





FERMILAB MUON g - 2:

FROM a_{μ} TO g

A.P. Schreckenberger [on behalf of the Muon g-2 Collaboration] Planck 2021

Acknowledgments

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TO PEEK BEYOND

Standard Model does a lot...

 Predictions of interactions, masses, experiment observables

Still some unanswered questions

- Matter-antimatter asymmetry
- Presence of dark matter
- Mass and strength hierarchy
- A bunch of anomalies
- Muon g-2 indirect new physics search
 - Virtual particles + behavior of muons



THROUGH WHICH EYES?

- Muon's magnetic moment is used as the handle to search for potential new physics
 - Relation between moment and spin through g-factor

$$\vec{\mu} = g \frac{q}{2m} \bar{S}$$

g also tells us the precession rate of the spin vector in a magnetic field

- For Dirac point-like particle, g = 2
 - And if nature only cared about one Feynman diagram...



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THROUGH WHICH EYES?



*T. Aoyama et al., Phys. Rev. Lett. 109, 111807 (2012)

THROUGH WHICH EYES?

- For Dirac point-like particle, g = 2
 - Radiative corrections from fundamental forces increase value of g





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Standard Model predicts g > 2, so what gives?

DEFINING AN ANOMALY



- Indicator for potential unknown processes
 - Define the anomaly (a_{μ}) , which tells us the fractional difference between exciting things and a Boring Universe
 - Anomaly is the parameter of interest for the Muon g-2 Experiment

$$a_{\mu}=\frac{g_{\mu}-2}{2}$$

REWIND TO MARCH 2021

- QED contributes most to anomaly, least to uncertainty
- Hadronic terms bring most uncertainty QCD is non-perturbative
- Hints from tension between Brookhaven (BNL) result and theory

$$a_{\mu}=\frac{g_{\mu}-2}{2}$$



CONTRIBUTION	$\text{VALUE} \times 10^{11}$
Experiment (Final BNL)	116 592 089. (63)
QED	116 584 718.931(104)
Electroweak	153.6 (1)
HVP (e^+e^- , LO + NLO + NNLO)	6845. (40)
HLbL (pheno. + lattice + NLO)	92. (18)
otal Standard Model (SM) Value	116 591 810. (43)
Difference: a_{μ} (Final BNL) – a_{μ} (SM)	279. (76)

BRIEF THEORETICAL ASIDE

- Collaboration compares result to WP20 prediction value
 - From Muon g-2 Theory Initiative
 - Group continues to update its result
 - BMW20 Lattice QCD calculation is first lattice result with sub-percent precision
 - Potential decrease in tension with experiment
 - Still being discussed in theory community
- Focus on explaining the experiment





BUILDING AT FERMILAB

- Physicists love tension... finding it... resolving it...
 - The Universe is the most imaginative thing in the room. How imaginative is it?
- After ~20 years, Fermilab Muon g-2 formed to try to answer the underlying questions from BNL
 - Fermilab experiment aims to make 140 ppb measurement
- Why the move? Lots of muons!
 - 8 GeV protons extracted from Recycler Ring
 - Sent incident on nickel-based target
 - Left with a highly polarized muon beam at the end of this beamline



THE EXPERIMENTAL PRINCIPLE

- Storage ring provides 1.45T field
- Physics ensnared in mismatch between cyclotron and spin precession frequencies

•
$$\vec{\omega}_{C} = -\frac{q}{\gamma m} \vec{B}$$

• $\vec{\omega}_{S} = -\frac{q}{\gamma m} \vec{B} (1 + \gamma a_{\mu})$
• $\vec{\omega}_{a} \cong \vec{\omega}_{S} - \vec{\omega}_{C} = -\frac{q}{m} a_{\mu} \vec{B}$



A MAGIC MOMENTUM



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$$\vec{\omega}_a \cong \vec{\omega}_S - \vec{\omega}_C = -\frac{q}{m} a_\mu \vec{B}$$

- Ring field = horizontal focusing
- Electrostatic quadrupoles used for vertical
 - Muons observe magnetic field

$$\vec{\omega}_a \cong -\frac{q}{m} \left(a_\mu \vec{B} - \left(a_\mu - \frac{1}{\gamma^2 - 1} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right)$$



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ADDED COMPLEXITY

 "Magic Momentum" minimizes electric field correction

Aomentum" minimizes electric
ection
$$\vec{\omega}_{a} \cong -\frac{q}{m} \left(a_{\mu} \vec{B} - \left(a_{\mu} - \frac{1}{\gamma^{2} - 1} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right) \qquad \gamma \sim 29.3$$
$$\vec{\omega}_{a} \equiv \vec{\omega}_{s} - \vec{\omega}_{c} = -\frac{q}{m_{\mu}} \left[a_{\mu} \vec{B} - a_{\mu} \left(\frac{\gamma}{\gamma + 1} \right) (\vec{\beta} \cdot \vec{B}) \vec{\beta} - \left(a_{\mu} - \frac{1}{\gamma^{2} - 1} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right]$$

al

- Muon beam swims and breathes in both horizontal and vertical directions
 - Pitch correction needed to address motion outside the ring plane
 - Beam dynamics effects become more pertinent to analysis
- Lots of effects to consider, but eventually we reach a form for the anomaly...

HOW WE TACKLE a_{μ}

$$a_{\mu}(expt) = \frac{g_e}{2} \frac{m_{\mu}\mu_p}{m_e\mu_e} \frac{\omega_p}{\omega_e}$$

$$= \frac{g_e}{2} \frac{m_\mu}{m_e} \frac{\mu_e(H)}{\mu_e} \frac{\mu'_p(T_r)}{\mu_e(H)} \frac{\omega_a}{\widetilde{\omega'_p}(T_r)}$$

Proton Larmor precession frequency in a spherical water sample. Temperature dependence known to < 1ppb/°C. $\tilde{\omega}_p'(T)$ Metrologia 13, 179 (1977), Metrologia 51, 54 (2014), Metrologia 20, 81 (1984)

 $\mu_e(H)$ Measured to 10.5 ppb accuracy at $T = 34.7^{\circ}C$ Metrologia 13, 179 (1977)

Bound-state QED (exact)

 $\mu'_p(T)$

- Rev. Mod. Phys. 88 035009 (2016)
- Known to 22 ppb from muonium hyperfine splitting m_{μ}
- Phys. Rev. Lett. 82, 711 (1999) m_{e}
- Measured to 0.28 ppt g_e
- $\mathbf{2}$ Phys. Rev. A 83, 052122 (2011)

- ω_a is the anomalous precession frequency
- $\widetilde{\omega}'_{p}(T_{r})$ is the Larmor precession frequency of protons in a water sample mapping the B field and weighted by the muon distribution
 - Evaluates the magnetic field observed by the muons as they propagate around the ring

Goal: 140 ppb [100 ppb (stat) + 100 ppb (sys)]

- Storage ring: 1.45T field, horizontal focusing
 - High uniformity through shimming process



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- Storage ring: 1.45T field, horizontal focusing
 - High uniformity through shimming process
- Inflector: Superconducting magnet
 - Entryway for muon beam
- Kickers: Nudge injected beam onto storable trajectories
- Electrostatic Quadrupoles: vertical focusing
 - Four quads cover 43% of the storage ring





TOOLS FOR $\omega_a / \widetilde{\omega}'_p(T_r)$

• Need to determine B at < 100 ppb to determine a_{μ}

• Use NMR to assess B-field in terms of proton precession frequency ω_p



MORE THAN JUST THE B-FIELD





- Decay positrons pass through straw trackers
- Construct muon beam profile from tracker data
- Combine with field map





THE DENOMINATOR

Magnetic field map + Beam profile = AVERAGE FIELD THE MUONS OBSERVE



related to $\widetilde{\omega}_{m{p}}'(T_{m{\gamma}})$

THE NUMERATOR

24 calorimeters placed around the ring measure positron energy spectrum



- The power of an energy cut...
- Parity-violating weak decay $[\mu^+ \rightarrow \overline{\nu}_{\mu}\nu_e e^+] \rightarrow$ high-energy positrons preferentially emitted in direction of muon spin

THE NUMERATOR

- Cut at events above 1.7 GeV $f(t) \simeq N_0 e^{-\lambda t} [1 + A \cos(\omega_a t + \phi)]$
- Number of events in that range depends on the anomalous precession frequency
 - Fit to determine ω_a
- All of the pieces are in place...



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THE REALITIES OF ANALYSIS

- Complexities discovered and considerations made
 - Kickers and quads operations required four subruns
 - Pulse-power systems also involved with the field transients
- Corrections and systematics studied in excruciating detail
 - "Expect results in a year!" ~Talk circa 2018



$\begin{aligned} \mathbf{f}_{clock} \boldsymbol{\omega}_{a} \left(\mathbf{1} + \mathbf{C}_{e} + \mathbf{C}_{p} + \mathbf{C}_{ml} + \mathbf{C}_{pa}\right) \\ \text{EXCRUCIATING DETAIL} \end{aligned}$

'pa

Source	Uncertainty	$R(\omega_a)$ with detailed s	ystemati	cs cate	gories	[ppb]		1a	1b	1c	10
	1	Total systematic uncertainty	65.2	70.5	54.0	48.8	C _c (nnh)	471	464	534	47
Frequency Standard	1 ppt	Time randomization	14.8	11.7	9.2	6.9	Ce (ppb)			004	
Frequency Synthesizers	0.1 ppb	Time correction	3.9	1.2	1.1	1.0	Statistical uncertainty	0.4	0.5	0.4	0.
	0 J	Gain	12.4	9.4	8.9	4.8	Fourier method	8.4	13.4	14.4	3.
Digitization Frequency	2 ppb	Pileup	39.1	41.7	35.2	30.9	Momentum-time correlation	52	52	52	5
Total Systematic	2 ppb	Pileup artificial dead time	3.0	3.0	3.0	3.0	Momentum-time correlation	52	52	52	52
	- 662	Muon loss	2.2	1.9	5.2	2.4	Quad alignment/voltage	6.4	6.4	6.4	6.
falsal		СВО	42.0	49.5	31.5	35.2	Field index	1.7	1.5	1.7	4.
CIOCK		Ad-hoc correction	21.1	21.1	22.1	10.3	Systematic uncertainty	53	54	54	51
		ω_a					C _e				
	A AL A	4.1									

	1a	1b	1c	1d
C _p (ppb)	176	199	191	166
Statistical uncertainty	<0.1	<0.1	<0.1	<0.1
Tracker alignment/reco.	11.0	12.3	12.0	10.7
Tracker res. & acc. removal	3.3	3.9	3.7	3.0
Azimuthal avg. & calo. acc.	1.0	1.3	2.2	1.1
Amplitude fit	1.2	0.4	1.0	2.9
Quad alignment/voltage	4.4	4.4	4.4	4.4
Systematic uncertainty	12.4	13.7	13.6	12.3

Data Set	Run-1a	Run-1b	Run-1c	Run-1d
C_{ml}	-14	-3	-7	-17
Phase-momentum	2	0	1	3
Form of $l(t)$	2	0	1	1
f_{loss} function	2	1	2	2
Linear sum $(\sigma_{C_{ml}})$	6	2	4	6

C_{ml}

Data Set	Run-1a	Run-1b	Run-1c	Run-1d
C_{pa}	-184	-165	-117	-164
Stat. uncertainty	23	20	15	14
Tracker & CBO	73	43	41	44
Phase maps	52	49	35	46
Beam dynamics	27	30	22	45
Total uncertainty	96	74	60	80

$(\mathbf{1} + \mathbf{B_q} + \mathbf{B_k}) \mathbf{f_{field}} \boldsymbol{\omega}_p \otimes \boldsymbol{\rho}(\mathbf{r})$ EXCRUCIATING DETAIL

total -15.0 ppb	81.7 ppb
2 nd 8-pulses	14.0 ppb
radial dependency	4.4 ppb
drift	$10.2\mathrm{ppb}$
repeatability	13.3 ppb
Q3L: fit, position	$1.5\mathrm{ppb}$
frequency extraction $(0.4/1 \text{ms})$	$4.6\mathrm{ppb}$
skin depth	12.6 ppb
azimuthal shape*	7.6 ppb
run-1 (substructure)	77.4 ppb

DRORE	Calibration Coefficients							
PROBE	Value (Hz)	Stat (Hz)	Syst (Hz)					
1	90.81	0.38	2.02					
2	84.21	0.65	1.18					
3	95.02	0.53	2.19					
4	86.03	0.25	1.28					
5	92.96	0.51	1.10					
6	106.24	0.46	1.35					
7	116.64	0.96	1.61					
8	76.39	0.60	1.21					
9	83.52	0.23	1.64					
10	24.06	1.39	1.26					
11	177.55	0.22	1.99					
12	110.85	0.44	1.73					
13	122.89	2.08	1.93					
14	77.11	0.53	1.88					
15	74.82	1.06	1.59					
16	20.35	0.44	2.94					
17	172.12	1.23	1.96					
AVG		0.70	1.70					

Run-1 Estimate: $B_k = -27.4 \pm 37 \text{ ppb}$

Source	Uncertainty (ppb)
Temperature	15 – 28
Configuration	22
Trolley	25
Fixed Probe Production	<1
Fixed Probe Baseline	8
Tracking Drift	22 – 43
Total	43 - 62

Quantity	Symbol	Value	Unit
Diamagnetic Shielding T dep	(1/σ)dσ/dT	-10.36(30)	ppb/°C
Bulk Susceptibility	δ _b	-1504.6 ± 4.9	ppb
Material Perturbation	δs	15.2 ± 13.3	ppb
Paramagnetic Impurities	δ _p	0 ± 2	ppb
Radiation Damping	δrd	0 ± 3	ppb
Proton Dipolar Fields	δ _d	0 ± 2.3	ppb

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		correction [ppb]				uncertai	nty [ppb]	
Dataset	1a	1b	1c	1d	1a	1b	1c	1d
1. Tracker and calo effects	-	-	-	-	9.2	13.3	15.6	19.7
2. COD effects	1.6	1.5	1.7	1.4	5.2	4.7	5.2	4.9
3. In-fill time effects	-1.9	-2.3	-1.2	-4.1	-	-	-	-
Total	-0.3	-0.8	0.5	-2.7	10.6	14.1	16.5	20.3

REACHING A RESULT



• $a_{\mu}(SM) = 0.00116591810(43) \rightarrow 368 \text{ ppb}$ [Muon g-2 Theory Initiative]

DIGGING A LITTLE DEEPER

Quantity	Correction Terms	Uncertainty
	(ppb)	(ppb)
ω_a^m (statistical)	_	434
ω_a^m (systematic)	-	56
$\overline{C_e}$	489	53
C_p	180	13
C_{ml}	-11	5
C_{pa}	-158	75
$f_{\text{calib}}\langle\omega_p(x,y,\phi)\times M(x,y,\phi)\rangle$	_	56
B_k	-27	37
B_q	-17	92
$\mu_p'(34.7^\circ)/\mu_e$	_	10
m_{μ}/m_e	_	22
$g_e/2$	_	0
Total systematic	_	157
Total fundamental factors	_	25
Totals	544	462

- FNAL experiment determined a_{μ} to unprecedented precision
- Run-1 uncertainties dominated by statistics
 - 6% of ultimate data sample
 - 15% smaller error than BNL
 - 157 ppb systematic error is half BNL level
- Phase acceptance and field transient systematics became major topics of study for Muon g-2

QUAD TRANSIENT (B_q)

• At FNAL repetition rate, quad pulsing induces mechanical vibrations — this is a new problem

- Vibrations perturb the B-field!
- Special NMR probes built to map this effect
 - Long & Winding Road
- 17 ppb correction
 - Only matters in window when muons are present (grey band in plot), averaged over 8 bunches and 43% of the ring
- 92 ppb uncertainty dominated by lack of information
 - Run-1 did not have complete map
 - Run-2 and beyond will = 2x-3x reduction





Time (ms)





PHASE ACCEPTANCE (C_{pa})

- Basic fit function follows: $f(t) \simeq N_0 e^{-\lambda t} [1 + A \cos(\omega_a t + \phi)]$
 - Consider case where $\phi \rightarrow \phi(t)$:

 $cos(\omega_a t + \phi(t)) = cos(\omega_a t + \phi_0 + \phi' t + \dots)$ $= cos((\omega_a + \phi')t + \phi_0 + \dots)$

- Extracted ω_a is shifted by ϕ'
- Detected decay positrons carry particular phase
 - Phase depends on decay position (x,y) and energy (E)
 - Not a big issue if muon distribution remains stable

PHASE ACCEPTANCE (C_{pa})



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Equipment failure in quad circuit led to instability

- Damaged resistors changed E-field
- Vertical distribution → changing acceptance → changing measurement
- 158 ppb correction with 75 ppb uncertainty
 - Resistors fixed by Run-2, remove significant impact



"Getting a charged particle to go in a circle is easy. Getting it to go in the one you want is a miracle of science" ~Adam KICKER EFFECTS $(C_e)(B_k)$

- Kicker plates receive 4kA in 200-ns timescale
 - Presents a technical challenge to the experiment
 - Current vs. muon beam distribution factors into momentum-time correlation
 - Part of the (C_e) correction
 - Concerned about eddy currents produced by main kick
 - Multiple magnetometers and groups assessed the inducedfield relaxation
 - Complementary methods agree on -27 ppb correction
 - Ongoing work to see if we can reduce 37 ppb uncertainty
- Kicker paper in peer review



17.5



BACKUP THINGS



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Campus