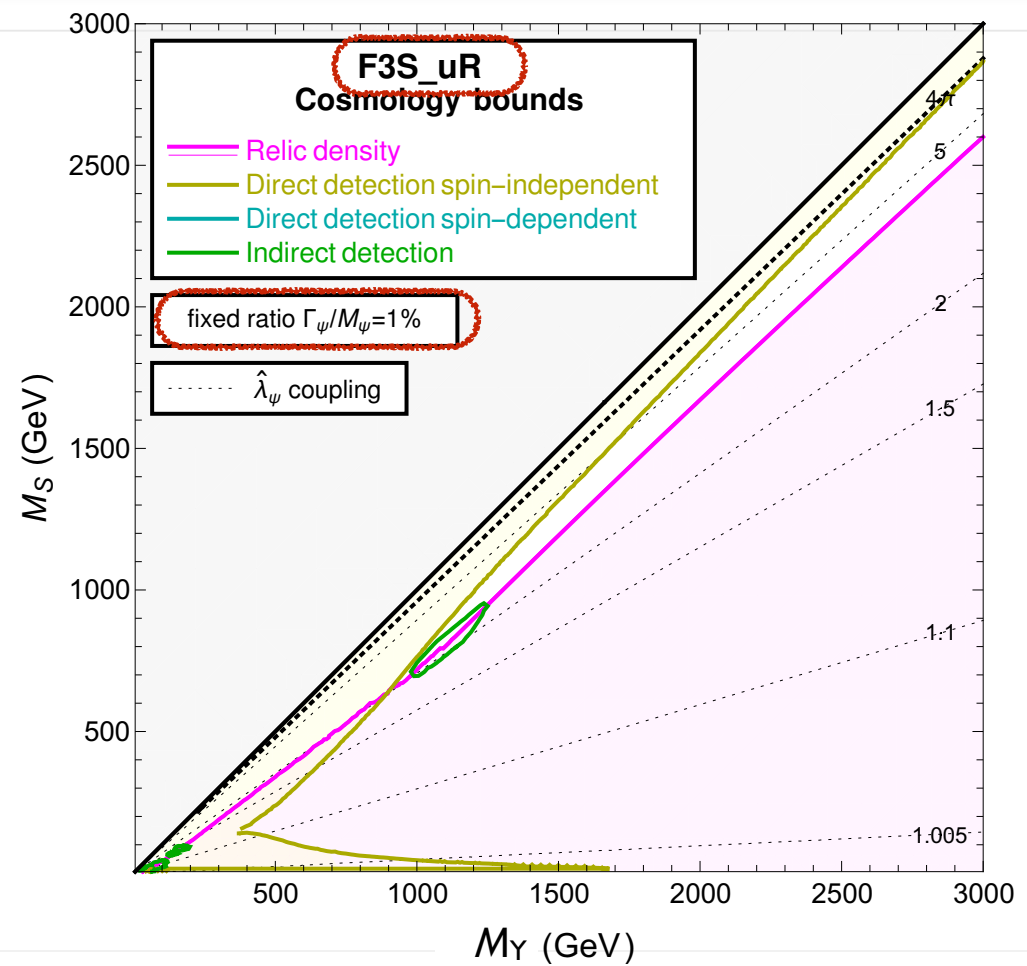
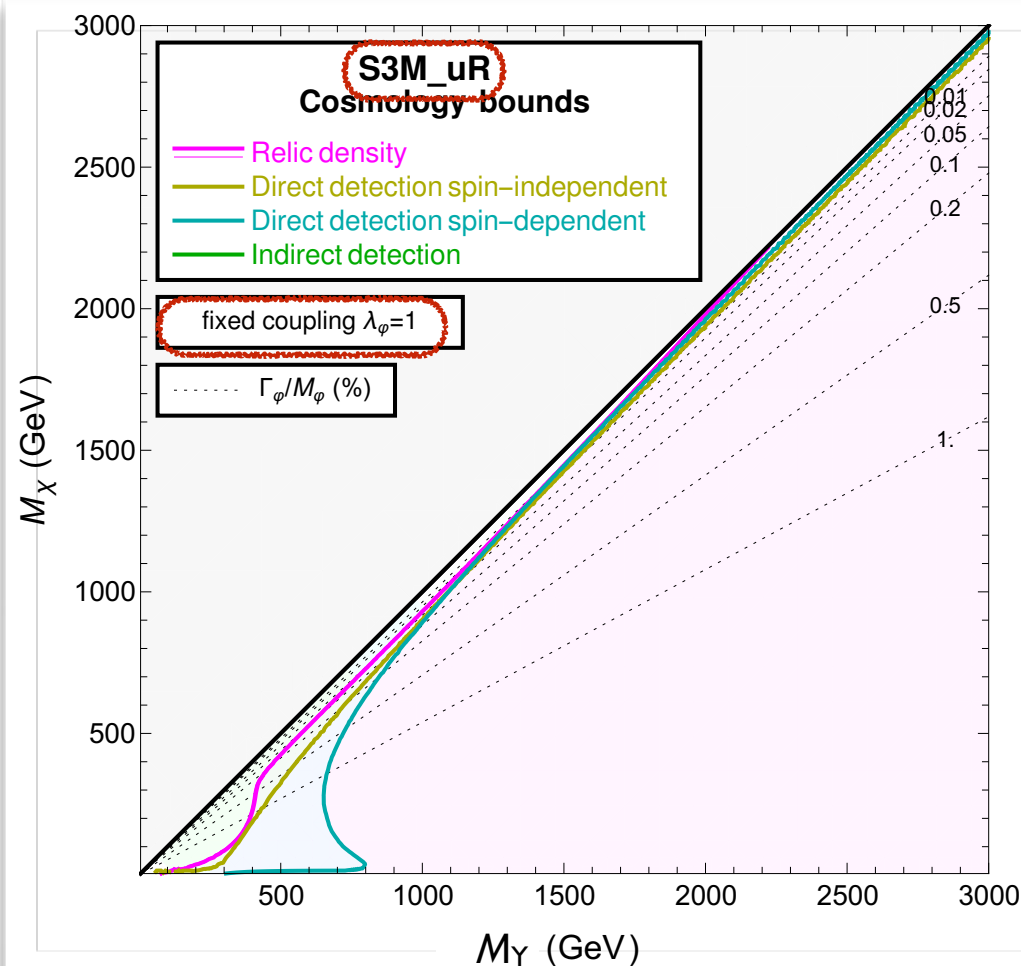


◆ Constraints on the model parameter spaces

- ♣ Relic density: over-abundant DM forbidden (magenta areas)
 - ★ Fixed $\lambda = 1$: broad mediators excluded (not a problem as non resonant)
 - ★ Fixed $\Gamma_Y/M_Y = 1\%$: large coupling is needed
- ♣ SI/SD DD + ID: targets the compressed regime, as well as light DM
- ♣ A significant part of the parameter space is still allowed by cosmology

→ Quite model dependent!

More extreme cases



◆ Barely viable configurations (for u_R -mediators)

♣ Many quite (dis)favoured configurations

★ Majorana DM with $\lambda=1$: relic + ID $\Rightarrow$ excludes all mass configurations

★ Scalar DM with $\Gamma_Y/M_Y = 1\%$: relic + DD $\Rightarrow$ strongly-coupled DM

◆ Cosmology severely constrains t -channel simplified models

♣ Regardless of λ and Γ_Y/M_Y

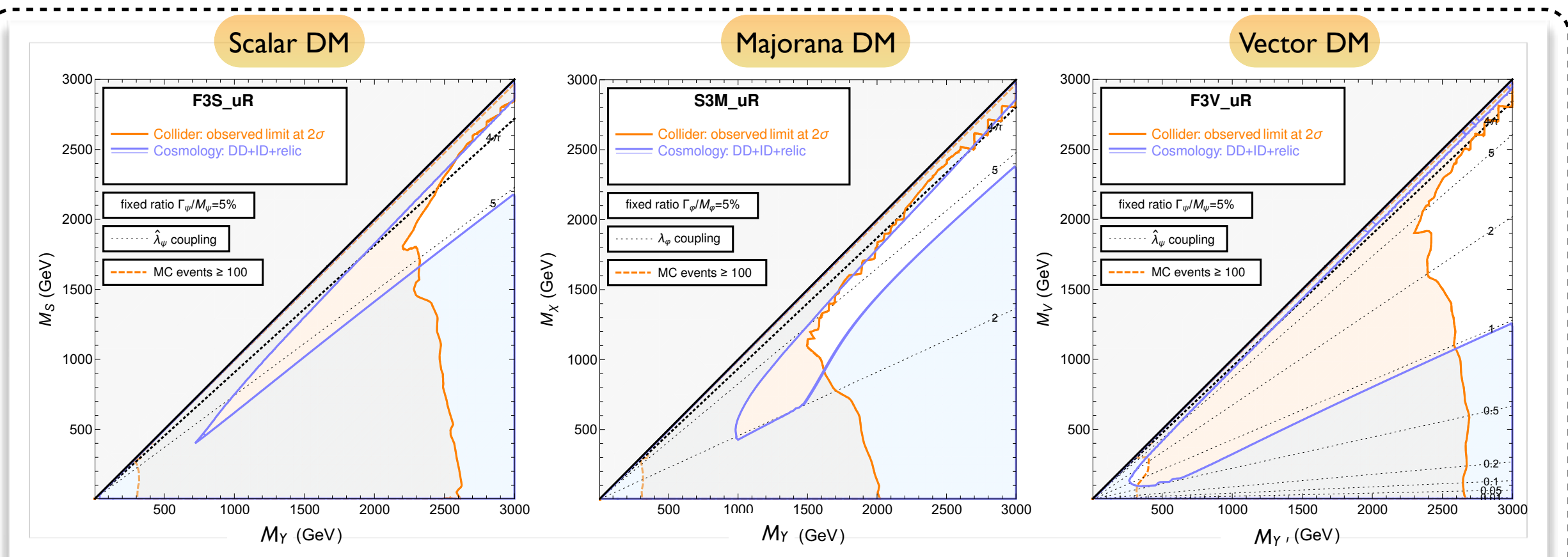
Cosmology-collider complementarity

Closing in it on!

[Arina, BF, Mantani, Mies, Panizzi & Salko (2020)]

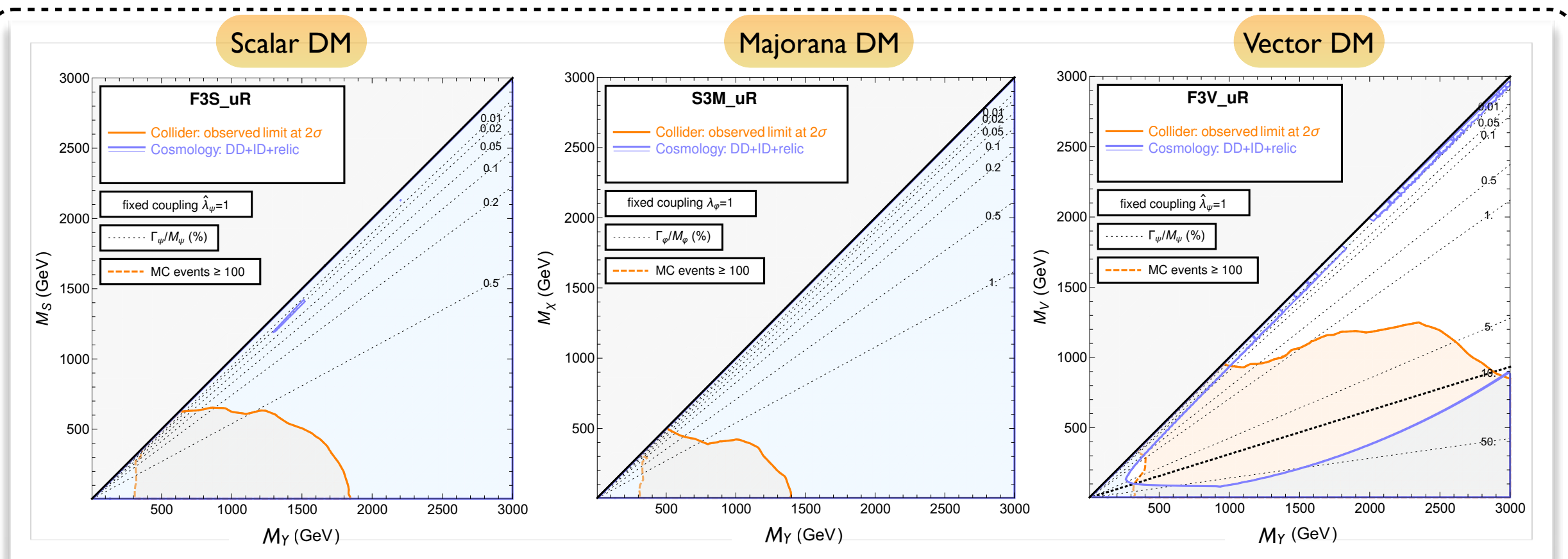
[Colucci, BF, Giacchino, Lopez Honorez, Tytgat & Vandecasteele (PRD`18)]

Example I: u_R mediator $\oplus \Gamma_Y/M_Y = 5\%$



- ◆ Colliders and cosmology are complementary
 - ♣ The mediator must be heavy $\rightarrow$ production at colliders
 - ♣ Cosmology further restricts DM $\rightarrow$ not too light
 - ♣ The spectrum cannot be too compressed $\rightarrow$ colliders/cosmo
- ◆ Implications for viable scenarios
 - ♣ Heavy DM and heavy mediator
 - ♣ A not too compressed/split spectrum
 - ♣ Strongly coupled regime

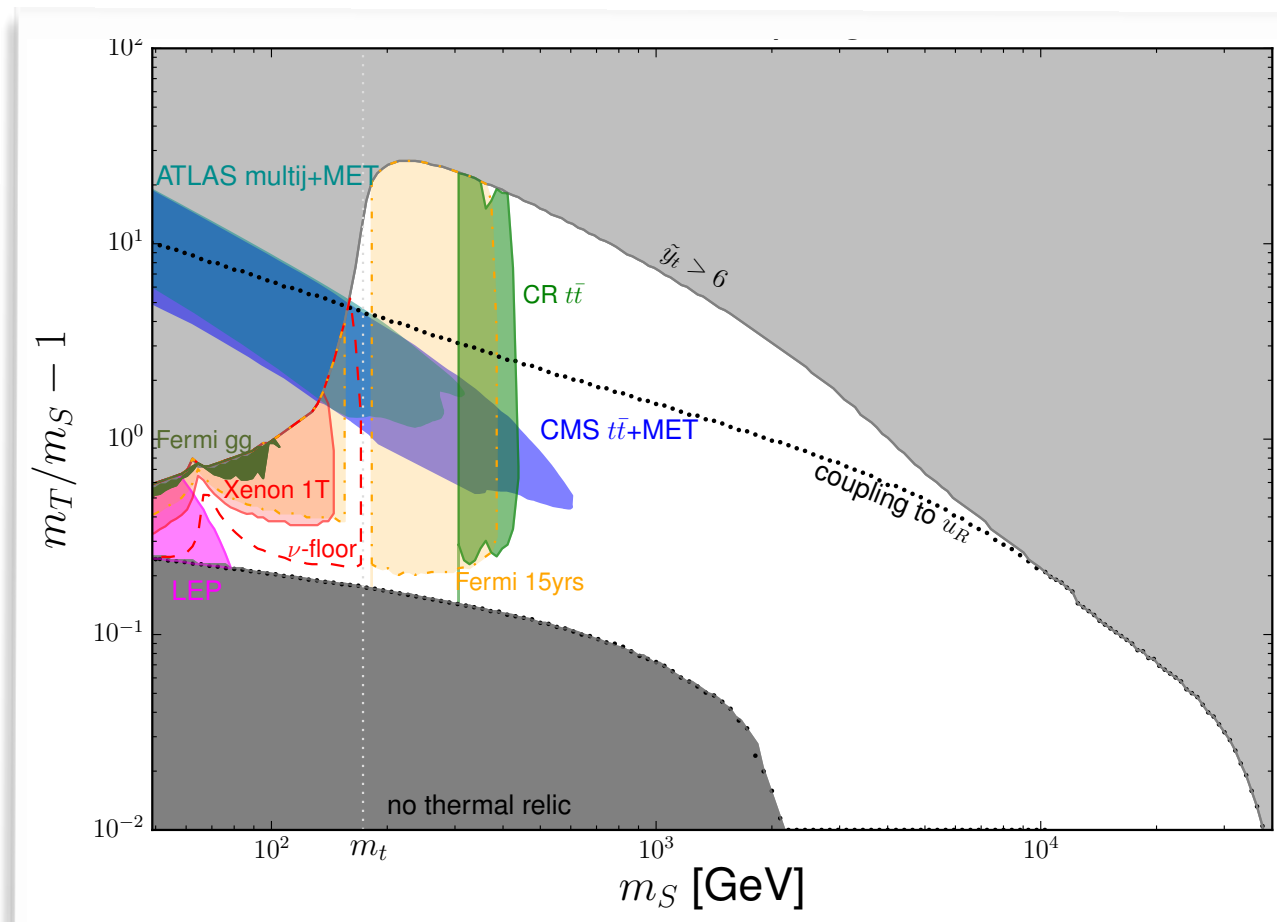
Example 2: u_R mediator $\oplus \lambda = 1$



- ◆ Majorana and scalar DM disfavoured by cosmology alone
- ◆ Vector DM remains mostly viable (if $m_X > 1$ TeV)

Example 3: Scalar DM with a t_R -mediator

◆ Collider-cosmology complementarity at work



❖ Relic-density favoured region

★ Fixes the coupling

★ Dark grey: no thermal relic

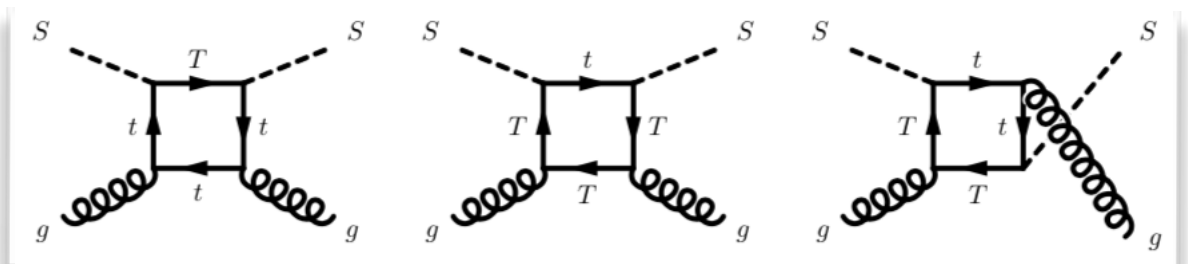
★ Light grey: loss of perturbativity

★ Annihilation into gg below the m_t threshold

❖ DM direct detection constraints

★ Poor sensitivity (loop-induced interactions)

★ Most parameter space below the ν floor



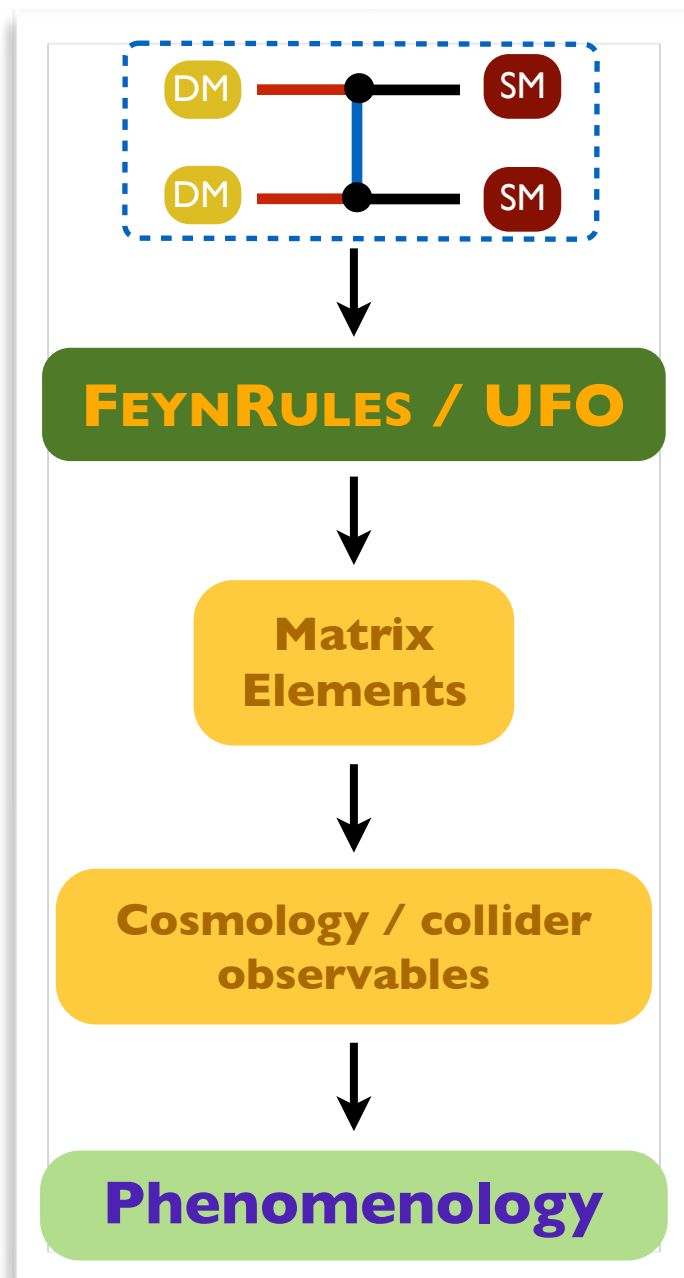
❖ DM indirect detection constraints

★ Exclude limited light DM regions

❖ Colliders: future probe of viable setups

Conclusions

Summary



- ◆ A generic t -channel DM framework is available
 - ♣ Higher order corrections included
 - ♣ **Robust predictions $\Leftrightarrow$ crucial for a discovery**
- ◆ Features
 - ♣ Minimal
 - ♣ Representative of different new physics scenarios
 - ♣ Strongly constrained by current bounds
 - Conclusive statements in the next decades
- ◆ Fingerprints
 - ♣ No non-minimal features (multi-component DM, etc.)
 - ♣ Can change the picture
- ◆ Automated NLO calculations
 - ♣ Important impact on the predictions and the bounds
 - ♣ More information:
 - ★ See the papers: 2001.05024, 2010.07559
 - ★ Web: <http://feynrules.irmp.ucl.ac.be/wiki/DMsimpt>