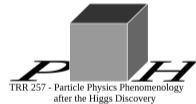


# Theory perspective on the flavour anomalies

Monika Blanke



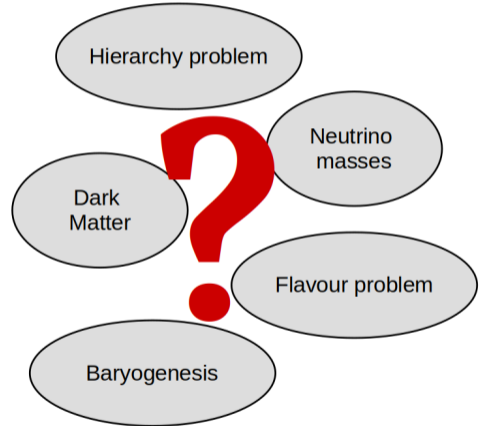
Planck 2021  
Durham/Zoom – June 30, 2021

# New Physics, where are you?

## After a decade of LHC operation

- discovery of **Higgs boson**
  - apparent completion of Standard Model
- Higgs, electroweak and top measurements in **impressive agreement with SM**
- no evidence for TeV-scale new particles, increasingly **stringent bounds**

➤ **huge success of the Standard Model!**



# The quest for high precision

## Possible paths to New Physics

```
graph TD; A[Possible paths to New Physics] --> B[Direct searches – energy frontier]; A --> C[Indirect probes – precision frontier]; B --> D[complementarity & interplay]; C --> D;
```

### Direct searches – energy frontier

- increased luminosity
- higher energies ( $\triangleright$  new collider)
- new observables

### Indirect probes – precision frontier

- rare processes
- theoretically clean
- experimentally under control

**complementarity & interplay**

# Flavour physics at the precision frontier

## Quark flavour physics

- SM flavour violation strongly suppressed by CKM hierarchy
- additional GIM suppression for neutral current processes
- plethora of measurable meson (and baryon) decays
- many processes theoretically well understood
- overall good agreement with SM predictions

## Lepton flavour physics

### Lepton flavour violation

- absent in the SM
- unambiguous sign of New Physics
- small rates, no interference with SM contribution

### Lepton flavour universality

- approximately conserved in the SM, broken only by small Yukawa couplings
- theoretically clean
- measurable rates

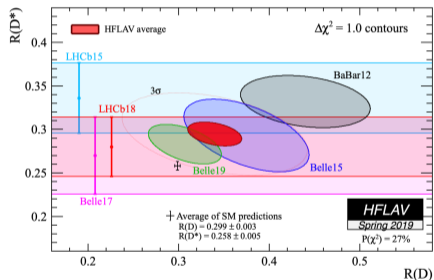
# (Not-so-)Recent news from lepton flavour universality tests

- $R(D^{(*)})$  **anomaly** –  $3.1\sigma$  anomaly in **charged current semi-tauonic  $B$  decays**, exhibiting LFU violation
- $R(K^{(*)})$  **anomaly** – various *consistent*  $2 - 3\sigma$  deviations in **neutral current semi-leptonic  $B$  decays**
- $(g - 2)_\mu$  **anomaly** –  $4.2\sigma$  tension between SM prediction and data in **anomalous magnetic moment of the muon**
- **Cabibbo angle anomaly** –  $3\sigma$  deviation from **first-row CKM unitarity**, hinting at possible violation of LFU in charged-current transitions



# The $R(D^{(*)})$ anomaly

## Test of lepton flavour universality in semi-tauonic $B$ decays



$$R(D^{(*)}) = \frac{\text{BR}(B \rightarrow D^{(*)}\tau\nu)}{\text{BR}(B \rightarrow D^{(*)}\ell\nu)} \quad (\ell = e, \mu)$$

- **theoretically clean**, as hadronic uncertainties largely cancel in ratio
- **measurements** by BaBar, Belle, LHCb ( $\mathcal{R}(D^{(*)})$  only)
- **model-independent sum-rule** relating values of  $R(D)$ ,  $R(D^{*})$  and  $R(\Lambda_c)$ 
  - **experimental consistency check**

MB, CRIVELLIN, DE BOER, KITAHARA,  
MOSCATI, NIERSTE, NIŠANDŽIĆ (2018), (2019)

➤ **3.1 $\sigma$  discrepancy with SM**

## Effective Hamiltonian for $b \rightarrow c\tau\nu$

New Physics above  $B$  meson scale described model-independently by

$$\mathcal{H}_{\text{eff}}^{\text{NP}} = 2\sqrt{2}G_F V_{cb} \left[ (1 + C_V^L) O_V^L + C_S^R O_S^R + C_S^L O_S^L + C_T O_T \right]$$

with

$$O_V^L = (\bar{c}\gamma^\mu P_L b) (\bar{\tau}\gamma_\mu P_L \nu_\tau)$$

$$O_S^R = (\bar{c}P_R b) (\bar{\tau}P_L \nu_\tau)$$

$$O_T = (\bar{c}\sigma^{\mu\nu} P_L b) (\bar{\tau}\sigma_{\mu\nu} P_L \nu_\tau)$$

$$O_S^L = (\bar{c}P_L b) (\bar{\tau}P_L \nu_\tau)$$

### Possible (tree-level) NP scenarios:

- **charged Higgs** contributions  $\triangleright C_S^{L,R} \neq 0$

KALINOWSKI (1990); HOU (1993)  
CRIVELLIN, KOKULU, GREUB (2013)...

- **charged vector boson**  $W'$   $\triangleright C_V^L \neq 0$  HE, VALENCIA (2012); GRELJO, ISIDORI, MARZOCCA (2015)...

- (scalar or vector) **leptoquark**  $\triangleright$  various  $C_j \neq 0$  (depending on model)

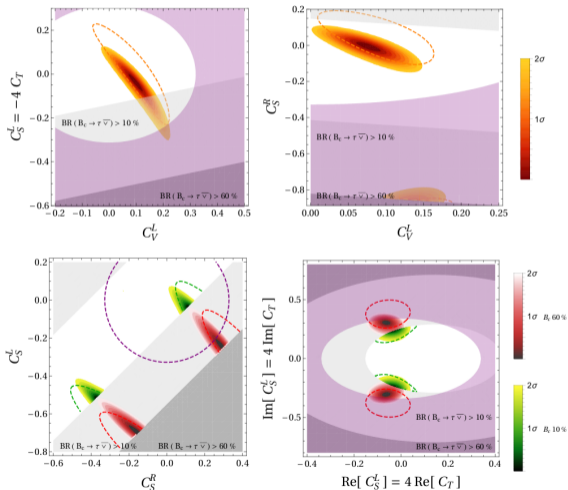
see e. g. TANAKA, WATANABE (2012); DESHPANDE, MENON (2012); KOSNIK (2012); FREYTSIS ET AL (2015)  
ALONSO ET AL (2015); CALIBBI ET AL (2015); FAJFER, KOSNIK (2015); BECIREVIC ET AL (2016),(2018)

# Single particle scenarios

MB, CRIVELLIN, KITAHARA, MOSCATI, NIERSTE, NIŠANDŽIĆ (2019)  
see also MURGUI ET AL (2019); SHI ET AL (2019)

## Main results

- $W'$  solution disfavoured by LHC direct searches FAROUGHY, GRELJO, KAMENIK (2016)
- significant improvement possible with various **leptoquark** scenarios
- **charged Higgs** scenario predicts very large  $\text{BR}(B_c \rightarrow \tau\nu) \simeq 50\%$   
see ALONSO, GRINSTEIN, MARTIN CAMALICH (2016)  
AKERROYD, CHEN (2017); MB ET AL (2018)  
AEBISCHER, GRINSTEIN (2021)
- constraints from **LHC mono- $\tau$  constraints**  
GRELJO, MARTIN CAMALICH, RUIZ-ALVAREZ (2018)





# More flavour observables to test NP in $R(D^{(*)})$

## Direct probes of NP structure

- $B \rightarrow D^{(*)}\tau\nu$  differential distributions, angular and polarisation observables

NIERSTE ET AL (2008); CELIS ET AL (2016); BECIREVIC ET AL (2016)  
IGURO ET AL (2018); MB, CRIVELLIN ET AL (2018); ALONSO ET AL (2018); BECIREVIC ET AL (2019)

## Additionally: implied by $SU(2)_L$ symmetry

- large impact on  $B \rightarrow K^{(*)}\nu\bar{\nu}$ ,  $B_s \rightarrow \tau^+\tau^-$ ,  $B \rightarrow K\tau^+\tau^-$  CRIVELLIN, MÜLLER, OTA (2017)
- contributions to  $\Upsilon \rightarrow \tau^+\tau^-$  and  $\psi \rightarrow \tau^+\tau^-$  ALONI ET AL. (2017)

## Complementary probes in high- $p_T$ searches

- strong constraints from  $b\bar{b} \rightarrow \tau\bar{\tau}$  and mono- $\tau$  at ATLAS and CMS

FAROUGHY, GRELJO, KAMENIK (2016); ALTMANNSHOFER, DEV, SONI (2017)  
GRELJO, MARTIN CAMALICH, RUIZ-ALVAREZ (2018)

➤ full NP resolution of  $R(D^{(*)})$  anomaly challenging

# The $R(K^{(*)})$ anomaly

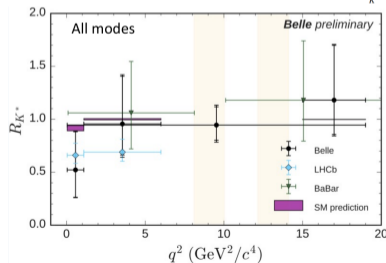
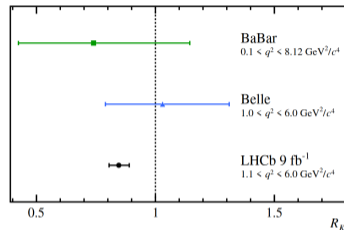
## Test of LFU in $b \rightarrow s\ell^+\ell^-$ transitions

$$R(K^{(*)}) = \frac{\text{BR}(B \rightarrow K^{(*)}\mu^+\mu^-)}{\text{BR}(B \rightarrow K^{(*)}e^+e^-)}$$

- recent LHCb update lifted  $R(K)$  anomaly above  $3\sigma$
- $R(K^*)$  and  $R(Kp)$  hint in same direction

## Anomalies seen in various $b \rightarrow s\mu^+\mu^-$ observables

- angular distribution of  $B \rightarrow K^*\mu^+\mu^-$  (mainly  $P'_5$ )
- less significant tensions in other decays, e. g.  $B_s \rightarrow \phi\mu^+\mu^-$ ,  $B_s \rightarrow \mu^+\mu^-$

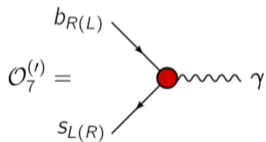


# New Physics in $b \rightarrow sl^+l^-$

Effective  $b \rightarrow sl^+l^-$  Hamiltonian:

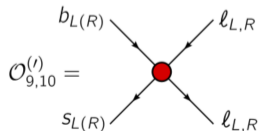
$$\mathcal{H}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{tb}^* V_{ts} \frac{e^2}{16\pi^2} \sum_i (C_i \mathcal{O}_i + C'_i \mathcal{O}'_i) + h.c.$$

with the operators most sensitive to New Physics



**electromagnetic dipole operators  $\mathcal{O}_7^{(\prime)}$**

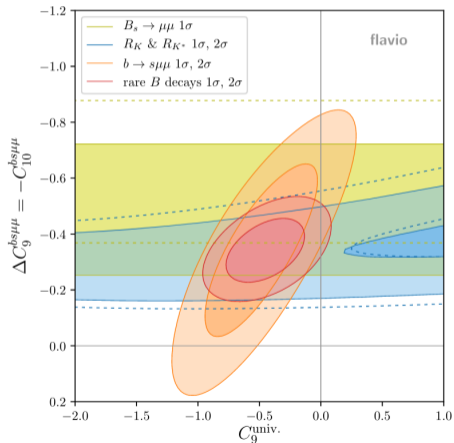
- govern inclusive and exclusive  $b \rightarrow s\gamma$  transitions
- enhanced contribution to  $B \rightarrow K^*\ell^+\ell^-$  in low  $q^2$  region



**semileptonic four-fermion operators  $\mathcal{O}_9^{(\prime)}, \mathcal{O}_{10}^{(\prime)}$**

- loop-suppressed in the SM, but potentially tree level in the presence of NP

# Status of global fits



ALTMANNSHOFER, STANGL (2021)

see also GENG, GRINSTEIN, JÄGER, LI, M. CAMALICH, SHI (2021)

## Main results

- best 1D fit solutions ( $\sim 6\sigma$  pulls):

- $C_9^{bs\mu\mu} \simeq -0.80$
- $C_9^{bs\mu\mu} = -C_{10}^{bs\mu\mu} \simeq -0.41$

- non-zero  $C_{10}^{bs\mu\mu}$  preferred by deviation in  $\text{BR}(B_s \rightarrow \mu^+ \mu^-)$
- small flavour-universal contribution to  $C_9$  possibly generated by RGE effects ( $b \rightarrow s\tau\tau$ ) (or non-perturbative SM charm loops)

see also CRIVELLIN ET AL (2018)

# Popular NP models

## Variety of NP models on the market

- tree-level flavour changing  $Z'$  ALTMANNSHOFER, STRAUB (2013); GAULD ET AL (2013)  
ALTMANNSHOFER ET AL (2014); CRIVELLIN ET AL (2015)...
- loop-induced NP BELANGER ET AL (2015); GRIPAIS ET AL (2015); ARNAN ET AL (2016)  
KAMENIK ET AL (2017)
- leptoquarks HILLER, SCHMALTZ (2014); ALONSO ET AL (2015); CRIVELLIN ET AL (2015)  
FAJFER, KOSNIK (2015); BECIREVIC ET AL (2016)...

## Most popular (subject to personal taste): $SU(2)_L$ -singlet vector leptoquark $U_1$

- least constrained by complementary data (e. g.  $B_s$  mixing, direct searches)
- potential common origin of  $R(K^{(*)})$  and  $R(D^{(*)})$  anomalies
- contained in the Pati-Salam gauge group  $SU(4) \times SU(2)_L \times SU(2)_R$

## ➤ plenty of model-building effort for UV-complete model

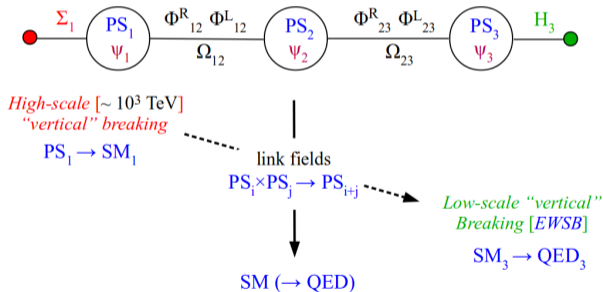
BARBIERI, MURPHY, SENIA (2016); DI LUZIO, GRELJO, NARDECCHIA (2017); CALIBBI, CRIVELLIN, LI (2017)  
BORDONE, CORNELLA, FUENTES-MARTIN, ISIDORI (2017); MB, CRIVELLIN (2018); GRELJO, STEFANEK (2018)  
HEECK, TERESI (2018); BALAJI, FOOT, SCHMIDT (2018)...

# PS<sup>3</sup> – a leptoquark model for flavour hierarchies

## PS<sup>3</sup> in a nutshell

- three copies of PS gauge group for each fermion generation
- cascade of symmetry breakings generates flavour hierarchy in leptoquark couplings
- SM Yukawa couplings governed by same hierarchies as  $U_1$  couplings

BORDONE, CORNELLA, FUENTES-MARTIN, ISIDORI (2017)  
model sketch from ISIDORI, CKM'18



# Complementary $U_1$ leptoquark signatures – flavour physics

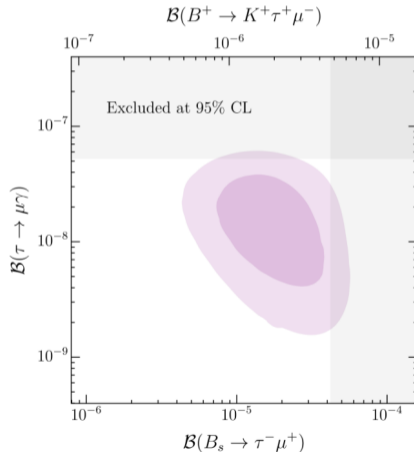
CORNELLA, FAROUGHY, FUENTES-MARTIN, ISIDORI, NEUBERT (2021)  
see also ANGELESCU ET AL. (2021)

## UV-insensitive observables

- Lepton flavour violating decays  
 $B \rightarrow K^{(*)}\tau\mu$ ,  $B_s \rightarrow \mu^+\tau^-$ ,  $\tau \rightarrow \mu\gamma\dots$
- di-tau final states  
 $B_s \rightarrow \tau^+\tau^-$ ,  $B \rightarrow K^{(*)}\tau^+\tau^-$

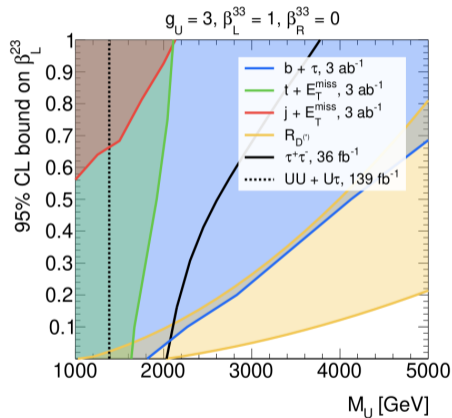
## Depending on UV-completion (loop-induced)

- $B_s - \bar{B}_s$  mixing
- $B \rightarrow K^{(*)}\nu\bar{\nu}$
- $D - \bar{D}$  mixing



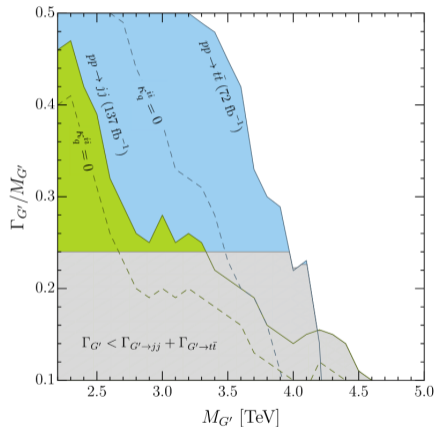
# Complementary $U_1$ leptoquark signatures – LHC

## $U_1$ pair and resonant production



HAISCH, POLESELLO (2020)

## Coloron $t\bar{t}, jj$ resonances



CORNELLA ET AL. (2021)



# The Cabibbo angle anomaly

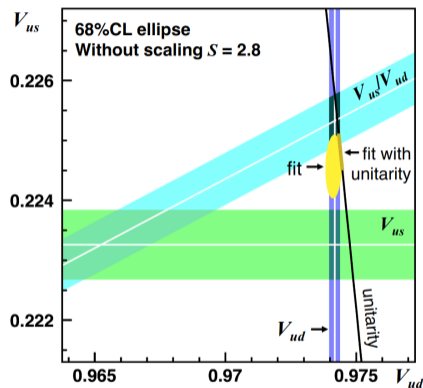
## Test of first-row CKM unitarity

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 < 1 \quad (\sim 3\sigma)$$

## Possible NP influence

- New Physics in nuclear  $\beta$  decay
- New Physics in  $G_F$  from  $\mu \rightarrow e\nu\bar{\nu}$
- violation of LFU in  $W_{\mu\nu}$  coupling

➤ connection to  $R(K^{(*)})$ ?



BELFATTO ET AL. (2019); GROSSMAN, PASSEMAR, SCHACHT (2019)  
KIRK (2020); CRIVELLIN, HOFERICHTER, MANZARI (2021) ...

# Common origin of the Cabibbo angle and $R(K^{(*)})$ anomalies?

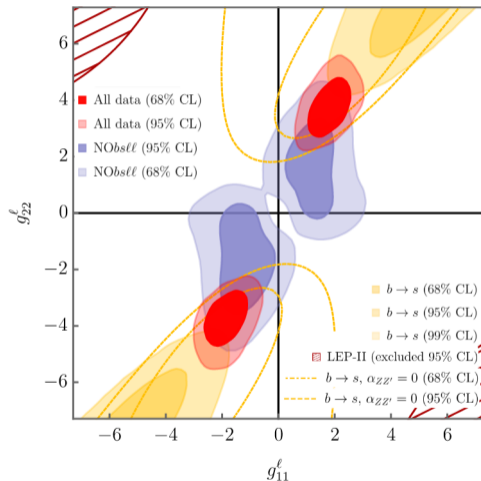
CAPDEVILA, CRIVELLIN, MANZARI, MONTULL (2020)

## Simplified model

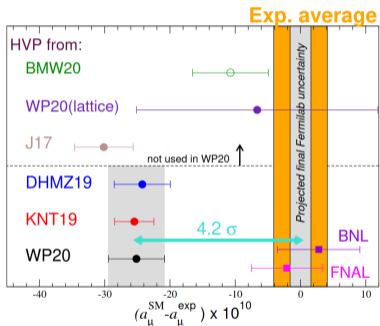
spin-1  $SU(2)$ -triplet with flavour-specific couplings

- $W$ - $W'$  mixing modifies  $W_{\mu\nu}$  coupling
- significant  $Z'$  contribution to  $b \rightarrow sl^+l^-$

- parameter regions resolving anomalies overlap: **good overall fit**
- **correlations** predicted between observables  
e.g.  $R(K^*)$  and  $\pi \rightarrow \mu\nu/e\nu$



# The $(g - 2)_\mu$ anomaly



## 4.2 $\sigma$ tension in muon $(g - 2)$

### Experiment

- recent **FNAL result** confirmed BNL result
- significant reduction of uncertainties with larger dataset
- upcoming J-PARC experiment to measure  $g - 2$  with different method

### SM prediction

- **consensus by  $g - 2$  theory initiative** ➤ whitepaper 2020
- tension reduced by recent lattice determination of **hadronic vacuum polarisation**, but inconsistent with global EW fit

CRIVELLIN ET AL. (2020)

## New Physics options for $(g - 2)_\mu$

Observed anomaly requires **NP contribution of similar size as SM EW contribution**

### Heavy ( $\gtrsim$ EW scale) New Physics

chiral enhancement required to avoid  $m_\mu$  suppression

- SUSY: enhancement by  $\tan\beta \sim 50$
- leptoquarks: enhancement by  $m_t/m_\mu \sim 1600$
- ...

### Light New Physics

enhanced by scale ratio  $\Lambda_{EW}/\Lambda_{NP}$

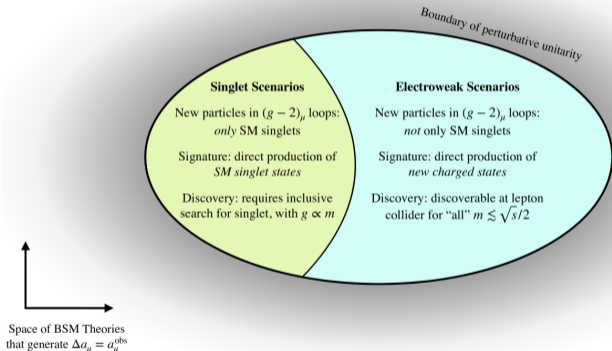
- axion/ALP models
- light scalars
- light  $Z'$
- ...

# $(g - 2)_\mu$ – a no-lose theorem for muon colliders

## Path to NP discovery

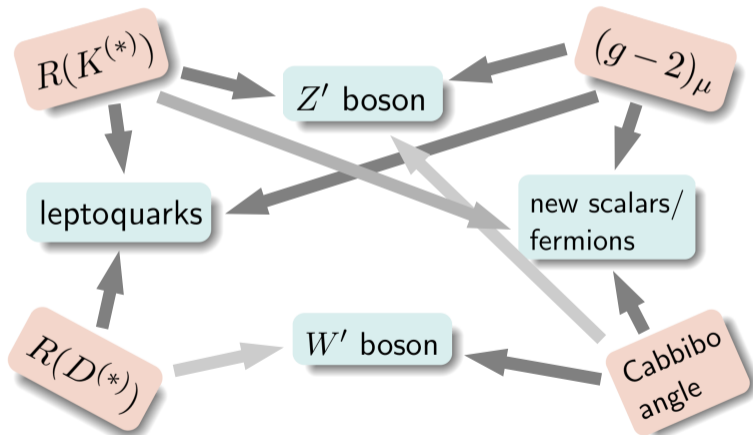
- 1 discover/falsify **low-scale EW singlet scenario** at fixed-target experiments & Belle II
- 2 discover/falsify **any singlet scenario** at 3 TeV muon collider
- 3 discover **EW scenarios**  $\lesssim 10$  TeV via direct NP production at 10 TeV muon collider
- 4 probe **unitarity ceiling** ( $\lesssim 100$  TeV) through  $\mu^+ \mu^- \rightarrow h\gamma$

CAPDEVILLA, CURTIN, KAHN, KRNJAC (2021)



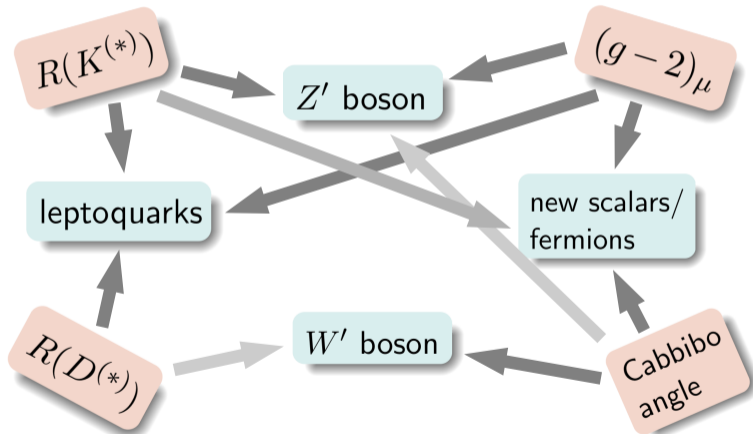
**Note:** muon collider also tests NP in  $b \rightarrow s\mu^+\mu^-$ !

# Towards combined explanations – model building 101

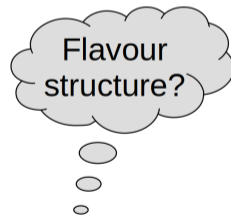


see also CRIVELLIN, LHCP'21

# Towards combined explanations – model building 101



see also CRIVELLIN, LHCP'21



## Summary & outlook

- various intriguing **anomalies** in observables testing **lepton flavour universality**
- resolution requires **TeV-scale New Physics** (or lighter)
- **complementary probes** in
  - related flavour observables
  - high- $p_T$  collider data
  - Dark Matter phenomenologydistinguish between underlying NP scenarios



## Summary & outlook

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